



# Voxels, Point Clouds, and Registration

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CMPT 464/764: Geometric Modeling in Computer Graphics

Lecture 3

# Outline on 3D representations

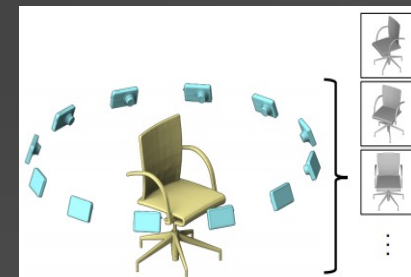
- Implicit reps
- Parametric reps
- Meshes (subdivision)
- Point clouds
- Volumes
- Projective reps
- Structured reps

Smooth curves and surfaces

Discrete representations

3D → 2D

**Parts + relations = structures**  
Encompasses all low-level reps



# Today

- Implicit reps

- Parametric reps

- Meshes (subdivision)

- Point clouds

- Volumes

- Projective reps

- Structured reps

Smooth curves and surfaces

Discrete representations

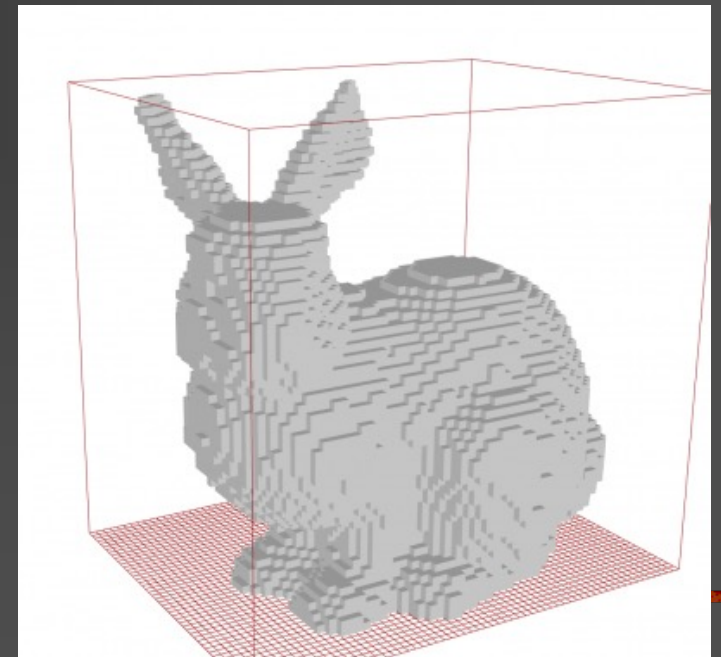
3D → 2D

**Parts + relations = structures**  
Encompasses all low-level reps



# Volumetric or voxel representations

- Embed 3D shape in regular volumetric grid: 3D shape = set of all voxels that lie **on or inside** shape
- Closely related to image and pixel representations: it is a **3D image**
- Closely tied to **implicit representations** and support similar operations
- Natural **“first choice” for neuralization** due to similarity to image/pixels



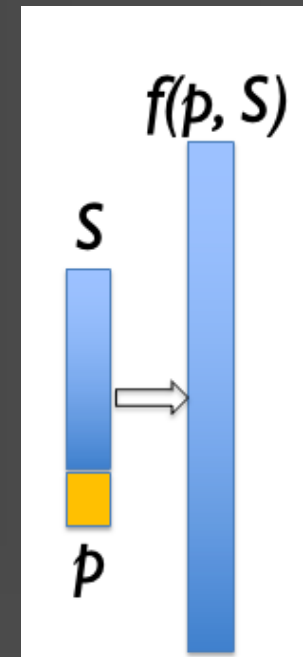
# Voxels vs. implicit functions

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- Voxels: intrinsically **discrete** representation, limited by resolutions
- Implicit functions: intrinsically **continuous** representation
  - There is an implicit field value for any  $(x, y, z)$
  - When processing an implicit function (e.g., rendering), need to discretize

