



Voxels, Point Clouds, and Registration

Richard (Hao) Zhang

CMPT 464/764: Geometric Modeling in Computer Graphics

Lecture 3

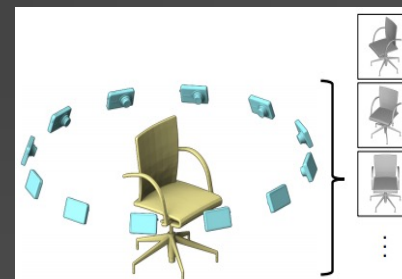
Outline

- Implicit representations
- Parametric representations
- Meshes (subdivision)
- Point clouds
- Voxels
- Multi-view representations

Smooth curves and surfaces

Discrete representations

2D → 3D



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Smooth curves and surfaces

Discrete representations

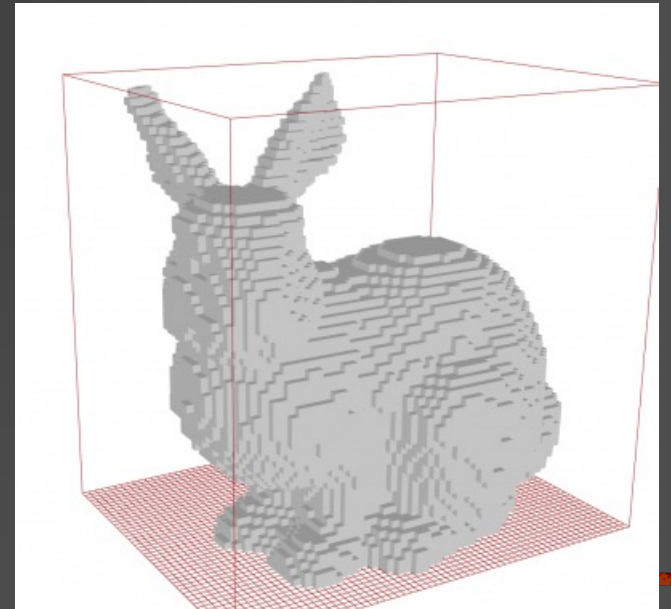
- Multi-view representations

2D $\rightarrow$ 3D



Volumetric or voxel representations

- Embed 3D shape in a regular volumetric grid: 3D shape = set of all voxels that lie **on or inside** the shape
- Closely related to image and pixel representations: it is a **3D image**
- Closely tied to **implicit representations** and support similar operations
- Natural **“first choice” for neuralization** due to similarity to images (more next week)

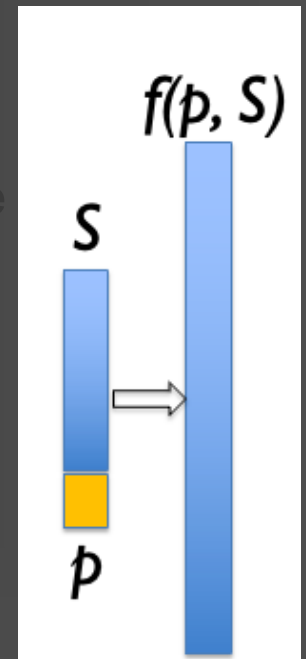


Voxels vs. implicit functions

- Voxels: intrinsically **discrete** representation, limited by resolutions
- Implicit functions: intrinsically **continuous** representation
 - There is an implicit field value for any (x, y, z)
 - When processing an implicit function (e.g., for rendering), one often need to discretize the function

