CMPT 473 Software Quality Assurance Scale & Combinatorial Testing

Nick Sumner material from Ammonn & Offutt

- Consider our triangle classifier
 - Takes 3 integers for sides 1, 2, & 3

Characteristic	b1	b2	b3
Side 1 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
Side 3 0	Side 3 > 0	Side 3 = 0	Side 3 < 0

3 guiding questions...

- Consider our triangle classifier
 - Takes 3 integers for sides 1, 2, & 3

Characteristic	b1	b2	b3
Side 1 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
Side 3 0	Side 3 > 0	Side 3 = 0	Side 3 < 0

How many tests does this create?

- Consider our triangle classifier
 - Takes 3 integers for sides 1, 2, & 3

Characteristic	b1	b2	b3
Side 1 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
Side 3 0	Side 3 > 0	Side 3 = 0	Side 3 < 0

How many tests does this create?

What will this test well? What won't this test well?

- Consider our triangle classifier
 - Takes 3 integers for sides 1, 2, & 3

Characteristic	b1	b2	b3
Side 1 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
Side 3 0	Side 3 > 0	Side 3 = 0	Side 3 < 0

How many tests does this create?

What will this test well? What won't this test well?

Recall from Last Time (part 2)

• We can subdivide partitions to cover more behavior

Characteristic	b1	b2	b3	b4
Value of side 1	Side 1 > 1	Side 1 = 1	Side 1 = 0	Side 1 < 0
Value of side 2	Side 2 > 1	Side 2 = 1	Side 2 = 0	Side 2 < 0
Value of side 3	Side 3 > 1	Side 3 = 1	Side 3 = 0	Side 3 < 0

How many tests now?

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

• How does the number of tests change?

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

- How does the number of tests change?
- $|D_1| * |D_2| * |D_3| * ... * |D_n| = k^n$
- This is combinatorial explosion

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

- How does the number of tests change?
- $|D_1| * |D_2| * |D_3| * ... * |D_n| = k n$
- This is combinatorial explosion

What does it mean in practice?

• Find command: 4x3x3x3x3x3x2 = 1944 tests

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

- How does the number of tests change?
- $|D_1| * |D_2| * |D_3| * ... * |D_n| = k^n$
- This is combinatorial explosion
- What does it mean in practice?
 - Find command: 4x3x3x3x3x3x2 = 1944 tests
- Website generator: > $30 \rightarrow$ > 1 billion tests

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

- How does the number of tests change?
- $|D_1| * |D_2| * |D_3| * ... * |D_n| = k^n$
- This is combinatorial explosion

What does it mean in practice?

- Find command: 4x3x3x3x3x3x2 = 1944 tests
- Website generator: > $30 \rightarrow$ > 1 billion tests

Too many to maintain!

Suppose inputs or characteristics I_1 , I_2 , I_3 , ..., I_n

- How does the number of tests change?
- $|D_1| * |D_2| * |D_3| * ... * |D_n| = k n$
- This is combinatorial explosion

What does it mean in practice?

- Find command: 4x3x3x3x3x3x2 = 1944 tests
- Website generator: > $30 \rightarrow$ > 1 billion tests

Too many to maintain!

Too many to reasonably even create!

• What did the input partitioning do?

- What did the input partitioning do?
 - Constraints

Pattern Size: Empty Single character Many characters Longer than any line in the file	<pre>[Property Empty] [Property NonEmpty] [Property NonEmpty] [Property NonEmpty]</pre>
Quoting: Pattern is quoted	[Property Quoted]

Pattern is not quoted Pattern is improperly quoted

[If NonEmpty] [If NonEmpty]

- What did the input partitioning do?
 - Constraints
 - [property] to identify rules for useful tests
 - [error] to identify when 1 test for a block is sufficient

Pattern Size:	
Empty	[Property Empty]
Single character	[Property NonEmpty]
Many characters	[Property NonEmpty]
Longer than any line in the file	[Property NonEmpty]
Quoting	

Quoting:				
Pattern	is	quoted		[Property Quo
Pattern	is	not quoted		[If NonEmpty]
Pattern	is	improperly	quoted	[If NonEmpty]
				L

Quoted]

- What did the input partitioning do?
 - Constraints
 - [property] to identify rules for useful tests
 - [error] to identify when 1 test for a block is sufficient
- What else might we do?