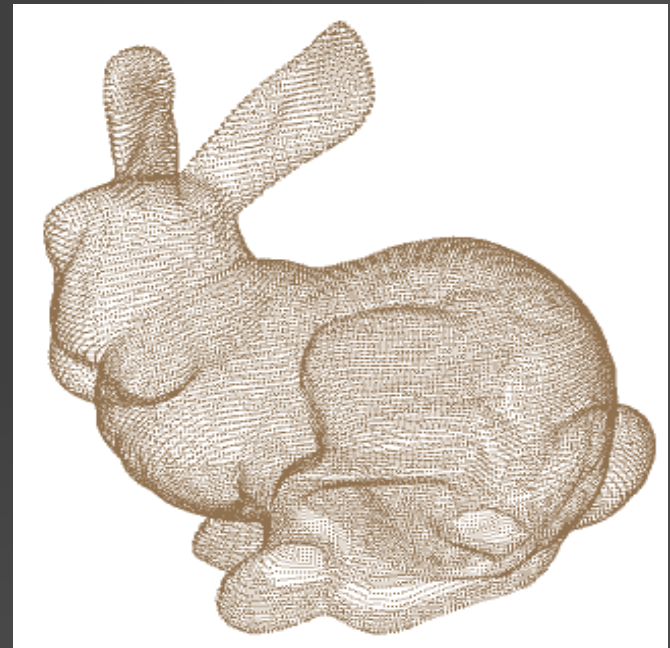
# Voxels vs. implicit functions

- Voxels: intrinsically **discrete** representation, limited by resolutions
- Implicit functions: intrinsically **continuous** representation
  - When processing an implicit function (e.g., rendering), need to discretize
- IM-Net (OCC-Net, DeepSDF) trained on voxel inputs, e.g., on  $64^3$  voxels, can learn **continuous** outputs, for all  $p \in \mathbb{R}^3$



# Point-based representation (PBR)

- A 3D surface model is represented using a set of **points near the surface**
- There is no (explicit) connectivity information between the points
- Typically need  $k$ NN –  **$k$  nearest neighbors** – during processing
- Point normals can also be specified or estimated for rendering



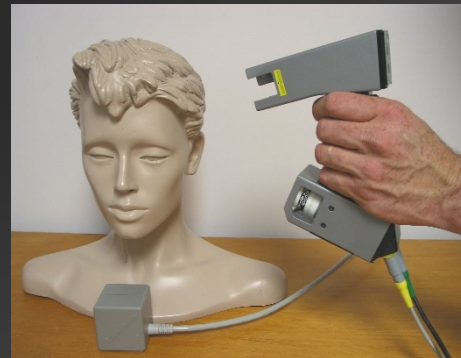
# Point cloud acquisition



Cyberware



InSpeck



FastScan (\$23K)



NextEngine (< \$3K)



Roland DGA LPX-250 (\$10K)

