Fall 2015 Page 1 CMPT 419/726: Machine Learning Instructor: Greg Mori

Quiz 1 October 26, 2015

Time: 50 minutes; Total Marks: 38

One double-sided 8.5" x 11" cheat sheet allowed

This test contains 4 questions and 6 pages

NAME:

STUDENT NUMBER:

Question	Marks	Time budget
1	/16	15 min
2	/6	10 min
3	/10	10 min
4	/6	10 min

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- 1. (16 marks) True or False questions. No explanation required.
 - (a) True or False. Test error always decreases when more training data are used.
 - (b) True or False. When modeling coin tossing, the maximum a posteriori estimate for μ is the same as the maximum likelihood estimate if a "flat" prior is used:

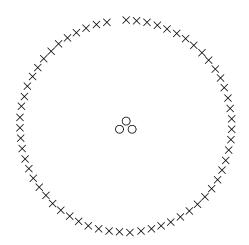
$$p(\mu) = \begin{cases} 1 & 0 \le \mu \le 1 \\ 0 & o.w. \end{cases}$$

(c) True or False. $p(x) \le 1$ for a Gaussian kernel density estimate:

$$p(\boldsymbol{x}) = \frac{1}{N} \sum_{n=1}^{N} \frac{1}{(2\pi h^2)^{1/2}} \exp\left\{-\frac{||\boldsymbol{x} - \boldsymbol{x}_n||^2}{2h^2}\right\}$$

- (d) True or False. Given any fixed test set for regression, there always exists a set of polynomials that gives zero error on this test set.
- (e) True or False. When training logistic regression with gradient descent, each iteration of gradient descent will cause the error (negative log likelihood) to decrease.
- (f) True or False. Kernelized perceptron can produce non-linear decision boundaries in the original input space.
- (g) True or False. If $k_1(x, z)$ is a valid kernel, then $k_2(x, z) = k_1(x, z) + 1$ is always valid too.
- (h) True or False. Removing a training data point which is a support vector will cause the SVM decision boundary to move.

2. (6 marks) Consider using a **K nearest neighbour** classification model with the training set shown below. Suppose we use leave-one-out cross-validation (LOO-CV) to determine the value of the parameter K from $\{1,3,5,7,\ldots\}$. Explain what the result of this procedure would be.

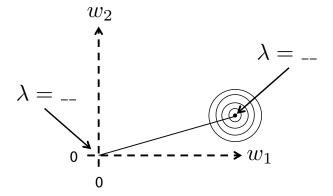


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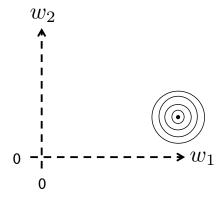
3. (10 marks) Recall regularized regression:

$$\tilde{E}(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^{N} \{y(x_n, \mathbf{w}) - t_n\}^2 + \frac{\lambda}{2} ||\mathbf{w}||^2$$

• (3 marks) The picture below shows the minimum of squared error and isocurves of equal squared error. Label the ends of the solid line segment according to the values of λ that will achieve these values for parameters w.



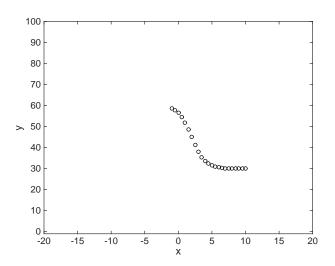
• (3 marks) Draw a similar picture for L_1 regularization (lasso). Draw the equivalent to the solid line and label its ends.



• (4 marks) Consider Gaussian versus sigmoid basis functions for un-regularized regression on the 1-d dataset below. Draw 2 curves: from using (a) $\phi_g(x)$ and a bias term; or (b) $\phi_s(x)$ and a bias term.

$$\phi_g(x) = \exp\left\{-\frac{(x-1)^2}{4}\right\}$$

$$\phi_s(x) = \frac{1}{1 + \exp(2-x)}$$



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4. (6 marks) Consider training a support vector machine with a linear kernel on a **linearly** separable dataset. Is there any difference in the hyperplane (\boldsymbol{w}, b) found using the exact (hard margin) classification constraints:

$$\arg\min_{\boldsymbol{w},b} \frac{1}{2} ||\boldsymbol{w}||^2$$
s.t. $\forall n, t_n(\boldsymbol{w}^T \boldsymbol{x}_n + b) \ge 1$

and using those with slack variables (soft margin):

$$\arg\min_{\boldsymbol{w},b,\xi_n} C \sum_{n=1}^N \xi_n + \frac{1}{2} ||\boldsymbol{w}||^2$$
s.t.
$$\forall n, t_n(\boldsymbol{w}^T \boldsymbol{x}_n + b) \ge 1 - \xi_n$$

$$\forall n, \xi_n \ge 0$$

State whether there is a difference for a **linearly separable dataset**. If so, explain and show an example of the different behaviour. If not, give a brief argument why not.