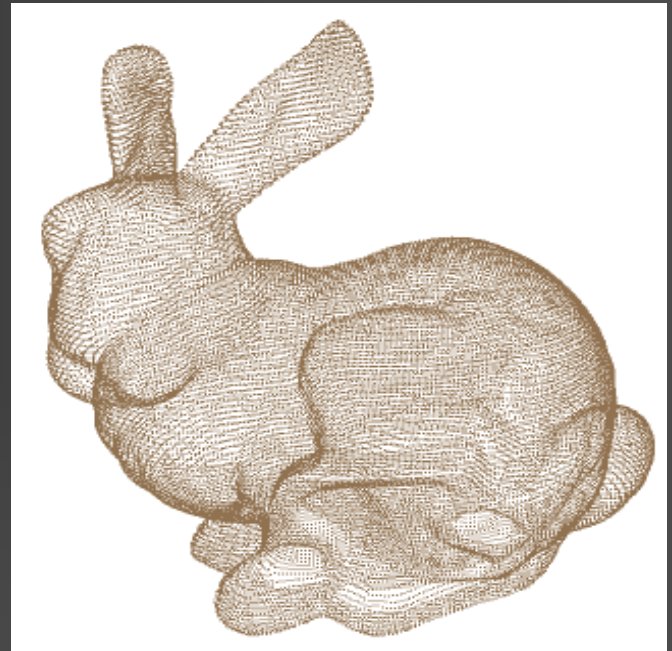
Voxels vs. implicit functions

- Voxels: intrinsically **discrete** representation, limited by resolutions
- Implicit functions: intrinsically **continuous** representation
 - There is a field value for any point
 - When processing an implicit function (e.g., for rendering), one need to discretize the function
- IM-Net (next week): trained on voxel inputs, e.g., on 64^3 voxels, but can learn **continuous** outputs, $\forall p \in \mathbb{R}^3$



Point-based representation (PBR)

- A 3D surface model is represented using a set of **points near the surface**
- There is no (explicit) connectivity information between the points
- Typically need k NN – **k nearest neighbors** – during processing
- Point normals can also be specified or estimated for rendering



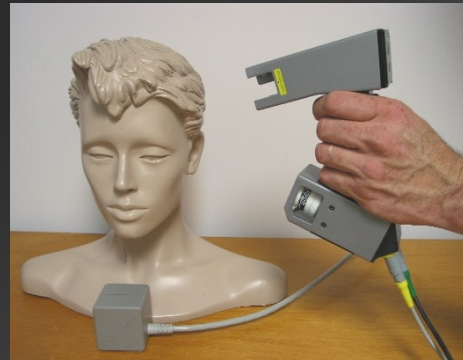
Point cloud acquisition



Cyberware



NextEngine (< \$3K)



FastScan (\$23K)



Roland DGA LPX-250 (\$10K)