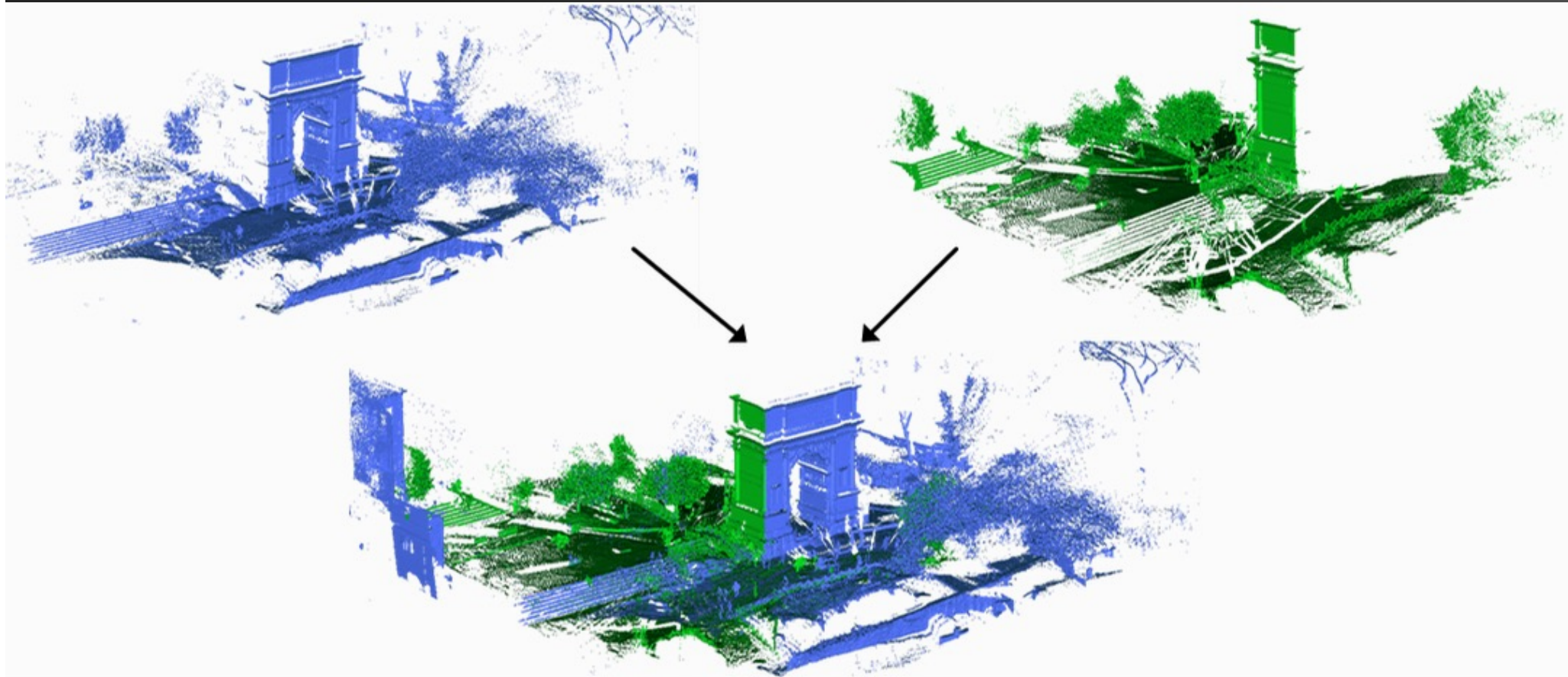


# Point cloud acquisition



NextEngine (< \$3K)

# Point cloud registration



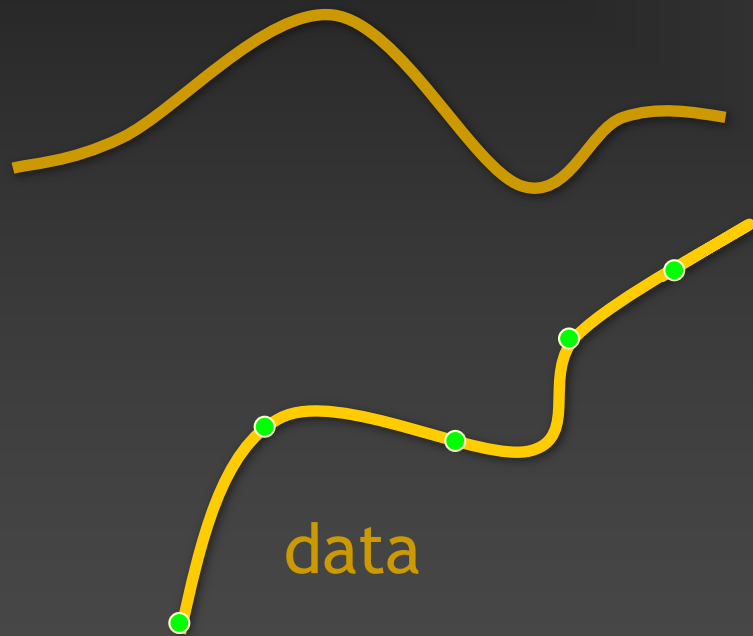
# Iterative closest point (ICP) algorithm

