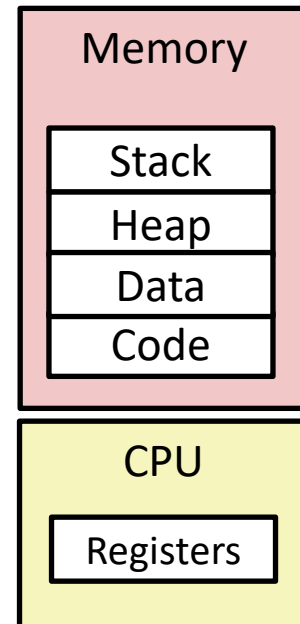


# Caches and Virtual Memory

CMPT 295 Week 8

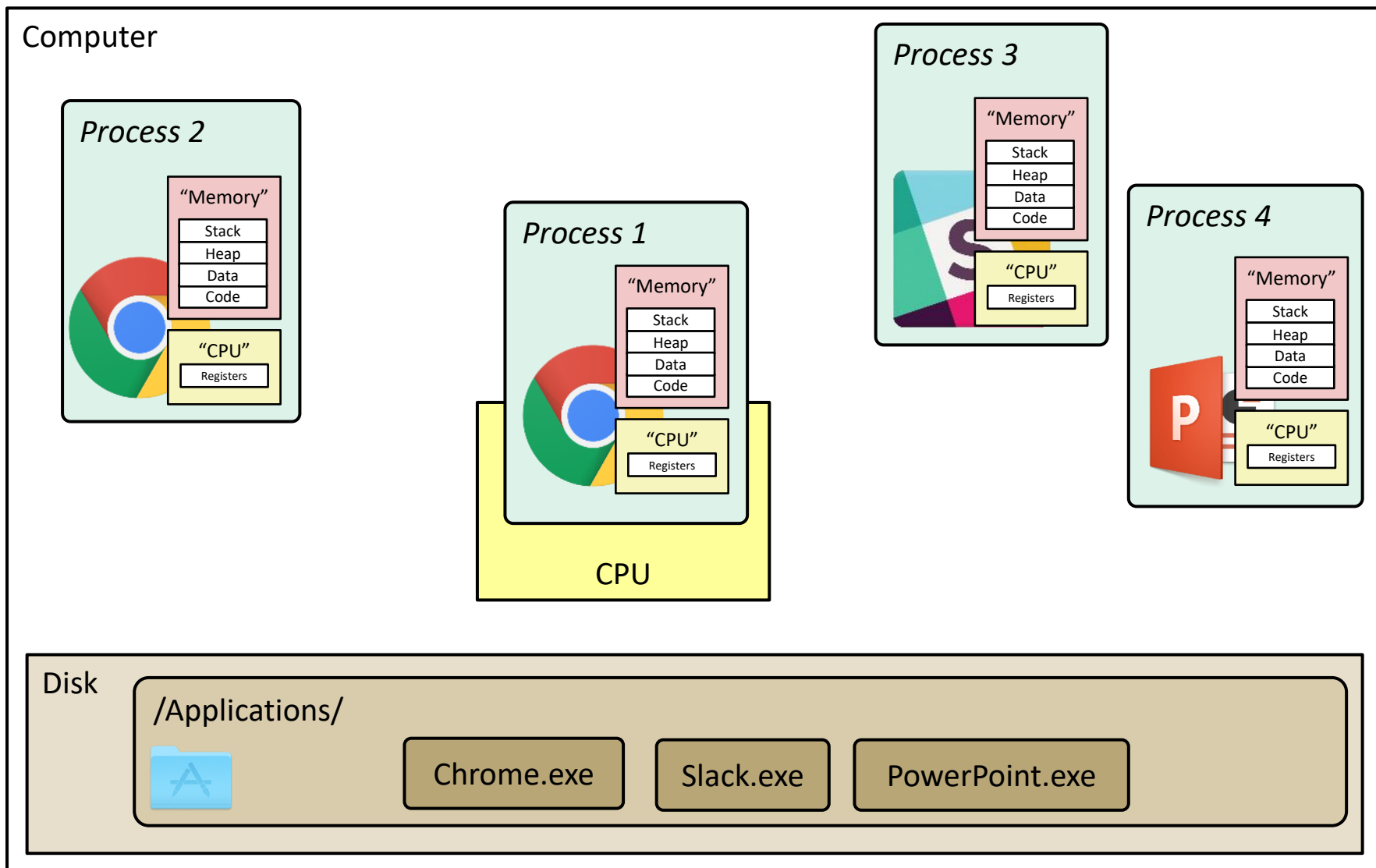
# Processes

- ❖ A **process** is an instance of a running program
  - Provided by the OS
    - OS uses a data structure (PCB) to represent each process
  - Maintains the **interface** between the program and the underlying hardware (CPU + memory)
  
