CMPT 473 Software Testing, Reliability and Security Input Space Partitioning

Nick Sumner



- Testing involves running software and comparing observed behavior against expected behavior
 - Select an input, look at the output

Recall

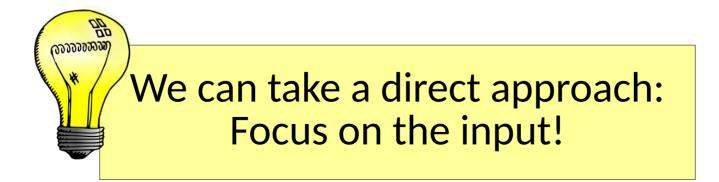
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What does this show? What does it *not* show?

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- e.g. abs(x)

Input Domain: ..., -3, -2, -1, 0, 1, 2, 3, ...

How many tests if done exhaustively?

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Input Domain:	, -3, -2, -1, 0, 1, 2, 3,
Partitions:	, -3, -2, -1, 0, 1, 2,
	3,
	What might reasonable partitions be?

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Input Domain:

Partitions:

How many tests for the partitions?

1) Identify the component



- 1) Identify the component
 - Whole program
 - Module
 - Class
 - Function



- 1) Identify the component
- 2) Identify the inputs / parameters





1) Identify the component

2) Identify the inputs / parameters

- Function/method parameters
- Object state
- Global variables
- File contents
- User provided inputs
- ...

$$x \in \mathbb{Z}$$

- 1) Identify the component
- 2) Identify the inputs / parameters
- 3) Develop an *input domain model* for input characteristics*

A way of partitioning the input space

$$abs(x) \qquad \begin{array}{c} x \in \mathbb{Z} \\ x < 0 \\ x = 0 \\ x > 0 \end{array}$$

- 1) Identify the component
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- 4) Refine combinations with constraints*

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$$x \in \mathbb{Z}$$
 $x < 0$ frame 1: $x < 0$ $x = 0$ frame 2: $x = 0$ $x > 0$ frame 3: $x > 0$

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- 6) Select concrete inputs*

abs(x)
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frame 1: x < 0 frame 2: x = 0 frame 3: x > 0

- test 1: abs(-3) = 3
- test 2: abs(0) = 0
- test 3: abs(7) = 7

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4) Refine c * some parts are more subtle than they appear

5) Generate combinations / test frames

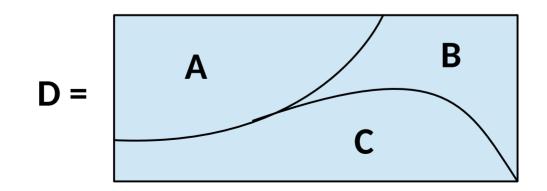
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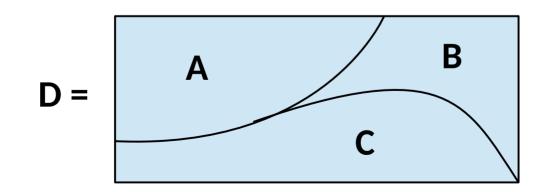
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• *Partition* a domain D on *characteristics*

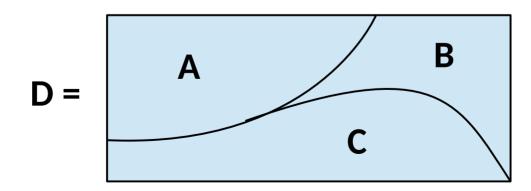


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What do these criteria intuitively provide?



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(|s| ≥ 2, ∄k...)

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- |s| < 2
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Reference **x** is null (boolean)

Size of string **s** (non-boolean)

- 0
- 1
- 2
- 2 < |s| < 1024
- |s| ≥ 1024

Input Domain Modeling: Partitioning Practice

• Suppose we have

```
classifyParallelogram(p1: Parallelogram) -> Kind
```

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- In class exercise: Suppose we have

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what should partitions be?

Input Domain Modeling – Choosing Characteristics

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2 main approaches:

- Interface based
 - Guided directly by identified parameters & domains
 - Simple
 - Automatable
- Functionality/Requirements based
 - Derived from expected input/output relationship by spec.
 - Requires more design & more thought
 - May be better (smaller, goal oriented, ...)

Input Domain Modeling – Interface Based

- Consider parameters individually
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 - Ignore relationships & dependencies

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How does this apply to our triangle classifier?

