# CMPT 473 Software Quality Assurance Scale & Combinatorial Testing

Nick Sumner material from Ammonn & Offutt

- Consider our triangle classifier
  - Takes 3 integers for sides 1, 2, & 3

Characteristic	b1	b2	b3
Side 1 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
Side 3 0	Side 3 > 0	Side 3 = 0	Side 3 < 0

3 guiding questions...

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## Recall from Last Time (part 2)

• We can subdivide partitions to cover more behavior

Characteristic	b1	b2	b3	b4
Value of side 1	Side 1 > 1	Side 1 = 1	Side 1 = 0	Side 1 < 0
Value of side 2	Side 2 > 1	Side 2 = 1	Side 2 = 0	Side 2 < 0
Value of side 3	Side 3 > 1	Side 3 = 1	Side 3 = 0	Side 3 < 0

How many tests now?

Suppose inputs or characteristics  $I_1$ ,  $I_2$ ,  $I_3$ , ...,  $I_n$ 

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What does it mean in practice?

• Find command: 4x3x3x3x3x3x2 = 1944 tests

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Too many to reasonably even create!

• What did the input partitioning do?

- What did the input partitioning do?
  - Constraints

Pattern Size: Empty Single character Many characters Longer than any line in the file	<pre>[Property Empty] [Property NonEmpty] [Property NonEmpty] [Property NonEmpty]</pre>
Quoting: Pattern is quoted	[Property Quoted]

Pattern is not quoted Pattern is improperly quoted

[If NonEmpty] [If NonEmpty]

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				<b>L</b>

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Why might this be okay?

- What did the input partitioning do?
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  - [property] to identify rules for useful tests
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- What else might we do?
  - Not test as thoroughly (sampling)
  - Identify related variables/domains & test together

Why would this lead to fewer tests?

## **Choosing Combinations**

Several possible strategies:

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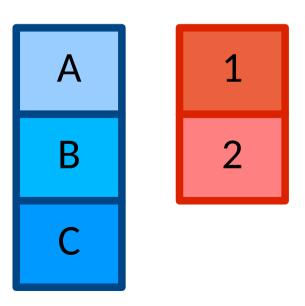
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But is it inherently bad?

• How can we minimize #tests and still test each block?

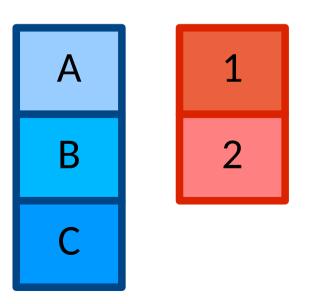
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Adequate Tests: (A,1), (B,2), (C,1)

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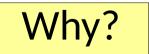
Are these tests good? Why?

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How many tests?

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  - 1 value from each block used in at least one test
  - # tests = maximum number of blocks

How many tests?

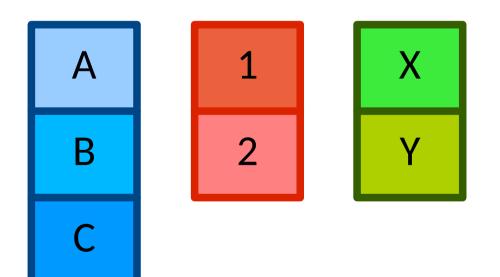


## Combinations – ???

• Can we come up with a compromise?