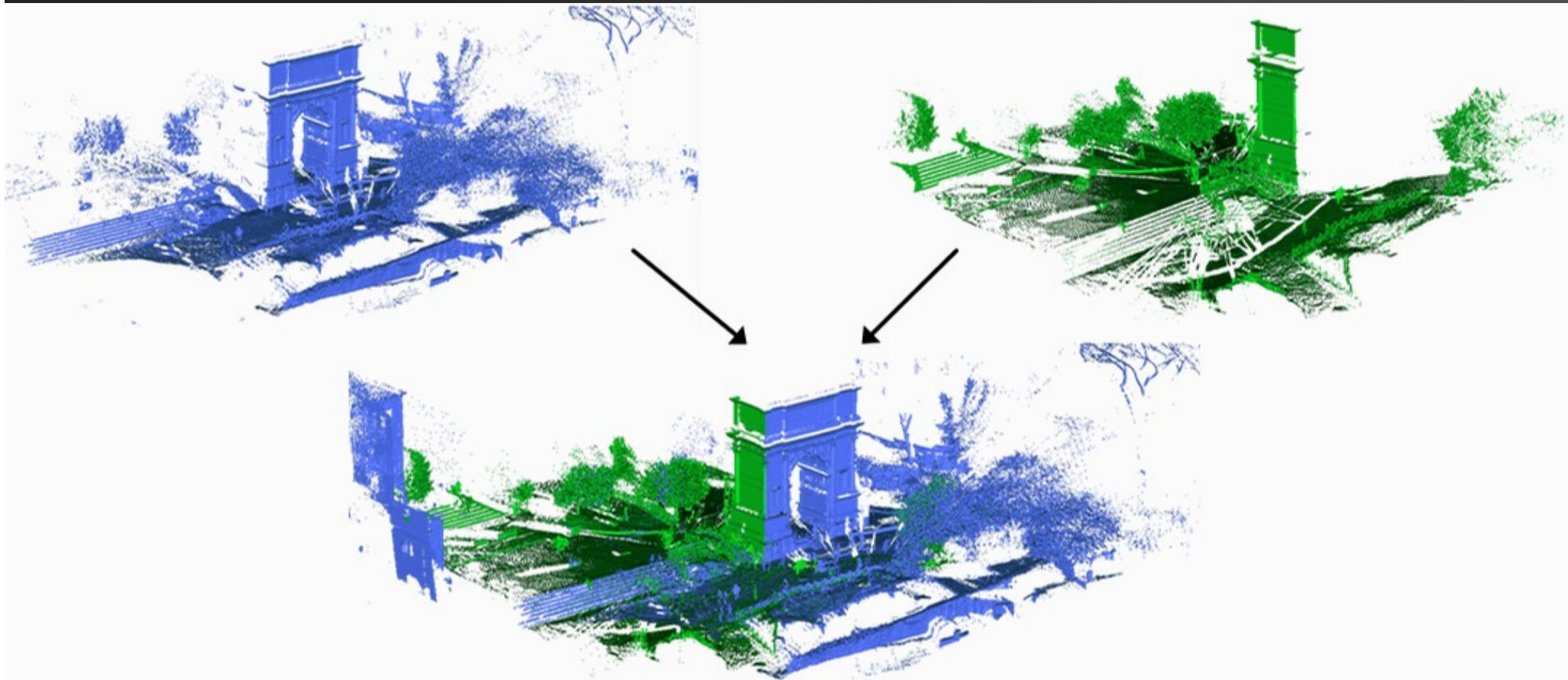
InSpeck

Point cloud acquisition



NextEngine (< \$3K)

Point cloud registration

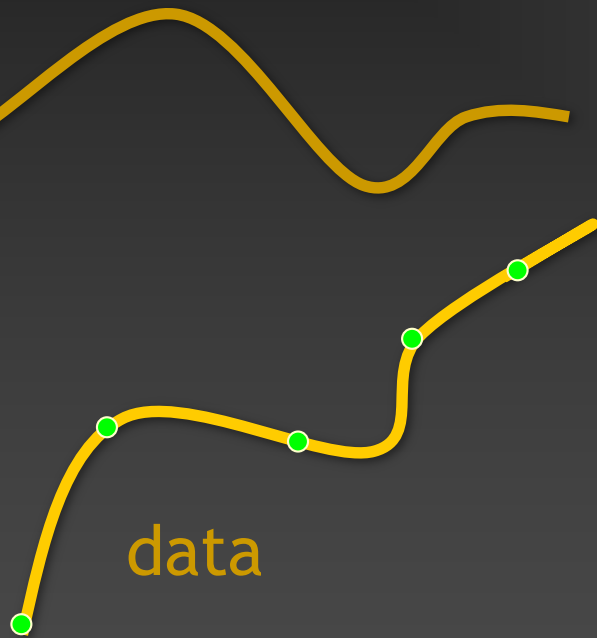


Iterative closest point (ICP) algorithm

- A classic registration/correspondence schemes
 - Input: **data** and **model shapes**
 - Objective:
 - Rigid transform = rotation + translation
 - **Minimize mean squared error** from data points to closest points in model [Besl and McKay 92]
 - Correspondence obtained by Euclidean proximity
-