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- A classic registration/correspondence schemes
  - Input: **data** and **model shapes**
  - Objective:
    - Rigid transform = rotation + translation
    - **Minimize mean squared error** from data points to closest points in model [Besl and McKay 92]
  - Correspondence obtained by Euclidean proximity
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# ICP algorithm

model

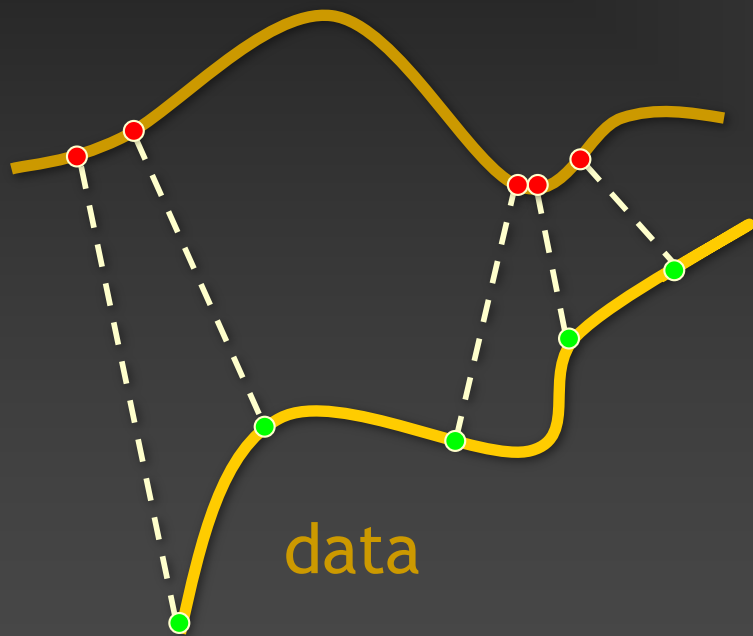


data

Model and data shapes (point samples)

# ICP algorithm

model

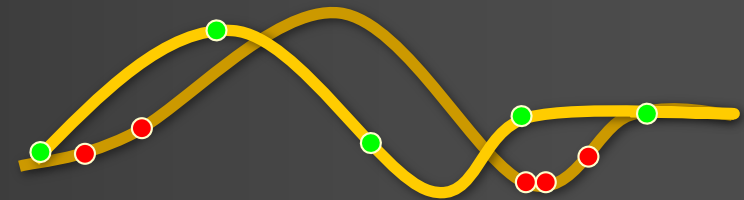
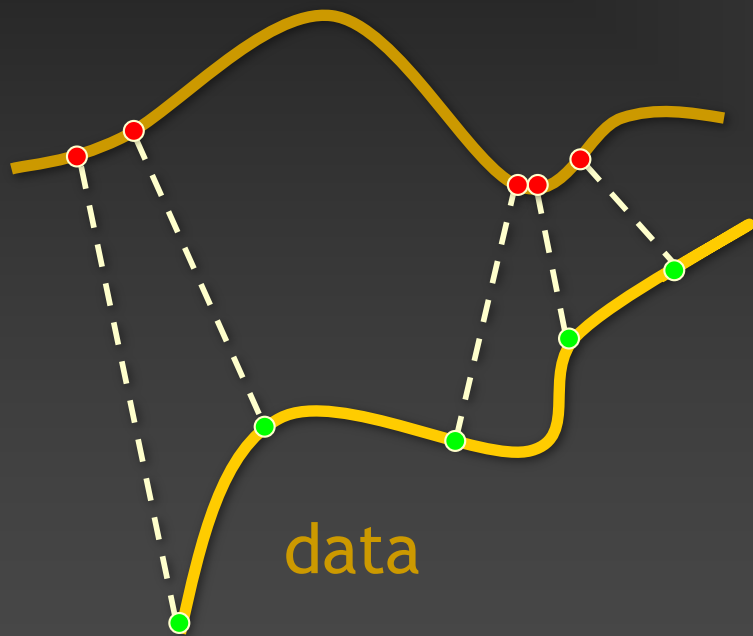