- What did the input partitioning do?
 - Constraints
 - [property] to identify rules for useful tests
 - [error] to identify when 1 test for a block is sufficient
- What else might we do?
 - Not test as thoroughly (sampling)

Why might this be okay?

- What did the input partitioning do?
 - Constraints
 - [property] to identify rules for useful tests
 - [error] to identify when 1 test for a block is sufficient
- What else might we do?
 - Not test as thoroughly (sampling)
 - Identify related variables/domains & test together

Why would this lead to fewer tests?

Choosing Combinations

Several possible strategies:

• All Combinations

Choosing Combinations

Several possible strategies:

- All Combinations
 - Every combination of every block is tried
 - Leaps headfirst into combinatorial explosion

Choosing Combinations

Several possible strategies:

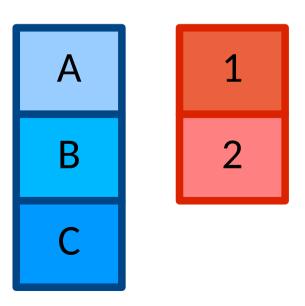
- All Combinations
 - Every combination of every block is tried
 - Leaps headfirst into combinatorial explosion

But is it inherently bad?

• How can we minimize #tests and still test each block?

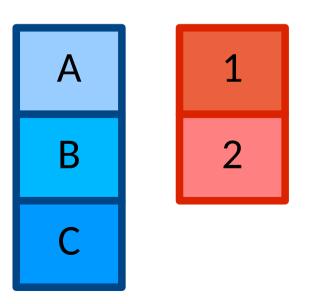
- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test



Adequate Tests:

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test



Adequate Tests: (A,1), (B,2), (C,1)

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test

What does this look like for the triangle classifier?

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test

What does this look like for the triangle classifier?

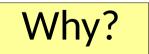
Are these tests good? Why?

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test

How many tests?

- How can we minimize #tests and still test each block?
- Each Choice
 - 1 value from each block used in at least one test
 - # tests = maximum number of blocks

How many tests?

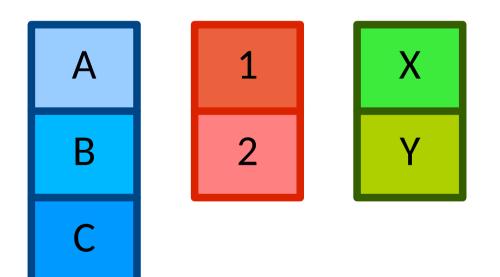


Combinations – ???

• Can we come up with a compromise?

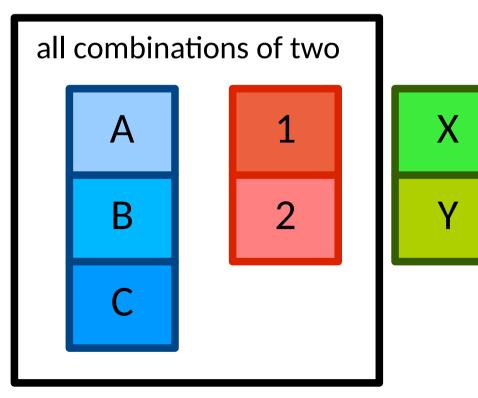
- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block



Adequate Tests:

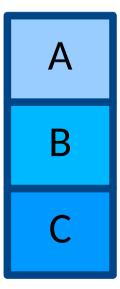
- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block

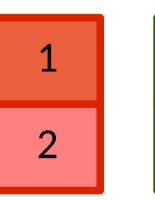


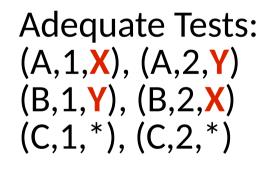
Adequate Tests: (A,1,*), (A,2,*) (B,1,*), (B,2,*) (C,1,*), (C,2,*)

X

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block





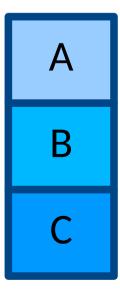


Fill in X and Y to make sure all pairwise combos are tested!

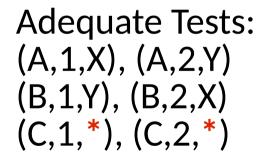
X

V

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block







What should the last two be?

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block

What does this look like for the triangle classifier?