ICP algorithm

model

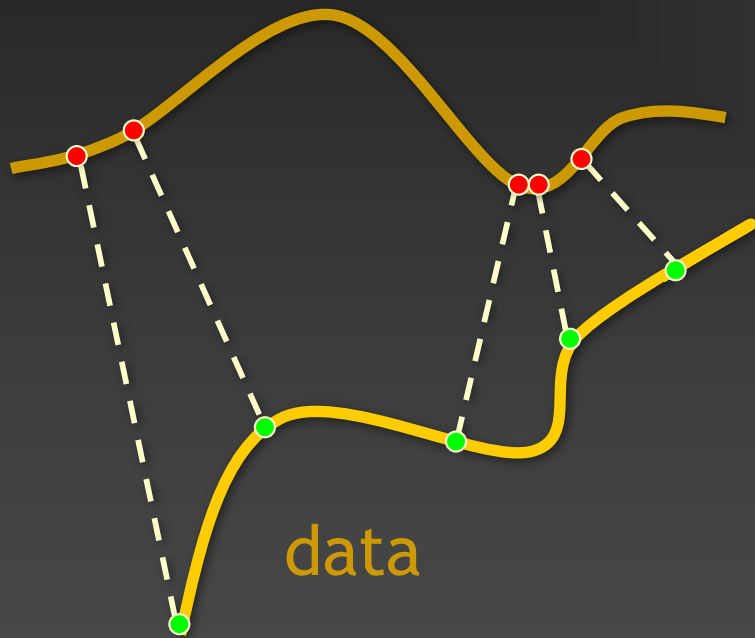


data

Model and data shapes (point samples)

ICP algorithm

model

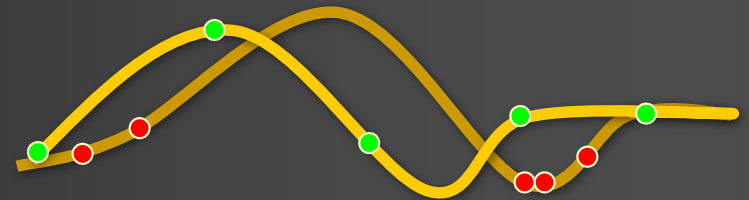
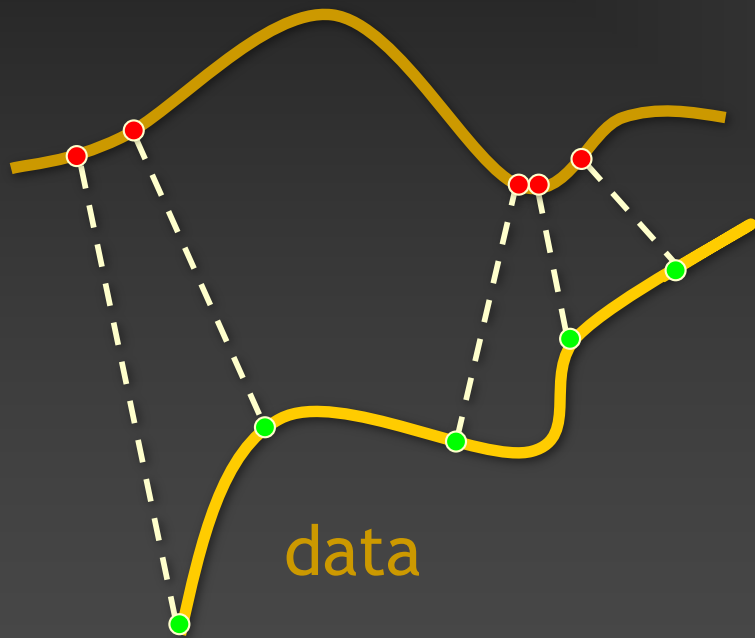


data

Find closest points from data to model

ICP algorithm

model



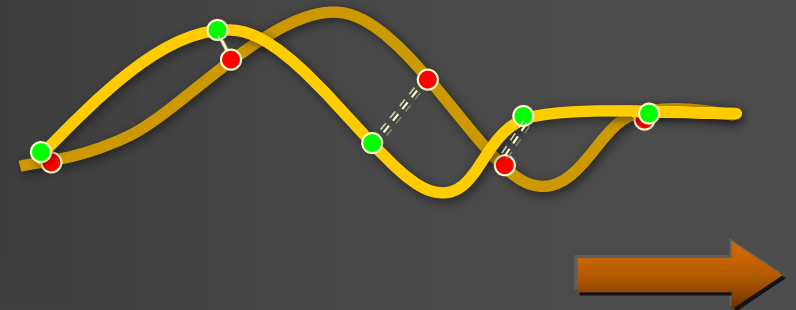
Find best rigid transform to align the corresponding points

ICP algorithm

model

data

Iterate ...



A historical note on PBRs

- “As the visual complexity of computer-generated scenes continue to increase, the use of classical modeling primitives (polygons) as display primitives becomes less appealing.”