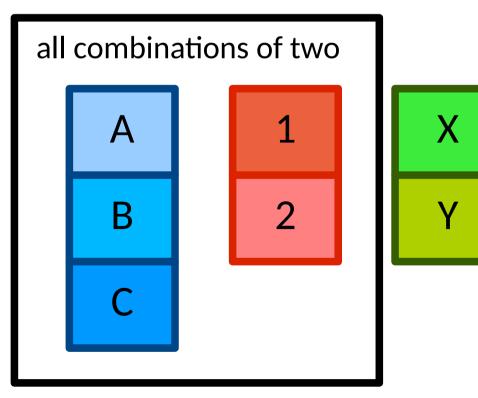
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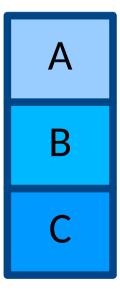
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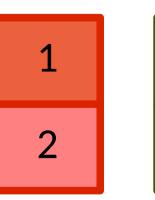


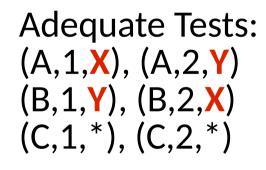
Adequate Tests: (A,1,\*), (A,2,\*) (B,1,\*), (B,2,\*) (C,1,\*), (C,2,\*)

X

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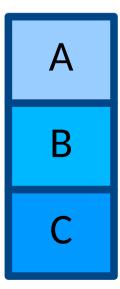


Fill in X and Y to make sure all pairwise combos are tested!

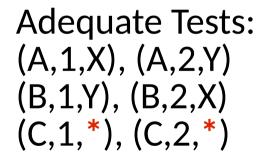
X

V

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What should the last two be?

- Can we come up with a compromise?
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How many tests?

Expected on the order of  $|D_1| * |D_2| * \log(n)$ 

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What happens as T increases?