- ❖ “Process” provides each program with two key abstractions:
  - *Logical control flow*
    - Each program seems to have exclusive use of the CPU
    - Provided by kernel mechanism called **context switching**
  - *Private address space*
    - Each program seems to have exclusive use of main memory
    - Provided by kernel mechanism called **virtual memory**



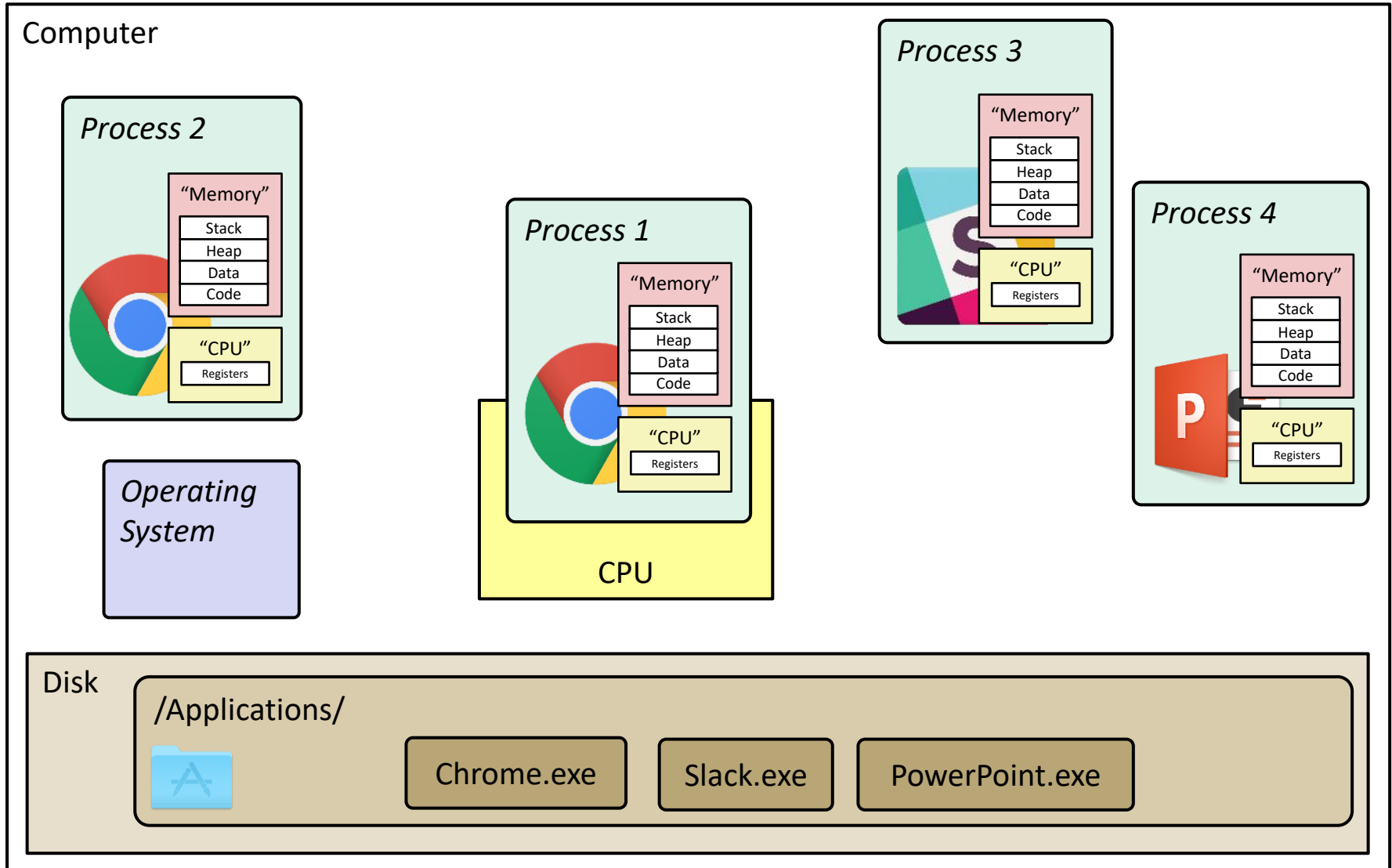
# What is a Process?