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How does this apply to our triangle classifier?

classifyTriangle(s1: int, s2: int, s3: int) -> Kind

$$\begin{array}{c|cccc} s1 \in \mathbb{Z} & s2 \in \mathbb{Z} & s3 \in \mathbb{Z} \\ \hline s1 < 0 & s2 < 0 & s3 < 0 \\ s1 = 0 & s2 = 0 & s3 = 0 \\ s1 > 0 & s2 > 0 & s3 > 0 \end{array}$$

We will revisit how this is good / bad

- Characteristics correspond to behaviors in the requirements
 - Includes knowledge from the problem domain
 - Accounts for relationships between parameters

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classifyTriangle(s1: int, s2: int, s3: int) -> Kind

<u>Kind</u> Scalene Isosceles - Equilateral Equilateral Invalid

- Component specifications
 - Preconditions
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- Component specifications
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- Domain knowledge
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- Checklists [Langr, Hunt, Thomas]
 - Correctness
 - Ordering
 - Range
 - Reference
 - Existence
 - Cardinality
 - Time

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- We can plan our tests by creating *test frames* that identify the combinations of partitions used in each abstract / planned test.

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classifyTr	iangle(s1:	<pre>int, s2:</pre>	<pre>int, s3: int)</pre>	-> Kind
	_s1∈ℤ	s2 ∈ ℤ	s3 ∈ ℤ	
	s1 < 0	s2 < 0	s3 < 0	
	s1 = 0	s2 = 0	s3 = 0	
	s1 > 0	s2 > 0	s3 > 0	

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classifyTriangle(s1: int, s2: int, s3: int) -> Kind $\frac{s1 \in \mathbb{Z}}{s1 < 0} \xrightarrow{s2 \in \mathbb{Z}} \frac{s3 \in \mathbb{Z}}{s3 < 0}$ $s1 = 0 \qquad s2 = 0 \qquad s3 = 0$ $s1 > 0 \qquad s2 > 0 \qquad s3 > 0$ We need to choose a value for each side.

- We may have multiple ways / dimensions of partitioning.
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C	classifyTri	angle(s1:	int, s2: :	int, s3: in	nt) -> Kir	nd
		s1∈ℤ	s2 $\in \mathbb{Z}$	s3 ∈ ℤ		
		s1 < 0	s2 < 0	s3 < 0		
		s1 = 0	s2 = 0	s3 = 0		
		s1 > 0	s2 > 0	s3 > 0		
Frame 1	Frame 2	Frame 3	Frame 4	Frame 5	Frame 6	Frame
S1: s1 <	0 S1: s1 = 0	S1: s1 < 0	S1: s1 < 0	S1: s1 > 0	S1: s1 < 0	S1:
S2: s2 <	0 S2: s2 < 0	S2: s2 = 0	S2: s2 < 0	S2: s2 < 0	S2: s2 > 0	S2:
S3: s3 <	0 S3: s3 < 0	S3: s3 < 0	S3: s3 = 0	S3: s3 < 0	S3: s3 < 0	S3:

How many tests does this create?

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What will this test well? What won't this test well?

$$\begin{array}{c|c} \underline{s1 \in \mathbb{Z}} & \underline{s2 \in \mathbb{Z}} & \underline{s3 \in \mathbb{Z}} \\ \hline s1 < 0 & \underline{s2 < 0} & \underline{s3 < 0} \\ s1 = 0 & \underline{s2 = 0} & \underline{s3 = 0} \\ s1 = 1 & \underline{s2 = 1} & \underline{s3 = 1} \\ s1 > 1 & \underline{s2 > 1} & \underline{s3 > 1} \\ \left\{ sn > 0 \right\} \rightarrow \left\{ sn = 1 \right\}, \left\{ sn > 1 \right\} \end{array}$$

How many tests now?

Practical Issues: Interface Based

classifyTriangle(s1: int, s2: int, s3: int) -> Kind

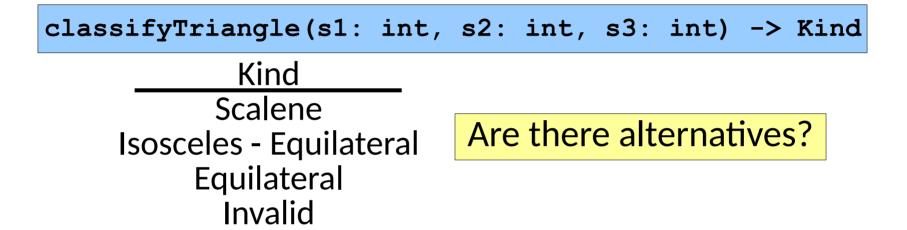
s1 $\in \mathbb{Z}$	$s2 \in \mathbb{Z}$	$s3 \in \mathbb{Z}$
s1 < 0	s2 < 0	s3 < 0
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y tests now?	Is it s	still disjoint? Complete?