Levoy and Whitted,
“The Use of Points as a Display Primitive”, 1985

- Use of points traces back to modeling of smoke, fire, and cloud around the late 70's [Csuri et al. 79, Blinn 82]

First renewed interest

- PBR was witnessing a revival around 2002 - 2006
- Points are directly available via **laser scanning**
 - Substantial advances in 3D digitizing and laser scanning and acquisition technology
 - High quality points (color and texture) easily obtained
 - Relatively inexpensive laser scanners available

Point-based Graphics Resource

Symposium on Point-Based Graphics

[Symposium on Point-Based Graphics 2006 \(On-line Papers\)](#) ***
[Symposium on Point-Based Graphics 2006 \(On-line Papers\)](#)
[Symposium on Point-Based Graphics 2005 \(On-line Papers\)](#)
[Symposium on Point-Based Graphics 2004 \(On-line Papers\)](#)

Books

Point-Based Graphics

Edited By [Markus Gross](#), Swiss Federal Institute of Technology (ETH), Zurich, Switzerland [Hanspeter Pfister](#), MERL (Mitsubishi Electric Research Laboratories), Cambridge, Massachusetts, U.S.A.

Tutorials/Course Notes/Survey

Point-Based Computer Graphics



[Marc Alexa](#), [Markus Gross](#), [Mark Pauly](#), [Hanspeter Pfister](#), [Marc Stamminger](#), [Matthias Zwicker](#)
SIGGRAPH 2004 Course Notes

Point-Based Computer Graphics



[Marc Alexa](#), [Carsten Dachsbacher](#), [Markus Gross](#), [Mark Pauly](#), [Jeroen van Baar](#), [Matthias Zwicker](#)
Eurographics 2003 Tutorial Notes

Point-Based Computer Graphics



[Marc Alexa](#), [Markus Gross](#), [Mark Pauly](#), [Hanspeter Pfister](#), [Marc Stamminger](#), [Matthias Zwicker](#)
Eurographics 2002 Tutorial Notes

A Survey of Point-Based Techniques in Computer Graphics



[Leif Kobbelt](#), [Mario Botsch](#)
to appear in Computers & Graphics

Dissertation/Thesis

Point-Based Modeling, Animation and Rendering of Dynamic Objects



[Bart Adams](#)
PhD Thesis, Katholieke Universiteit Leuven, May 2006

Point-Based Multi-Resolution Rendering



[Michael Wand](#)
PhD Thesis, University of Tübingen, Department of Computer Science and Cognitive Science, 2004

Dynamic Point Samples as Primitives for Free-Viewpoint Video



[Stephan Wurmlin](#)
PhD Thesis, ETH Zurich, 2004

Reconstruction and Rendering of Implicit Surfaces from Large Unorganized Point Sets