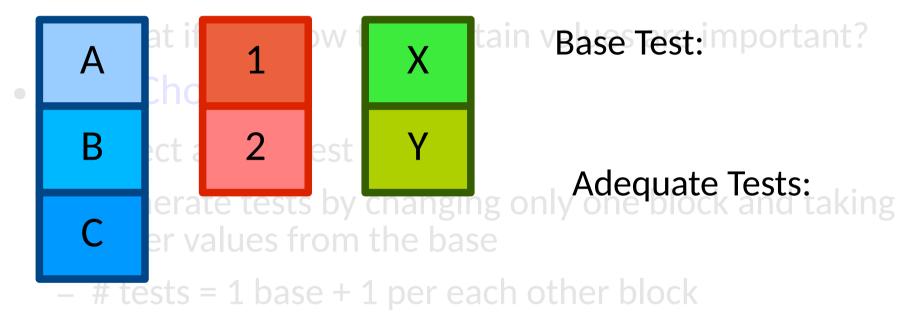
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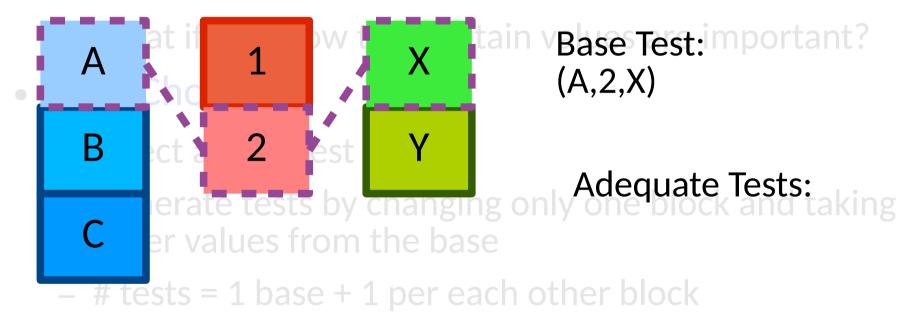
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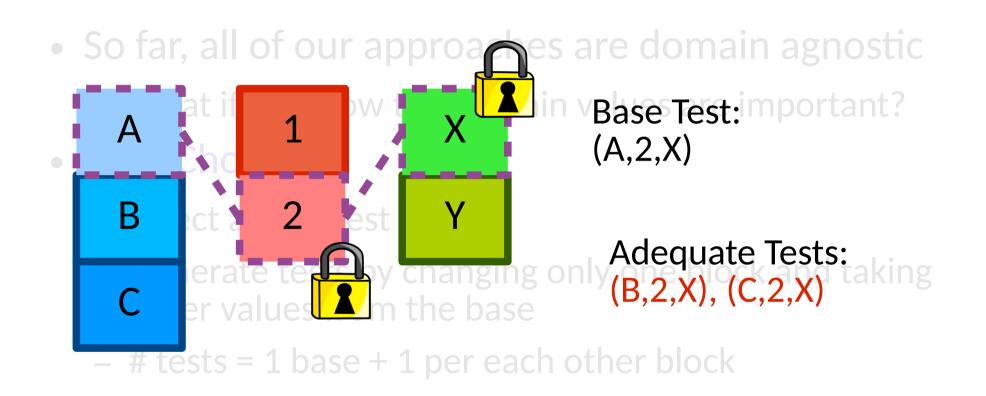
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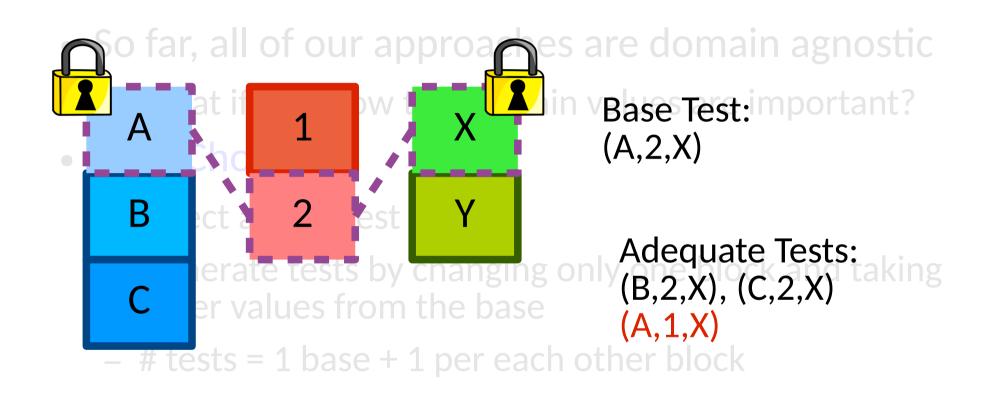
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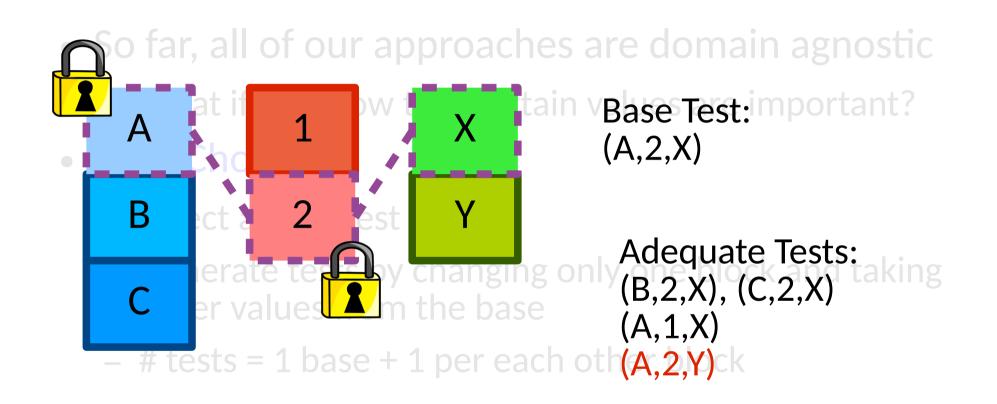


