

CMPT 473  
Software Quality Assurance

# Input Space Partitioning

Nick Sumner - Fall 2014  
With material from Patrick Lam, Jeff Offutt

# Recall

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- Testing involves running software and comparing observed behavior against expected behavior
  - Select an input, look at the output

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  - Select an input, look at the output
- Problem: The *input domain* is infinite or pragmatically infinite.

```
for test in allPossibleInputs:  
    run_program(test)
```



# Recall

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- Testing involves running software and comparing observed behavior against expected behavior
  - Select an input, look at the output
- Problem: The *input domain* is infinite or pragmatically infinite.
- Testing is about selecting a finite subset of inputs that can help measure quality

# Input Space Partitioning



Take the direct approach:  
Focus on the input!

# Input Space Partitioning

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  - Divide (*partition*) the set of possible inputs into equivalence classes

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e.g. `abs(x)`

Input Domain: `..., -3, -2, -1, 0, 1, 2, 3, ...`

How many tests if done exhaustively?



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Input Domain:  $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

Partitions:  $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

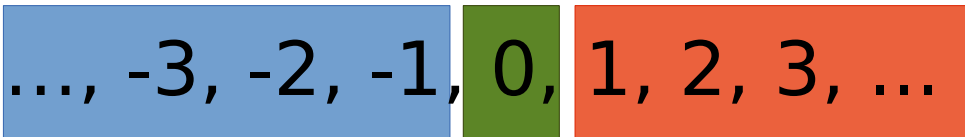
What might reasonable partitions be?

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Partitions:  $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

How many tests for the partitions?

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Input Domain:  $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

Partitions:  $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

Impressive! How do we do it?

# Input Space Partitioning

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1) Identify the component

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- Whole program
- Module
- Class
- Function

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## 1) Identify the component

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## 2) Identify the inputs

What might the inputs be?

# Input Space Partitioning

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## 1) Identify the component

- Whole program
- Module
- Class
- Function

## 2) Identify the inputs

- Function/method parameters
- File contents
- Global variables
- Object state
- User provided inputs



# Input Space Partitioning

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3) Develop an *Input Domain Model*

# Input Space Partitioning

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What does that even mean?

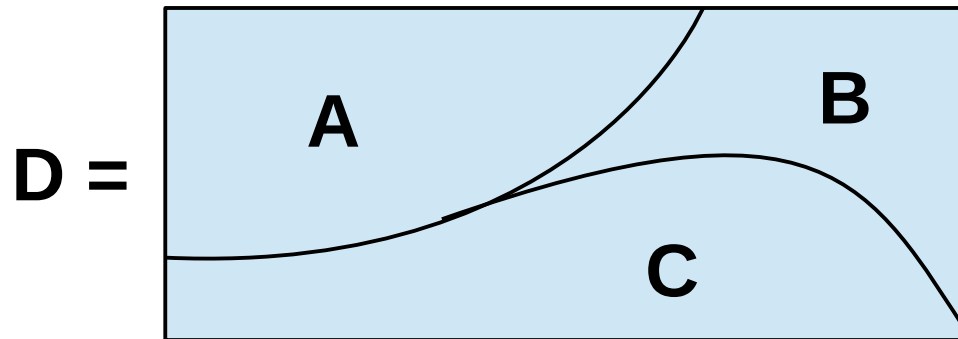
# Input Space Partitioning

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- 3) Develop an *Input Domain Model*
- A way of *describing* the possible inputs
  - Partitioned by characteristics

# Partitioned Input Domain

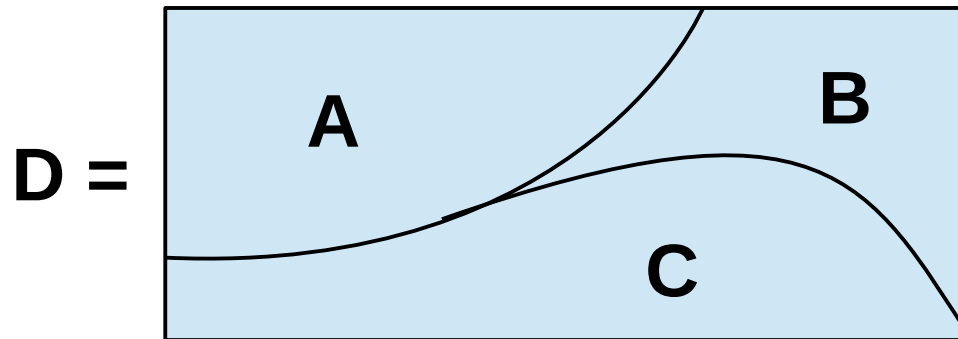
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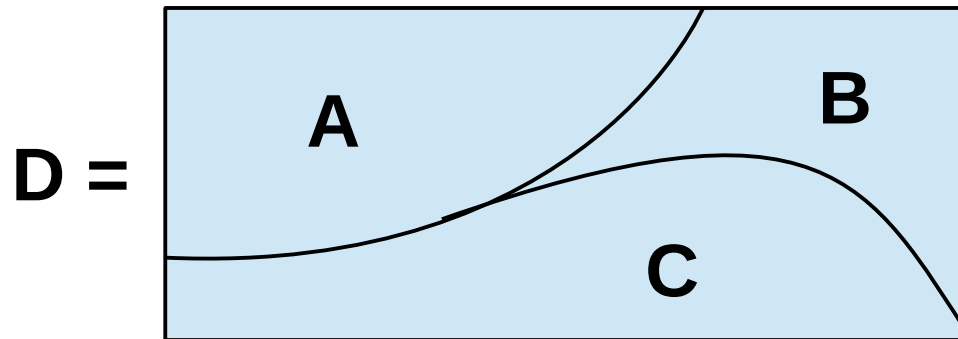
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What are **characteristics**?