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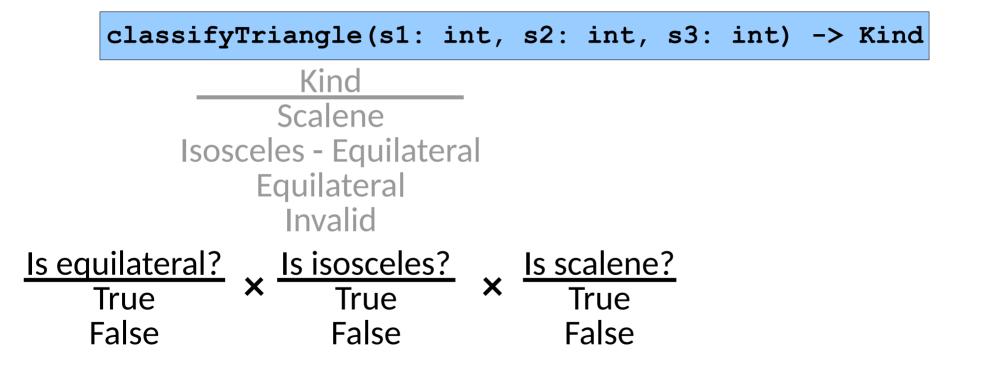
_s1 ∈ ℤ	s2 €	$\exists \mathbb{Z}$	$s3 \in \mathbb{Z}$	
s1 < 0	s2	< 0	s3 < 0	
s1 = 0	s2	= 0	s3 = 0	
s1 = 1	s2	= 1	s3 = 1	
s1 > 1	s2	> 1	s3 > 1	
How many tests now?		ls it s	still disjoint	? Complete?

What does it test well? Not well?

Practical Issues: Functionality Based



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classify!	[riangle(s1	: int,	s2:	int,	s3:	int)	->	Kind
ISOS	Kind Scalene celes - Equila Equilateral Invalid	ateral						
<u>Is equilateral?</u> True False	× Is isoscele True False	es? ×	-	calene True False	?			
<u>Frame 1</u> Is Eq: False Is Iso: False Is Sc: False	<u>Frame 2</u> Is Eq: True Is Iso: False Is Sc: False	Frame Is Eq: Is Iso: Is Sc:		Why	mig	<mark>ht yo</mark>	<mark>u u</mark> s	se it?

Another Functionality Based Example

• Suppose we have a simple function:

symmetricDifference(s1: list, s2: list) -> list

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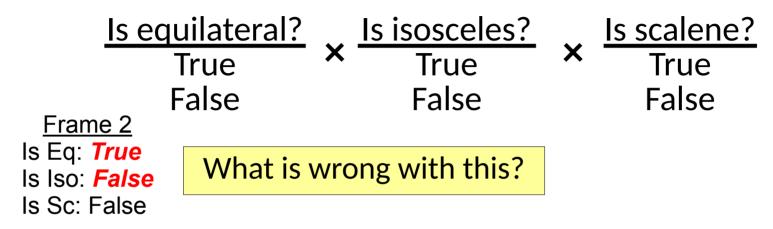
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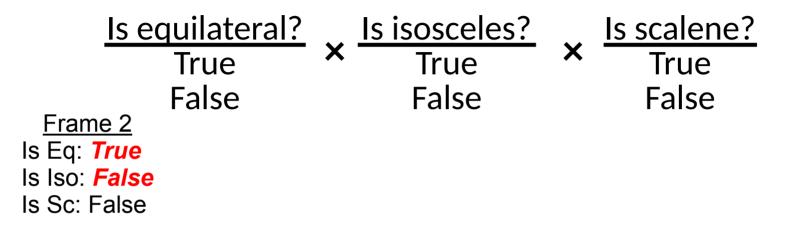
- Try to construct a functionality based input domain model.
- Keep disjointness and coverage in mind.