[Patrick Reuter](#)
PhD Thesis, LaBRI - Université Bordeaux-1, 2003

Point Primitives for Interactive Modeling and Processing of 3D Geometry



[Mark Pauly](#)
PhD Thesis, ETH Zurich, 2003

Continuous Reconstruction, Rendering, and Editing of Point-Sampled Surfaces



[Matthias Zwicker](#)
PhD Thesis, ETH Zurich, 2003

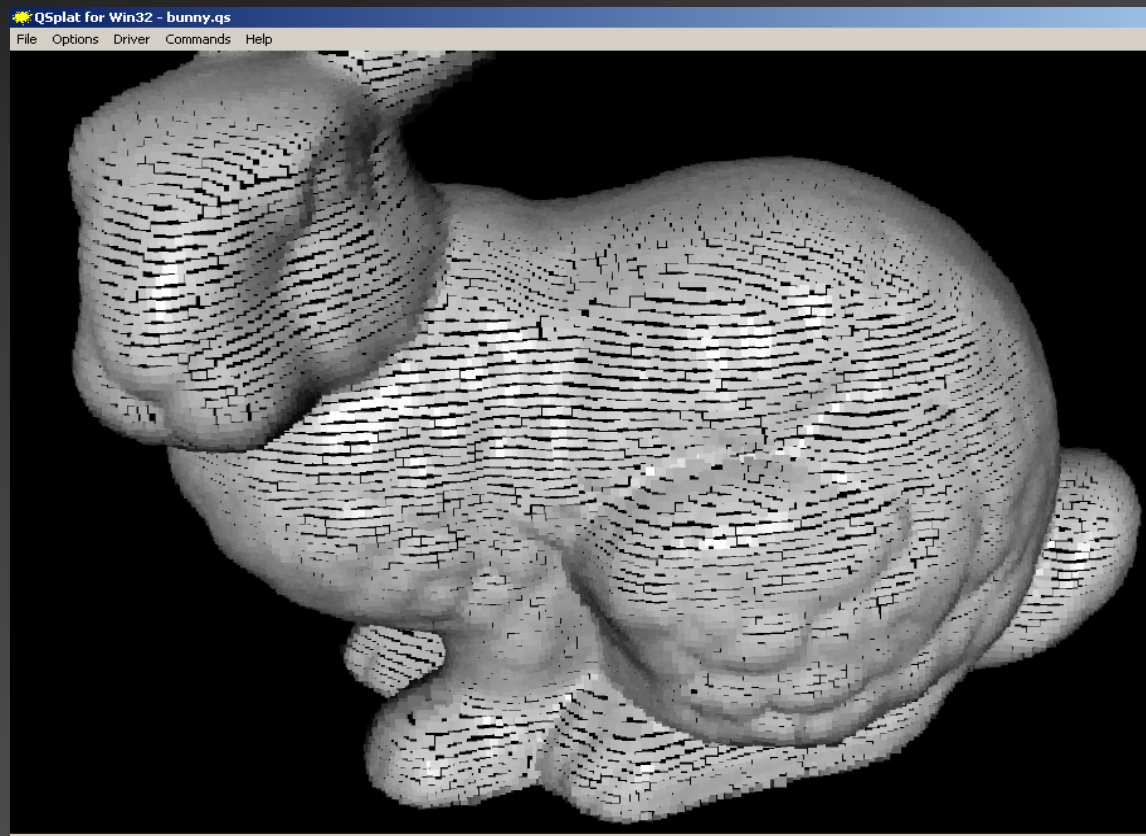
Point Set Surfaces



[Shachar Fleishman](#)
PhD Thesis, 2003

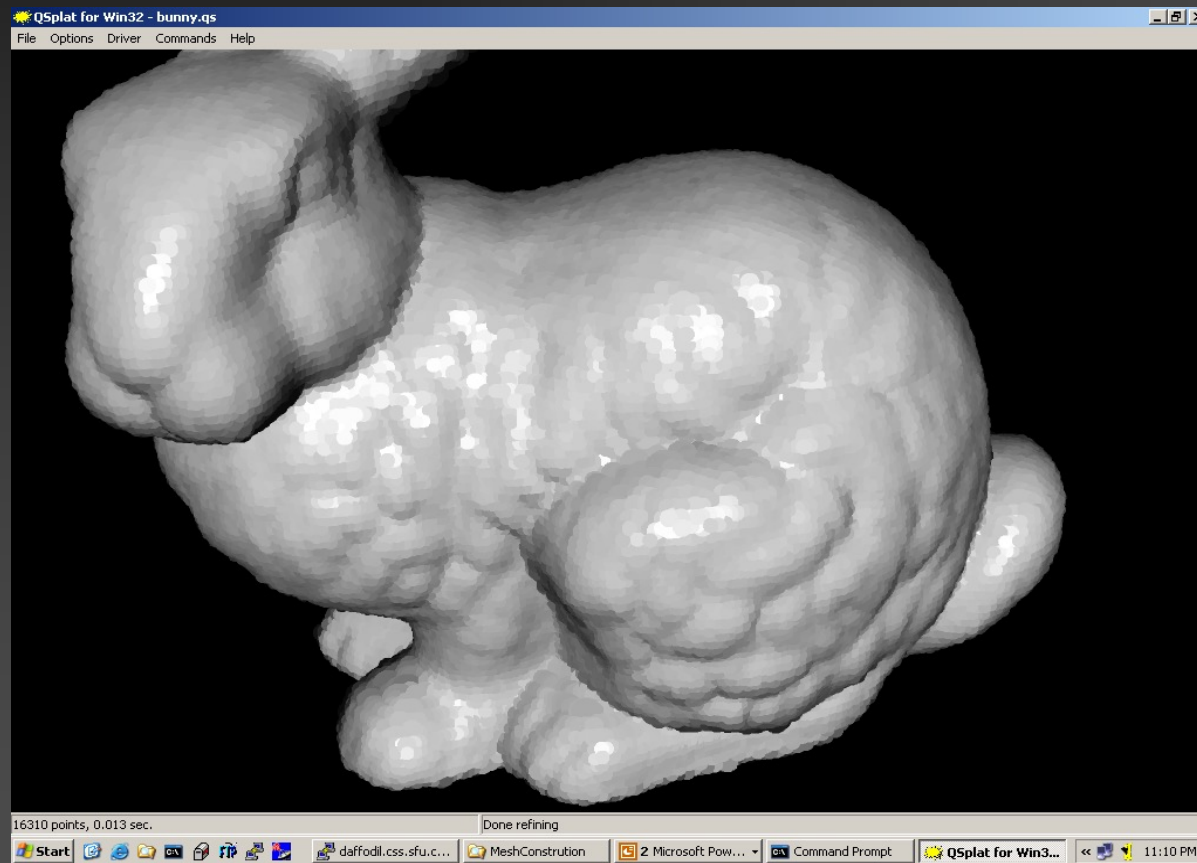
<https://www.realtimerendering.com/kesen/PointBasedPaper.html>