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block

What does this look like for the triangle classifier?

Are these tests good? Why?

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block
 - #tests \geq product of 2 largest domain partitionings

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block
 - #tests \geq product of 2 largest domain partitionings

- Can we come up with a compromise?
- Pair Wise
 - 1 value for each block combined with 1 value for each other block
 - #tests \geq product of 2 largest domain partitionings

How many tests?

Expected on the order of $|D_1| * |D_2| * \log(n)$

Combinations - ???

• Can we extend this further?

- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics

- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics

- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics
 - #tests ≥ product of T largest domain partitionings

- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics
 - #tests ≥ product of T largest domain partitionings

What happens as T increases?

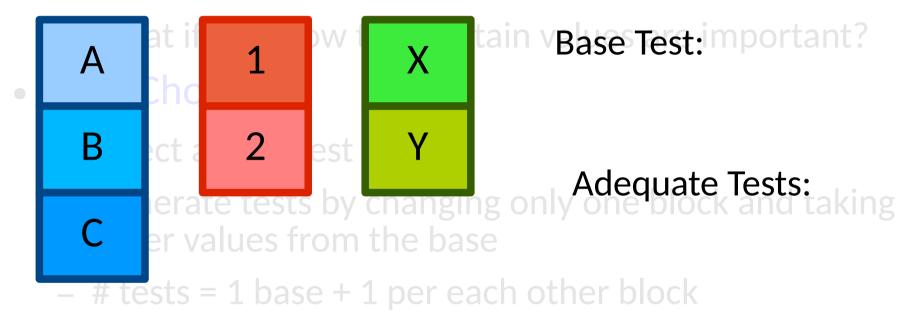
- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics
 - #tests \geq product of T largest domain partitionings
 - Bounded by (max number of blocks)^T
 - More expensive than pairs & uncertain gains

- Can we extend this further?
- T-wise
 - 1 value from each block for each group of T characteristics
 - #tests \geq product of T largest domain partitionings
 - Bounded by (max number of blocks)^T
 - More expensive than pairs & uncertain gains

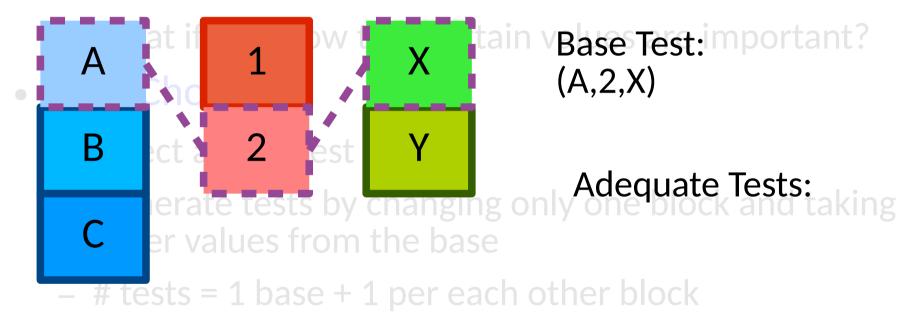
- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?

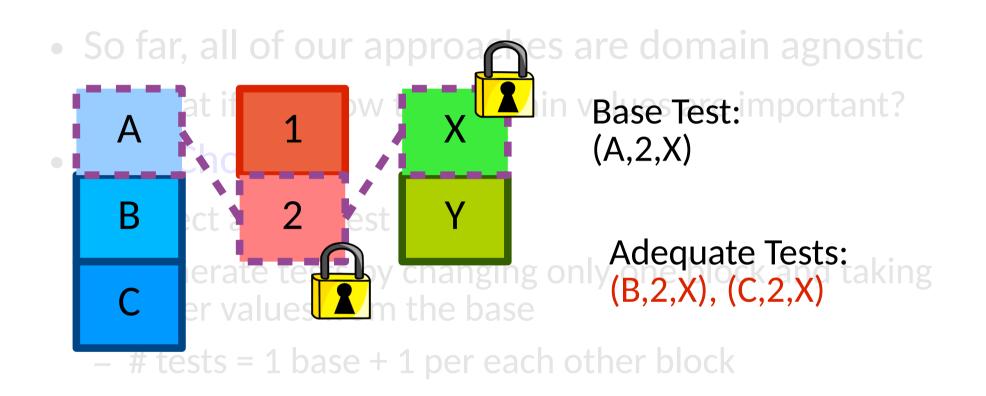
- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?
- Base Choice
 - Select a base test
 - Generate tests by changing only one block and taking other values from the base