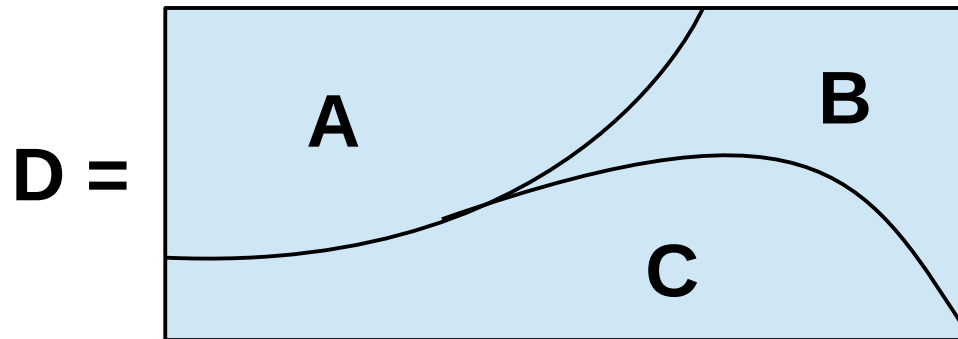
# Partitioned Input Domain

- **Partition** the domain  $D$  on characteristics
- Must satisfy 2 criteria:
  - Disjoint:  $A \cap B \cap C = \emptyset$
  - Cover:  $A \cup B \cup C = D$



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What do these criteria intuitively provide?

# Using Partitions

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- Select one input from each block
- Each input in a block is assumed equally useful



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How many tests might this imply?  
Might there be more? Fewer?

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We're hiding some details in this last step.  
It's not quite right yet.

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- Select one input from each block
- Each input in a block is assumed equally useful
- How?
  - Identify ***characteristics*** of the possible inputs  
(from requirements, types, etc.)
  - Partition into ***blocks*** based on each characteristic
  - Create tests by ***selecting values*** for each block
- Characteristics:
  - List s is sorted ascending
  - X is null
  - String length
  - ...