data

Find closest points from data to model

# ICP algorithm

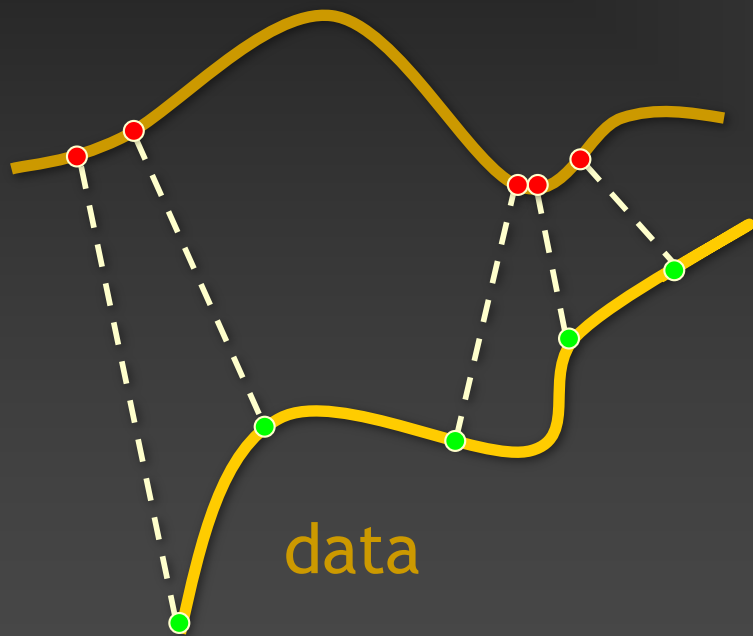
model



Find best rigid transform to align the corresponding points

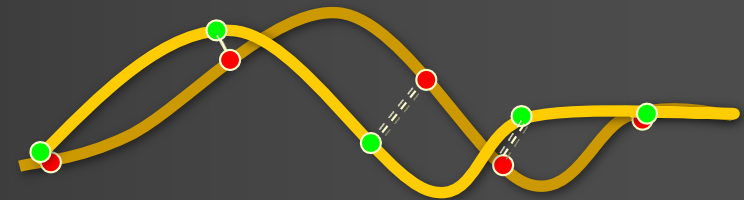
# ICP algorithm

model



data

Iterate ...



# A historical note on PBRs

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- “As the visual complexity of computer-generated scenes continue to increase, the use of classical modeling primitives (polygons) as display primitives becomes less appealing.”