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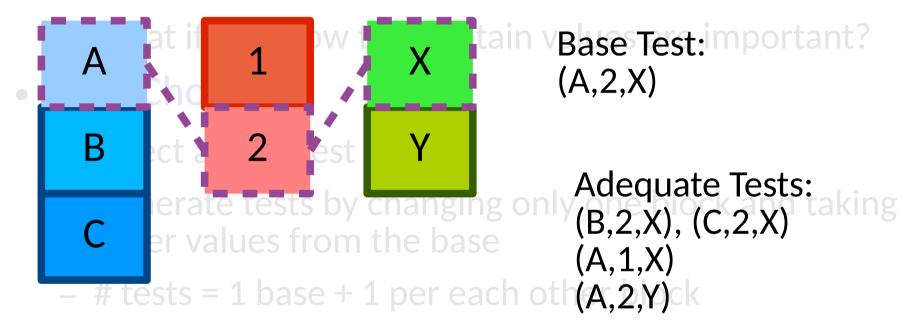








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Which test to use as a base is crucial

Why? What if we choose poorly?

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How might we select a base test?

## **Base Choices**

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- Must at least be feasible
  - Do the combined values create a valid run?
- Guided by:
  - Most likely?
  - Simplest?
  - Smallest?
  - Etc.

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- Must at least be feasible
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  - Etc.
- Decision must be well understood & well maintained

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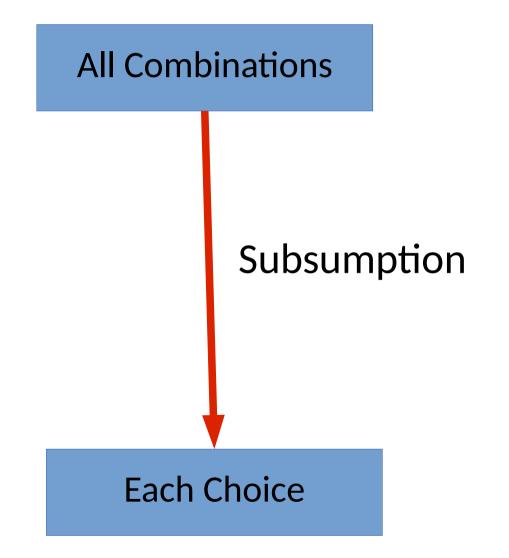
This yields a set of base tests

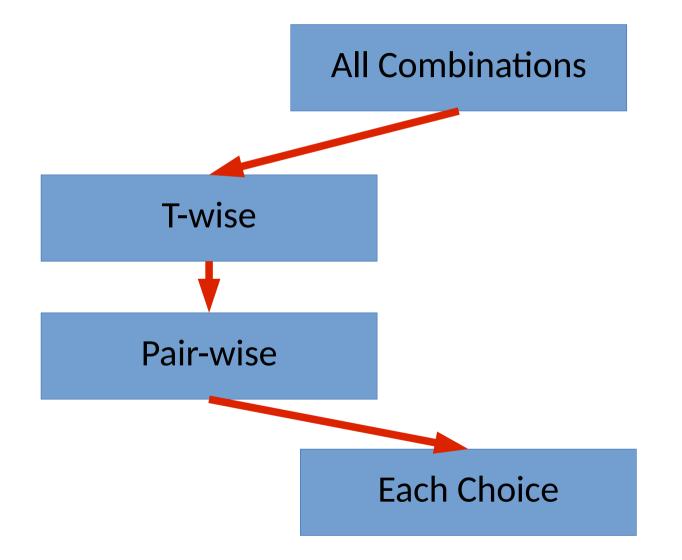
- Notice the pattern.
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  - Generate base tests by using each at least once
  - Change 1 block at a time to an unselected one just as before