Try it out, and we'll discuss

Refining Combinations with Constraints



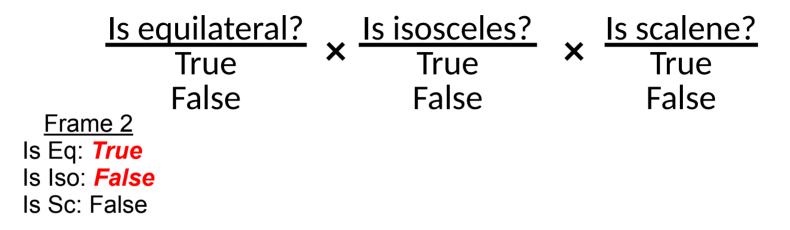
Refining Combinations with Constraints



We can add *properties* and *constraints* to prune impossible or redundant tests

Is equilateral?		Is isosceles?		<u>Is scalene?</u>
True [if Iso]	- X	True [property Iso]	— x	True [if not Iso]
False		False		False

Refining Combinations with Constraints



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[Error] annotations can identify cases not benefiting from combinations • In theory, any value in a partition can represent it. (equivalence classes)

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```
void toUppercase(char *str) {
   for (int i = 0, e = strlen(str) - 1; i < e; ++i) {
      if (isletter(str[i]) && islower(str[i])) {
        str[i] = str[i] - 32;
      }
   }
   printf("%s\n", str);
}</pre>
```

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 - This is the same reason we look for OBOEs (off by one errors)

Selecting Concrete Inputs

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- So we might consider
 - Expected values
 - Invalid, valid, and special values
 - Boundary values

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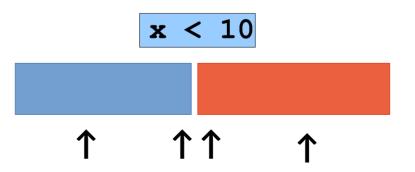
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abs(x) ..., -3, -2, -1, 0, 1, 2,

$$\uparrow^{3, \dots} \uparrow \uparrow \uparrow$$

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Command FIND

Syntax FIND <pattern> <file>

Function The FIND command is used to locate one or more instances of a given pattern in a text file. All lines in the file that contain the pattern are written to standard output. A line containing the pattern is written only once, regardless of the number of times the pattern occurs on it.

The pattern is any sequence of characters whose **length does not exceed** the maximum length of a line in the file. To include a blank in the pattern, the entire pattern must be **enclosed in quotes (")**. To include a quotation mark in the pattern, **two quotes in a row ("")** must be used.

Part 1: Analyze the specification

- What is the component?
- What are the *parameters*?
- What are the characteristics?

Command Syntax	Parameters: Pattern Input file (& its contents!)
Function	The FIND command is used to locate one or more instances of a given pattern in a text file . All lines in the file that contain the pattern are written to standard output. A line containing the pattern is written only once , regardless of the number of times the pattern occurs on it.
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Command Syntax	Parameters: Pattern Input file (& its contents!)	
Function	Characteristics: Pattern Input file Pattern Size Quoting Embedded Quotes File Name Environment / System Characteristics:	es of a given ittern are written only s on it. bes not exceed in the pattern, de a quotation d.
	<pre># of pattern occurrences in file # of occurrences on a particular line: the component: re the parameters?</pre>	

- What are the *characteristics*?

- Part 2: Partition the Input Space
 - Guided by intelligence and intuition
 - Combine interface and functionality based approaches as necessary

```
Parameters:

Pattern Size:

Empty

Single character

Many characters

Longer than any line in the file

Quoting:

...
```

• Part 3: Refine with constraints

Pattern size : empty Quoting : pattern is quoted Embedded blanks : several embedded blanks Embedded quotes : no embedded quotes File name : good file name Number of occurrences of pattern in file : none Pattern occurrences on target line : one

• Part 3: Refine with constraints

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Pattern size : empty	Problem?		
Pattern Size:			
Empty	[Property Empty]		
Single character	[Property NonEmpty]		
Many characters	[Property NonEmpty]		
Longer than any line in the file	[Property NonEmpty]		
Dettern commences on terret line , and			

Pattern occurrences on target line : one

• Part 3: Refine with constraints

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Pattern Size:	
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Longer than any line in the file	[Property NonEmpty]
Quoting:	
Pattern is quoted	[Property Quoted]
Pattern is not quoted	[If NonEmpty]
Pattern is improperly quoted	[If NonEmpty]

• Part 3: Refine with constraints

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What should this do to the number of tests? To the quality of tests?

- Part 4:
 - Generate test frames.
 - Analyze.
 - Select concrete values and tests.
 - Prune redundant tests.

Why might scenarios be redundant?

- Part 4:
 - Generate test frames.
 - Analyze.
 - Select concrete values and tests.
 - Prune redundant tests.

• Then take your tests and automate them



- Partition based testing allows for testing software without detailed knowledge of its implementation
- Careful design of an input domain model helps ensure useful tests and avoid less useful tests
- The assumption of equivalence in a partition is a convenience.