Levoy and Whitted,

“The Use of Points as a Display Primitive”, 1985

- Use of points traces back to modeling of smoke, fire, and cloud around the late 70’s [Csurí et al. 79, Blinn 82]
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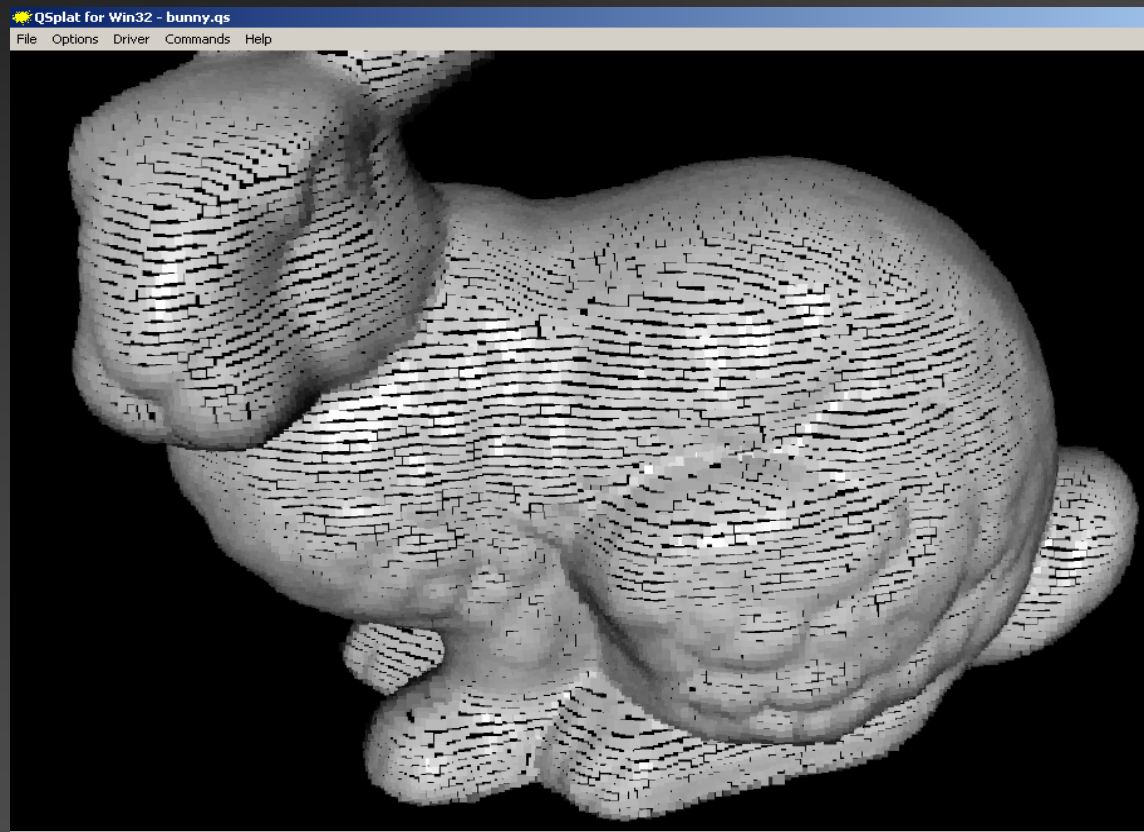


# First renewed interest

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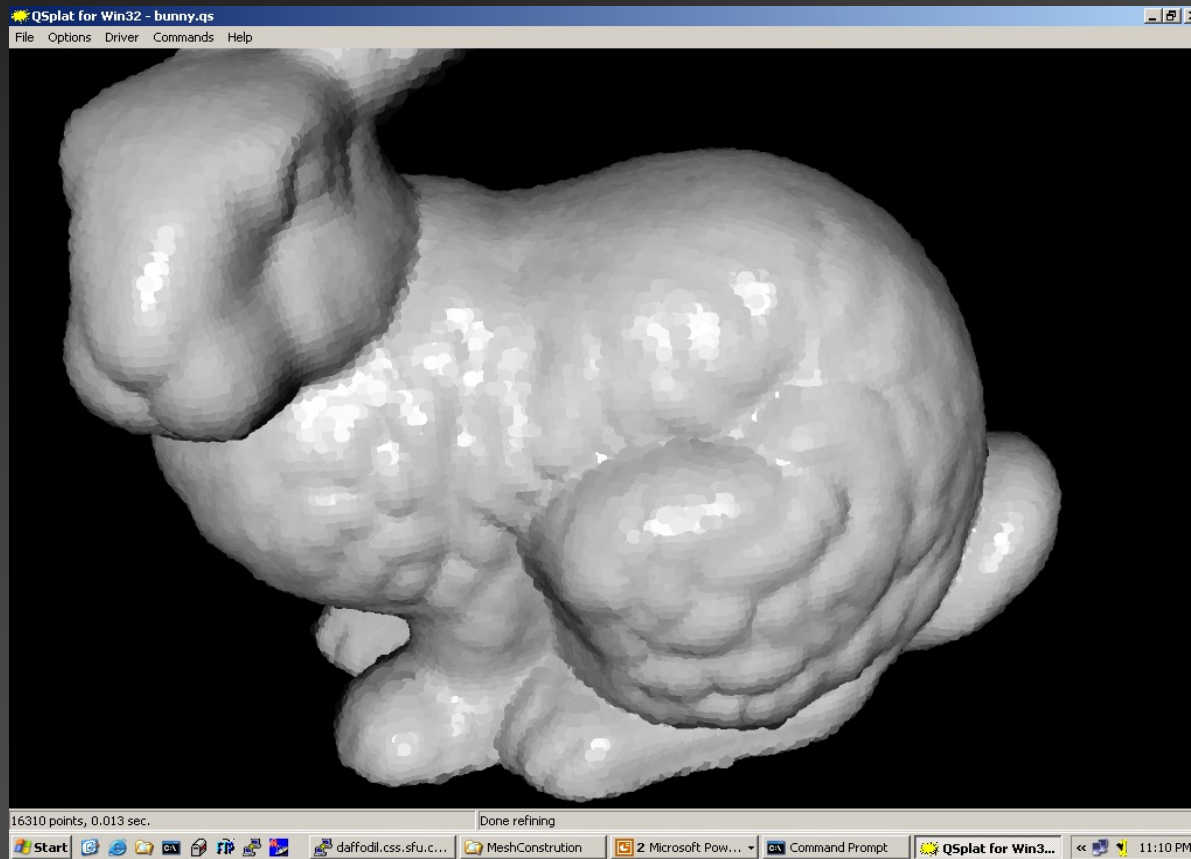
- PBR was witnessing a revival around 2002 - 2012
- Points are directly available via **laser scanning**
  - Substantial advances in 3D digitizing and laser scanning and acquisition technology
  - High quality points (color and texture) easily obtained
  - Cheap scanners (< \$3,000) available now