PBR rendering via splatting: QSplat



Splat = OpenGL
points

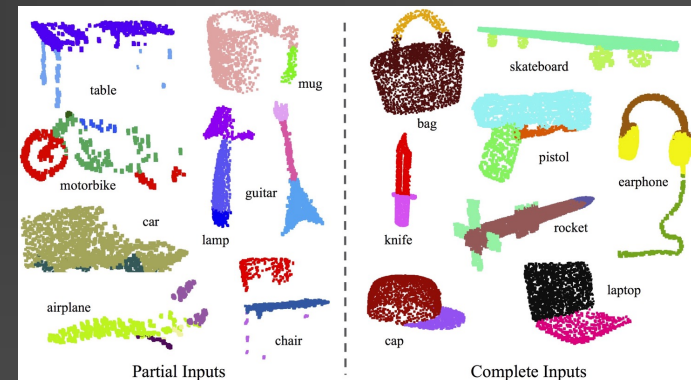
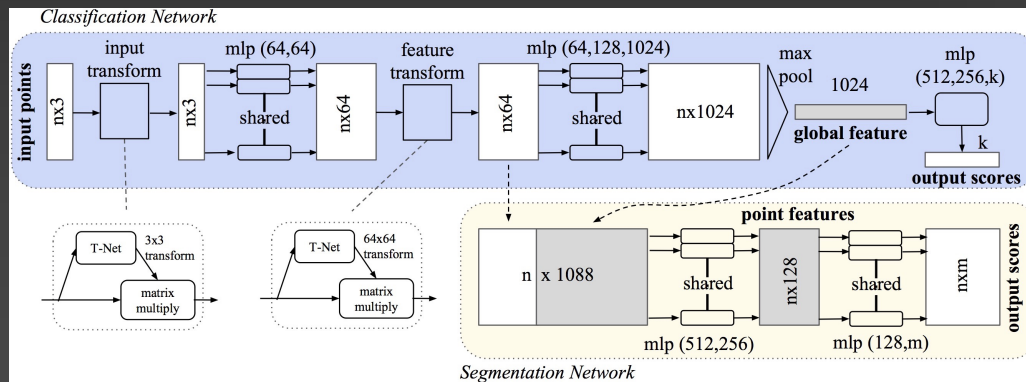
PBR rendering via splatting: QSplat



Splat = circles

Second revival: deep learning

- PointNet and PointNET++, since 2016/17
- Deep neural network to **encode and aggregate point features** for shape recognition, segmentation, etc. (more next week)





