◆□▶ ◆□▶ ▲□▶ ▲□▶ □ のQ@

# Recurrent Neural Networks Greg Mori - CMPT 419/726

#### Goodfellow, Bengio, and Courville: Deep Learning textbook Ch. 10

◆□▶ ◆□▶ ▲□▶ ▲□▶ ■ ののの

# Sequential Data with Neural Networks

- Sequential input / output
  - Many inputs, many outputs x<sub>1:T</sub> → y<sub>1:S</sub>
    - c.f. object tracking, speech recognition with HMMs; on-line/batch processing
  - One input, many outputs *x* → *y*<sub>1:S</sub>
    - e.g. image captioning
  - Many inputs, one output  $x_{1:T} \rightarrow y$ 
    - e.g. video classification



**Recurrent Neural Networks** 

Long Short-Term Memory

**Temporal Convolutional Networks** 

Examples

◆□▶ ◆□▶ ◆□▶ ◆□▶ ●□ ● ● ●



#### **Recurrent Neural Networks**

Long Short-Term Memory

**Temporal Convolutional Networks** 

Examples



◆□▶ ◆□▶ ▲□▶ ▲□▶ ■ ののの

## Hidden State

- Basic idea: maintain a state h<sub>t</sub>
- State at time *t* depends on input *x*<sub>t</sub> and previous state *h*<sub>t-1</sub>
- It's a neural network, so relation is non-linear function of these inputs and some parameters *W*:

$$\boldsymbol{h}_t = f(\boldsymbol{h}_{t-1}, \boldsymbol{x}_t; \boldsymbol{W})$$

• Parameters W and function  $f(\cdot)$  reused at all time steps

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □



• Output *y<sub>t</sub>* also depends on the hidden state:

$$y_t = f(\boldsymbol{h}_t; \boldsymbol{W}_y)$$

· Again, parameters/function reused across time



**Recurrent Neural Networks** 

Long Short-Term Memory

Temporal Convolutional Networks

Examples



◆□▶ ◆□▶ ◆□▶ ◆□▶ ● ● ● ●

# Gradients

- Basic RNN not very effective
- Need many time steps / complex model for challenging tasks
- Gradients in learning are a problem
  - Too large: can be handled with gradient clipping (truncate gradient magnitude)
  - Too small: can be handled with network structures / gating functions (LSTM, GRU)

### Long Short-Term Memory



- Hochreiter and Schmidhuber, Neural Computation 1997
  - (Figure from Donohue et al. CVPR 2015)
- Gating functions  $g(\cdot), f(\cdot), o(\cdot)$ , reduce vanishing gradients

#### Long Short-Term Memory



$$i_t = \sigma(W_{xi}x_t + W_{hi}h_{t-1} + b_i) \tag{1}$$

$$f_t = \sigma(W_{xf}x_t + W_{hf}h_{t-1} + b_f)$$
(2)

$$o_t = \sigma(W_{xo}x_t + W_{ho}h_{t-1} + b_o) \tag{3}$$

$$g_t = tanh(W_{xc}x_t + W_{hc}h_{t-1} + b_c)$$
(4)

$$c_t = f_t \odot c_{t-1} + i_t \odot g_t \tag{5}$$

$$h_t = o_t \odot tanh(c_t) \tag{6}$$

see Graves, Liwicki, Fernandez, Bertolami, Bunke, and Schmidhuber, TPAMI 2009 🖌 🚓 👘 🖌 👍 🖕 🚖 🖉



**Recurrent Neural Networks** 

Long Short-Term Memory

**Temporal Convolutional Networks** 

Examples

▲□▶▲圖▶▲≣▶▲≣▶ ≣ のQ@

## Convolutions to Aggregate over Time



- Control history by *d* (dilation, holes in the filter) and *k* (width of the filter)
- Causal convolution, only use elements from the past
- Bai, Kolter, Koltun arXiv 2018

## **Residual (skip) Connections**



 Include residual connections to allow long-range modeling and gradient flow



**Recurrent Neural Networks** 

Long Short-Term Memory

Temporal Convolutional Networks

Examples

◆□ > ◆□ > ◆三 > ◆三 > ・三 ・ のへぐ

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □

#### Example: Image Captioning



Karpathy and Fei-Fei, CVPR 2015

・ロット (雪) ・ (日) ・ (日)

-

Examples

#### **Example: Video Description**



 S. Venugopalan, M. Rohrbach, J. Donahue, R. Mooney, T. Darrell, K. Saenko, ICCV 2015

#### **Example: Machine Translation**



• Wu et al., Google's Neural Machine Translation System: Bridging the Gap between Human and Machine Translation, arXiv 2016

◆□▶ ◆□▶ ▲□▶ ▲□▶ □ のQ@

## Conclusion

- Readings: http://www.deeplearningbook.org/ contents/rnn.html
- Recurrent neural networks, can model sequential inputs/outputs
  - Input includes state (output) from previous time
  - Different structures:
    - RNN with multiple inputs/outputs
    - Gated recurrent unit (GRU)
    - Long short-term memory (LSTM)
  - Error gradients back-propagated across entire sequence