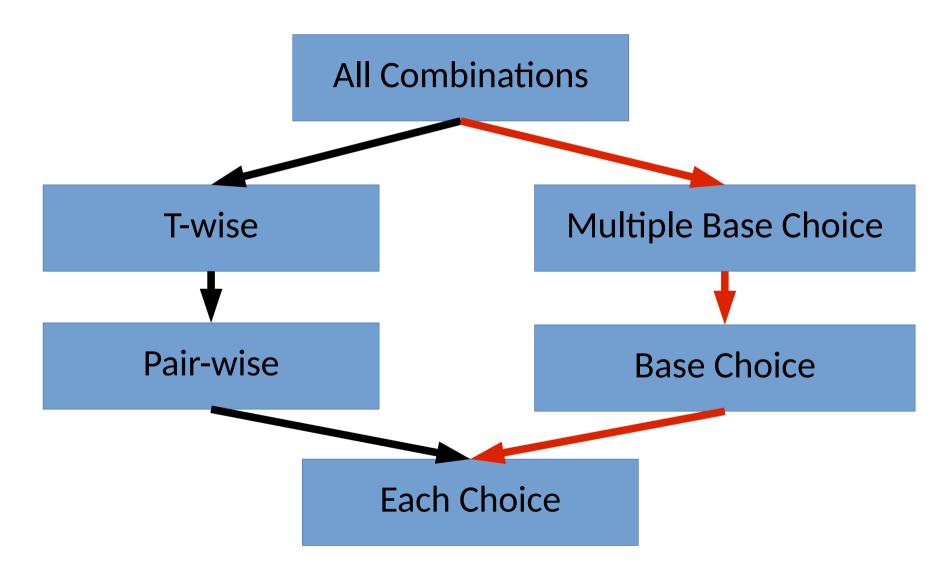
M base tests: M \*  $(1 + \sum |D_i-1|)$ 