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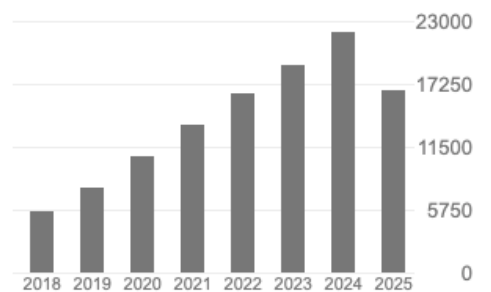
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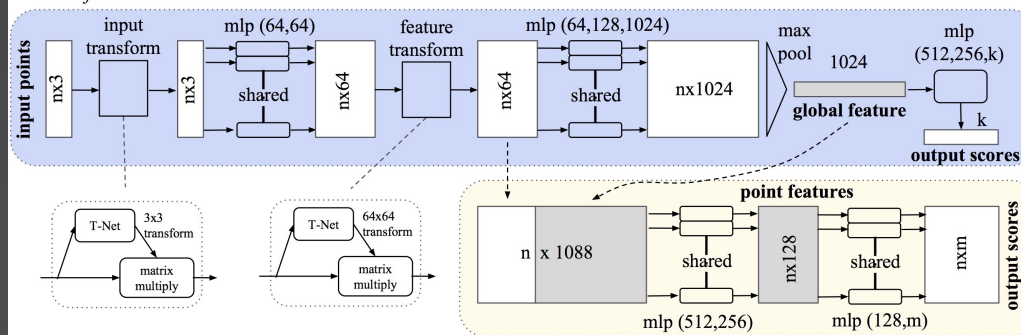


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UCSD CSE

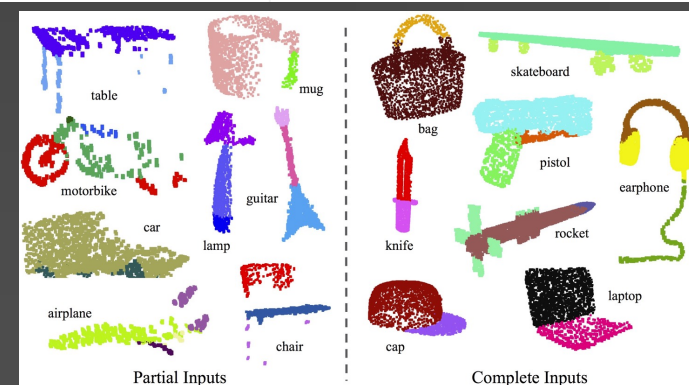


TITLE	CITED BY	YEAR
Pointnet: Deep learning on point sets for 3d classification and segmentation CR Qi, H Su, K Mo, LJ Guibas Proceedings of the IEEE conference on computer vision and pattern ...	21564	2017
Pointnet++: Deep hierarchical feature learning on point sets in a metric space CR Qi, L Yi, H Su, LJ Guibas Advances in neural information processing systems 30	16028	2017
Shapenet: An information-rich 3d model repository AX Chang, T Funkhouser, L Guibas, P Hanrahan, Q Huang, Z Li, ... arXiv preprint arXiv:1512.03012	7141	2015
The earth mover's distance as a metric for image retrieval Y Rubner, C Tomasi, LJ Guibas International journal of computer vision 40 (2), 99-121	7138	2000
Kpconv: Flexible and deformable convolution for point clouds H Thomas, CR Qi, JE Deschaud, B Marcotegui, F Goulette, LJ Guibas Proceedings of the IEEE/CVF international conference on computer vision ...	3725	2019
Frustum pointnets for 3d object detection from rgb-d data CR Qi, W Liu, C Wu, H Su, LJ Guibas Proceedings of the IEEE conference on computer vision and pattern ...	3184	2018
A point set generation network for 3d object reconstruction from a single image H Fan, H Su, LJ Guibas Proceedings of the IEEE conference on computer vision and pattern ...	3014	2017

Classification Network



Segmentation Network



Third revival: 3D Gaussian splatting (3DGS)

- 3DGS [Kerbl et al. SIG 2023] superseding NeRF (2000) – more later