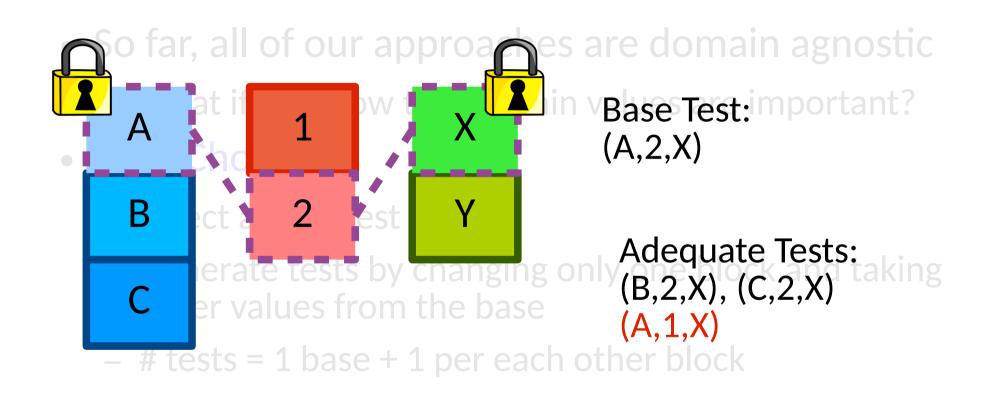
• So far, all of our approaches are domain agnostic

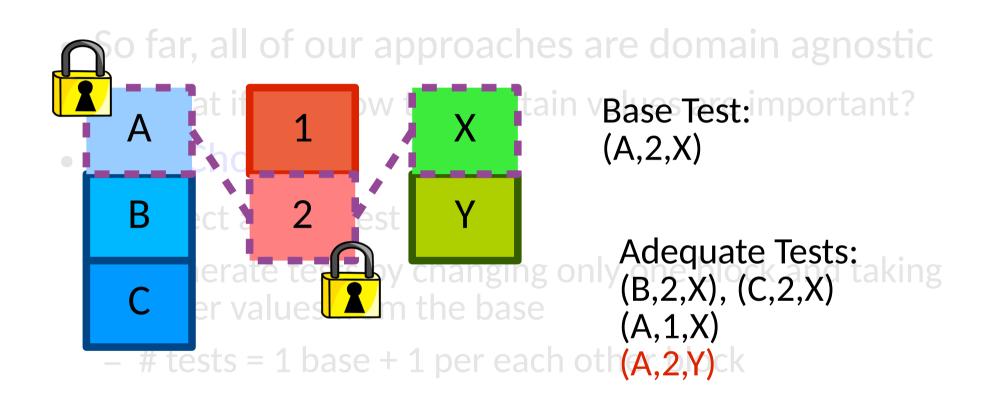


• So far, all of our approaches are domain agnostic

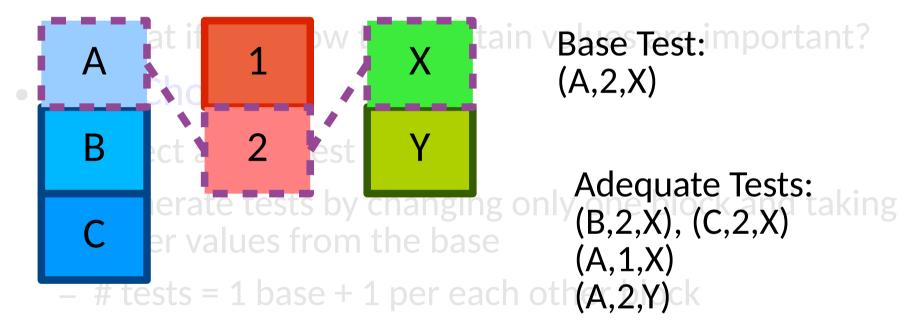








• So far, all of our approaches are domain agnostic



- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?
- Base Choice
 - Select a base test
 - Generate tests by changing only one block and taking other values from the base
 - # tests = 1 base + 1 per each other block

- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?
- Base Choice
 - Select a base test
 - Generate tests by changing only one block and taking other values from the base
 - # tests = 1 base + 1 per each other block

What does this look like for the triangle classifier?

- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?
- Base Choice
 - Select a base test
 - Generate tests by changing only one block and taking other values from the base
 - # tests = 1 base + 1 per each other block

What does this look like for the triangle classifier?

- So far, all of our approaches are domain agnostic
 - What if we know that certain values are important?
- Base Choice
 - Select a base test
 - Generate tests by changing only one block and taking other values from the base
 - # tests = 1 base + 1 per each other block

What does this look like for the triangle classifier?

Which test to use as a base is crucial

Why? What if we choose poorly?

Which test to use as a base is crucial

- Must at least be *feasible*
 - Do the combined values create a valid run?

Which test to use as a base is crucial

- Must at least be *feasible*
 - Do the combined values create a valid run?

How might we select a base test?

Base Choices

Which test to use as a base is crucial

- Must at least be feasible
 - Do the combined values create a valid run?
- Guided by:
 - Most likely?
 - Simplest?
 - Smallest?
 - Etc.

Base Choices

Which test to use as a base is crucial

- Must at least be feasible
 - Do the combined values create a valid run?
- Guided by:
 - Most likely?
 - Simplest?
 - Smallest?
 - Etc.
- Decision must be well understood & well maintained

Combinations - ???

- Notice the pattern.
 - Can base choices be extended?

- Notice the pattern.
 - Can base choices be extended?
- Multiple Base Choice
 - Select 1 or more base characteristics

- Notice the pattern.
 - Can base choices be extended?
- Multiple Base Choice
 - Select 1 or more base characteristics
 - Generate base tests by using each at least once

- Notice the pattern.
 - Can base choices be extended?
- Multiple Base Choice
 - Select 1 or more base characteristics
 - Generate base tests by using each at least once

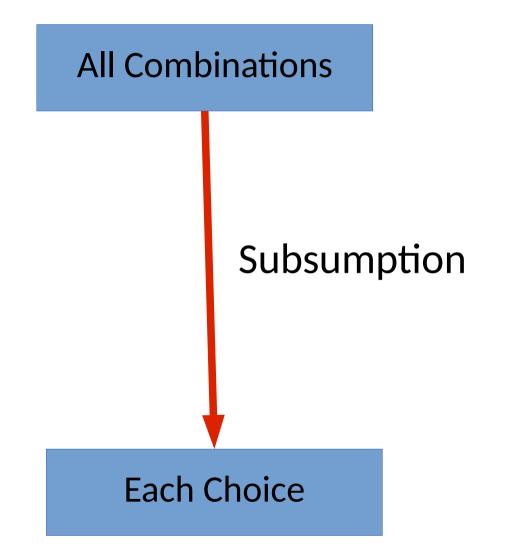
This yields a set of base tests

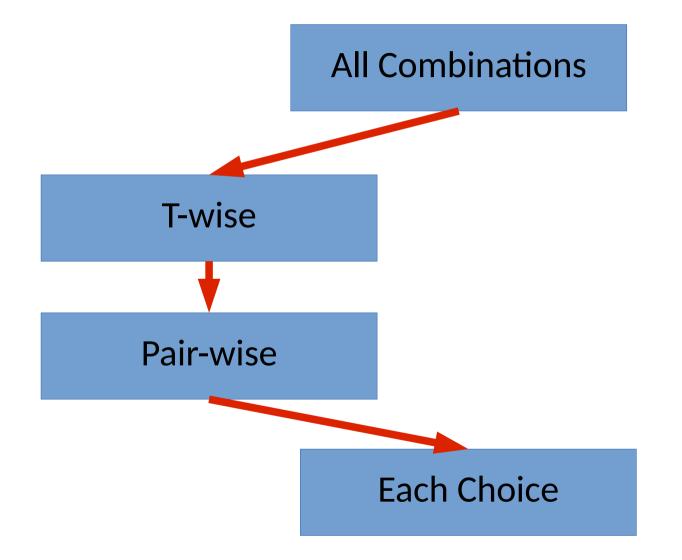
- Notice the pattern.
 - Can base choices be extended?
- Multiple Base Choice
 - Select 1 or more base characteristics
 - Generate base tests by using each at least once
 - Change 1 block at a time to an unselected one just as before