# Partitioning is Subtle

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- Suppose we have:

```
classifyParallelogram(p1)
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Characteristic: “The subtype of parallelogram”

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Partitioning a triangle classifying program
- It is easy to create overlapping partitions.
  - Care and design required to avoid it.

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- It is easy to create overlapping partitions.
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Why do disjoint partitions matter?

# Process (Reiterated)

---

3 step process (for now):

- 1) Find the component / function to test  
methods, classes, programs, functions

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- Must identify ***everything***  
locals, globals, files, databases, schedules, servers, ...

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3) Model the input domain

- Identify characteristics
- Partition the input domain
- Select values for each region

# Process (Reiterated)

3 step process (for now):

1) Find the component / function to test  
methods, classes, programs, functions

2) Find all test parameters

• Must identify *everything*

Domain knowledge, tactics, and creativity apply here.

3) Model the input domain

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# Approaches to Input Modeling

We still haven't talked about ***how*** to model input!

# Approaches to Input Modeling

2 Main approaches:

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1) **Interface based**

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- Derived from expected input/output by spec.

# Approaches to Input Modeling

2 Main approaches:

## 1) Interface based

- Guided directly by identified parameters & domains
- Simple
- Automatable

## 2) Functionality/Requirements based

- Derived from expected input/output by spec.
- Requires more design & more thought
- May be better (smaller, goal oriented, ...)

# Interface Based Modeling

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- Consider parameters individually
  - Examine their types/domains
  - Ignore relationships & dependences



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How does this apply to our  
triangle classifier?

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- Identify characteristics corresponding to behaviors/functionality in the requirements
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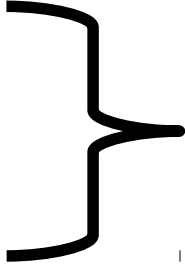
How might this apply to our triangle classifier?

# Finding Typical Characteristics

What might typical characteristics be?

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What might typical characteristics be?

- Preconditions
  - Postconditions
  - Relationships to special values
  - Relationships between variables
- 
- Invariants



# Finding Typical Values

---

How might you select values for a block?

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- Expected values (e.g. exemplified from spec)
- Invalid, valid, & special values
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Thought experiment:  
What do boundary values as a  
selection approach indicate?

# An Interface Based Example

- Consider our triangle classifier
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Characteristic	b1	b2	b3
Side 1 <?> 0	Side 1 > 0	Side 1 = 0	Side 1 < 0
Side 2 <?> 0	Side 2 > 0	Side 2 = 0	Side 2 < 0
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How many tests does this create?

What **will** this test well?  
What **won't** this test well?

# Refining the Example

- We can subdivide partitions to cover more behavior

Characteristic	b1	b2	b3	b4
Value of side 1	Side 1 > 1	Side 1 = 1	Side 1 = 0	Side 1 < 0
Value of side 2	Side 2 > 1	Side 2 = 1	Side 2 = 0	Side 2 < 0
Value of side 3	Side 3 > 1	Side 3 = 1	Side 3 = 0	Side 3 < 0

$\{\text{Side } n > 0\} \rightarrow \{\text{Side } n = 1\}, \{\text{Side } n > 1\}$



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How many tests now?

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How many tests now?

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What does it test well? Not well?

# A Functionality Based Example

- Consider our triangle classifier again
  - What might our characteristics & partitions be?

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# A Functionality Based Example

- Consider our triangle classifier again
  - What might our characteristics & partitions be?
  - Are there alternatives?
  - Why might you use them?

# A Classic Example

- Start with a component / specification:

<b>Command</b>	FIND
<b>Syntax</b>	FIND <pattern> <file>
<b>Function</b>	<p>The FIND command is used to locate one or more instances of a given pattern in a text file. All lines in the file that contain the pattern are written to standard output. A line containing the pattern is written only once, regardless of the number of times the pattern occurs on it.</p> <p>The pattern is any sequence of characters whose length does not exceed the maximum length of a line in the file. To include a blank in the pattern, the entire pattern must be enclosed in quotes (""). To include a quotation mark in the pattern, two quotes (""") must be used.</p>

# A Classic Example

---

- Step 1: Analyze the specification
  - What is the component?
  - What are the parameters?
  - What are the characteristics?



# A Classic Example

- Step 1: Analyze the specification

- What are the Parameters:
  - Pattern
  - Input file (& its contents!)
- What are the characteristics?

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- What Parameters:
  - Pattern
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- What are the characteristics?

Characteristics:

Pattern

Input file

Pattern Size

Quoting

Embedded Quotes

File Name

Environment / System Characteristics:

# of pattern occurrences in file

# of occurrences on a particular line:

# A Classic Example

---

- Step 2: Partition the Input Space
  - Guided by intelligence and intuition
  - *Combine* interface and functionality based approaches as necessary

# A Classic Example

- Step 2: Partition the Input Space
  - Guided by intelligence and intuition
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Parameters:

Pattern Size:

Empty

Single character

Many characters

Longer than any line in the file

Quoting:

...

# A Classic Example

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- Familiar Idea:
  - Select one region per characteristic at a time
  - Combine into test *frames* (test case plans)
  - e.g. ...

# A Classic Example

- Familiar Idea:
  - Select one block per characteristic at a time
  - Combine into test *frames* (test case plans)
  - e.g.

Pattern size : empty

Quoting : pattern is quoted

Embedded blanks : several embedded blanks

Embedded quotes : no embedded quotes

File name : good file name

Number of occurrences of pattern in file : none

Pattern occurrences on target line : one

# A Classic Example

- Familiar Idea:
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# A Classic Example

- Step 3: Identify **constraints** among the characteristics & blocks

Pattern Size:

Empty	[Property Empty]
Single character	[Property NonEmpty]
Many characters	[Property NonEmpty]
Longer than any line in the file	[Property NonEmpty]

# A Classic Example

- Step 3: Identify **constraints** among the categories

## Pattern Size:

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Pattern is quoted	[Property Quoted]
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Pattern is improperly quoted	[If NonEmpty]

What should this do to the number of tests?  
To the quality of tests?

# A Classic Example

---

- Step 4
  - Create tests by selecting values that satisfy the selected blocks for each frame
  - Eliminate tests that cover redundant scenarios

# A Classic Example

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  - Create tests by selecting values that satisfy the selected blocks for each frame
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Why might scenarios be redundant?

# A Classic Example

- Step 5:
  - Take your generated test cases and automate them

# Your Assignment

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- Posted tonight/tomorrow morning.
- You will be applying the C-P method to a file parsing function of an open source project.