# PBR rendering via splatting: QSplat



Splat = OpenGL  
points

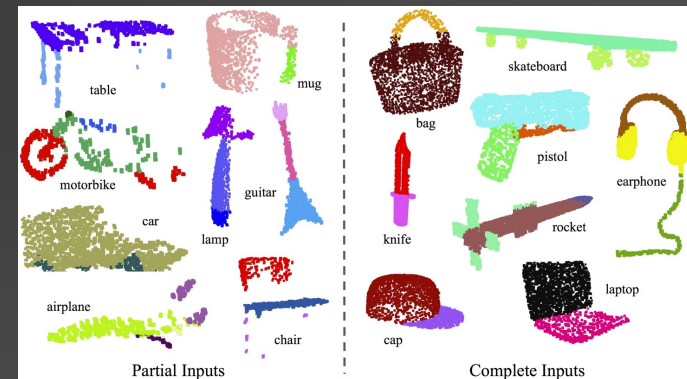
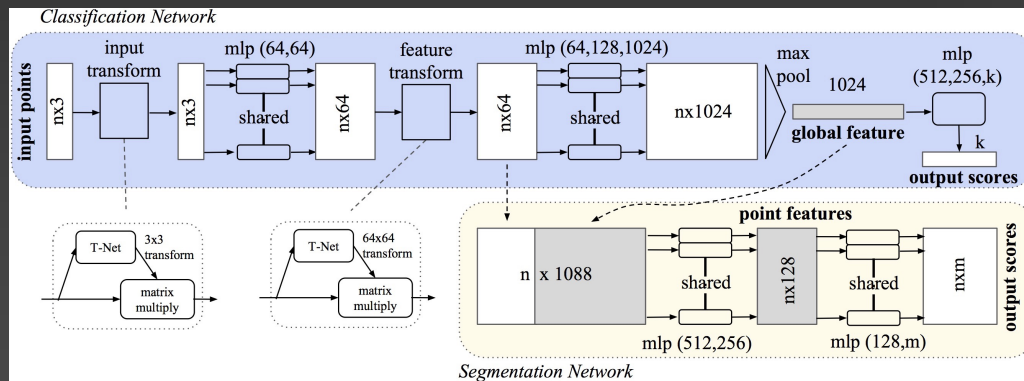
# PBR rendering via splatting: QSplat



Splat = circles

# Second revival: deep learning

- PointNet and PointNET++, since 2016/17
- Deep neural network to **encode and aggregate point features** for shape recognition, segmentation, etc.



# Third revival: 3D Gaussian splatting (3DGS)

- 3DGS [Kerbl et al. SIGGRAPH 2023] superseding NeRF (2000)