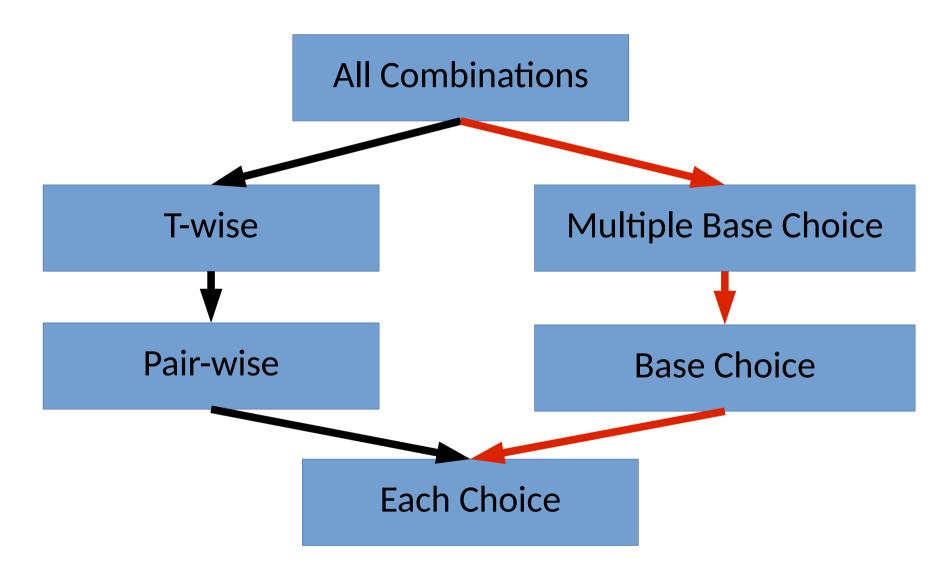
M base tests: M * $(1 + \sum |D_i-1|)$

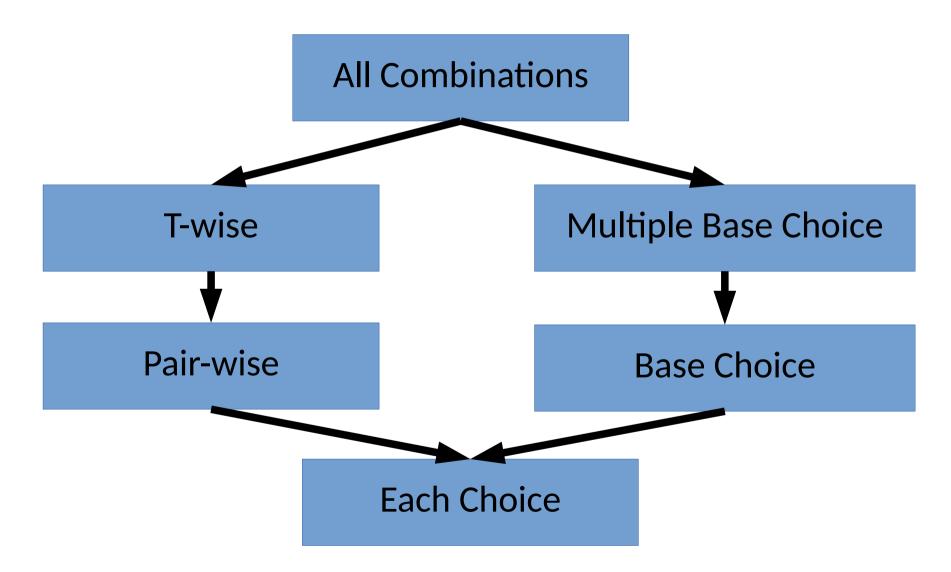
All Combinations

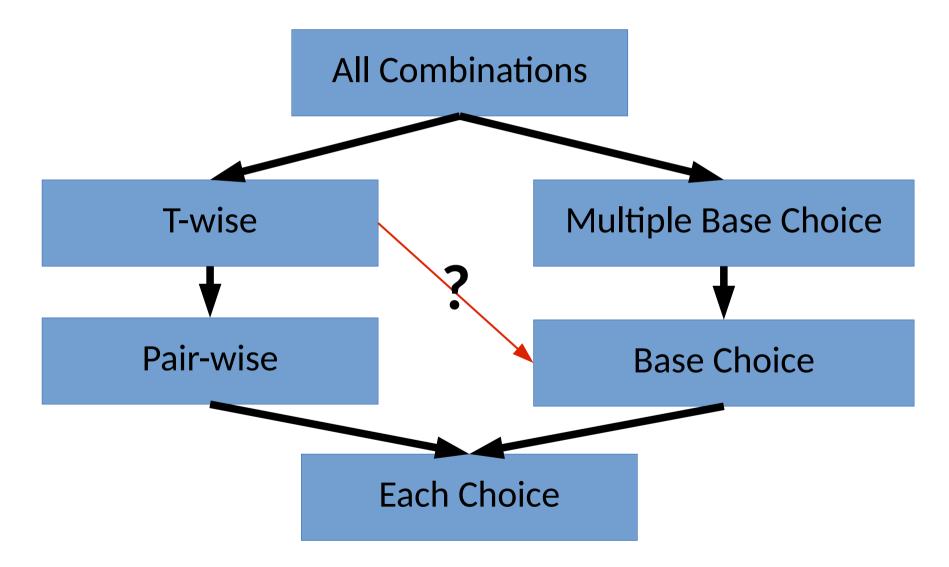
Each Choice

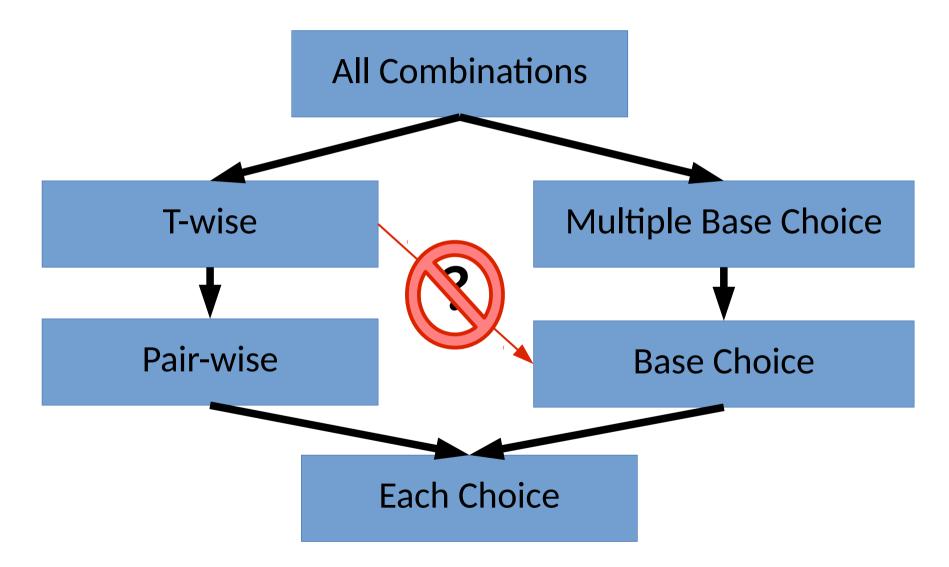










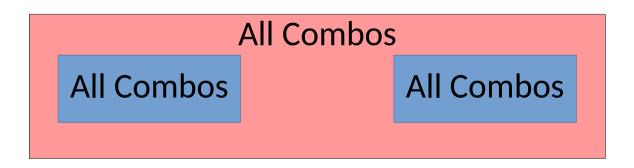


Using Your Intuition

• Broadly, some subset of inputs may interact, and some will be independent.

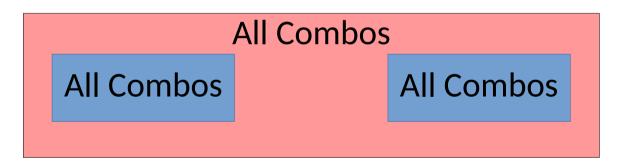
Using Your Intuition

- Broadly, some subset of inputs may interact, and some will be independent.
- Careful combinations of different approaches can yield more meaningful tests.



Using Your Intuition

- Broadly, some subset of inputs may interact, and some will be independent.
- Careful combinations of different approaches can yield more meaningful tests.



• And we have already seen another strategy for reducing test suites...

Remember the Constraints

- Constraints, and [error]s can reduce the # of tests further
 - No need to test invalid constraints
 - No need to test more than one [error]