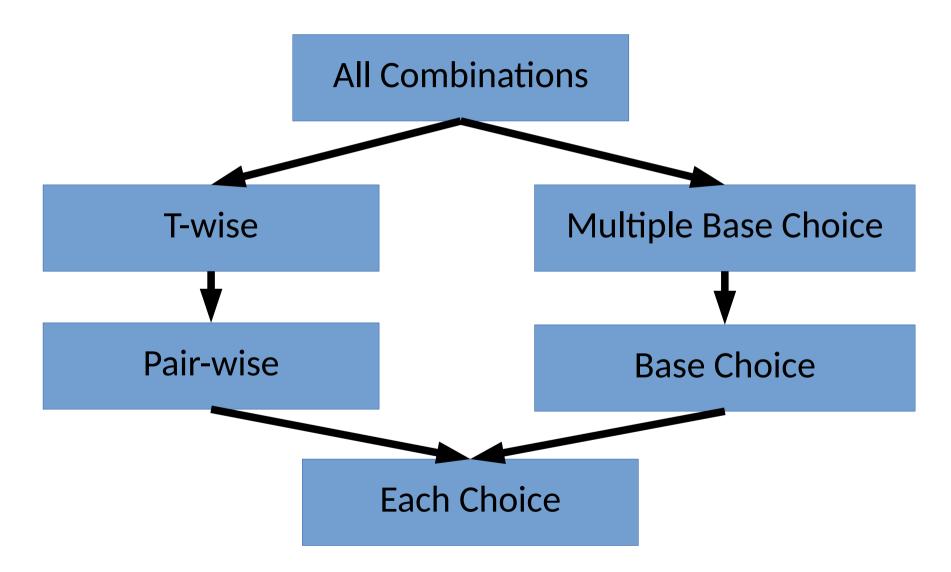
#### **All Combinations**

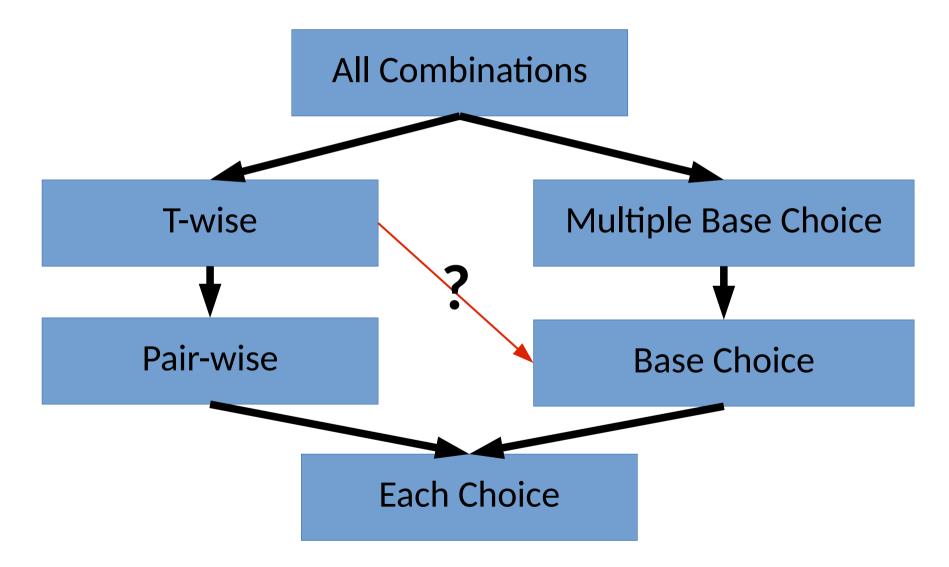
#### **Each Choice**

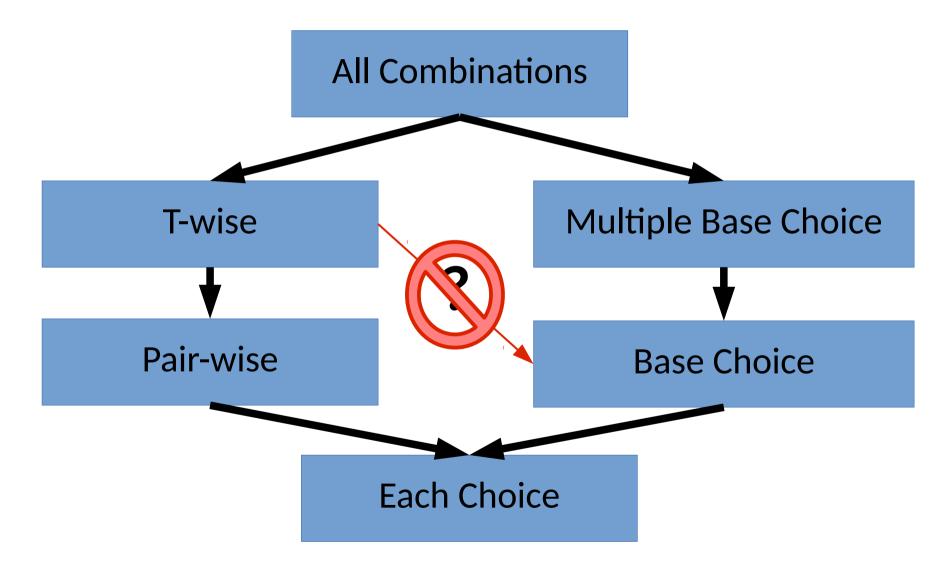










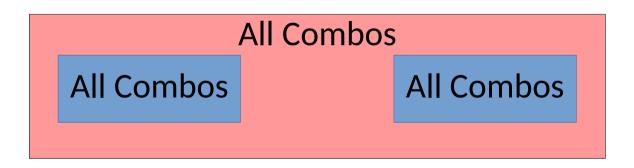


## **Using Your Intuition**

• Broadly, some subset of inputs may interact, and some will be independent.

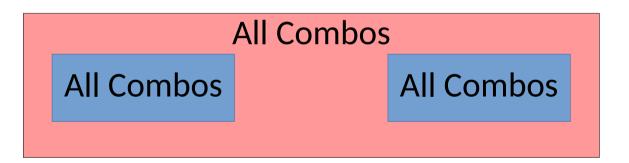
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- Careful combinations of different approaches can yield more meaningful tests.



• And we have already seen another strategy for reducing test suites...

### **Remember the Constraints**

- Constraints, and [error]s can reduce the # of tests further
  - No need to test invalid constraints
  - No need to test more than one [error]