## Assignment 2 for CMPT 307 (2013) September 25, 2013

These problems on Graphs will prepare you for Quiz 1, scheduled to be held on October 1, 2013.

- 1. Exercises 1, 2, 5, 7, 10 of Chapter 3 of the textbook.
- 2. Suppose an adjacent list  $(L_G)$  of a directed graph G = (V, E), |V| = nand |E| = m, is given. Determine the the adjacency list  $(L_{G^{rev}})$  from  $L_G$  where  $G^{rev} = (V, E')$ , and for each  $(u, v) \in E$ ,  $(v, u) \in E'$ .  $G^{rev}$  is called the reverse of G. The algorithm should run in O(m + n) time.
- 3. A tour of a graph G is a closed walk of the nodes which includes every edge of G at least once. An **Euler tour** of an undirected graph G = (V, E) is a tour which includes every edge exactly once (it may visit a node more than once).
  - (a) Show that a connected graph G has an Euler tour if and only if the degree of each node is even.
  - (b) Describe an O(|V| + |E|)-time algorithm to find a Euler tour of G if one exists.