It's an *illusion!*

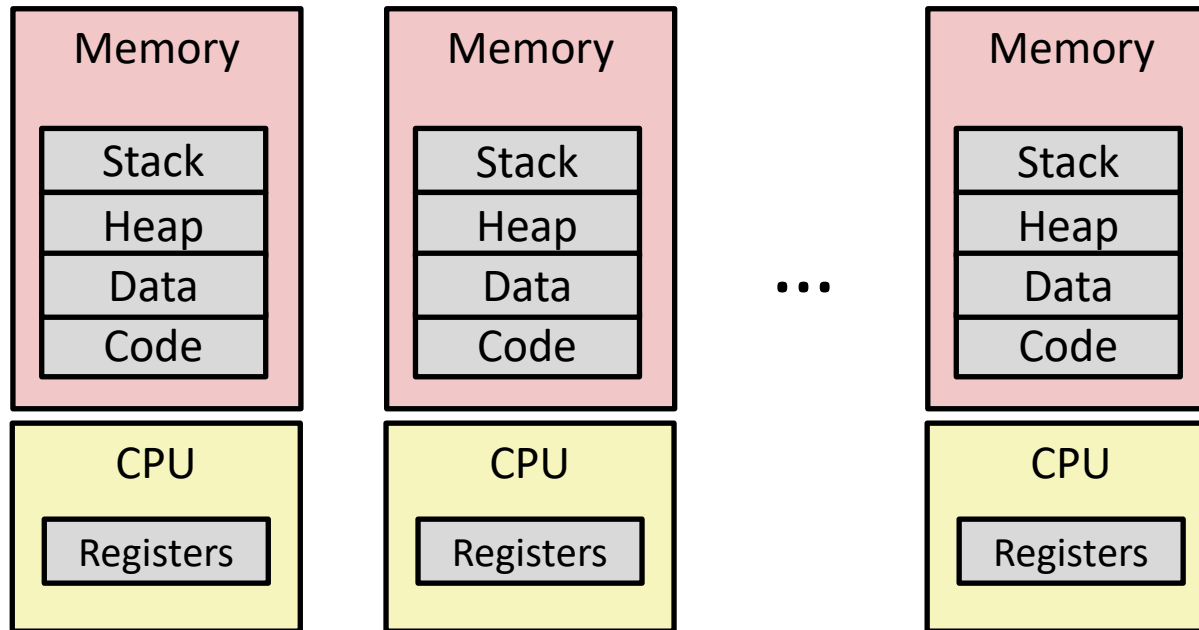


# What is a Process?

*It's an illusion!*

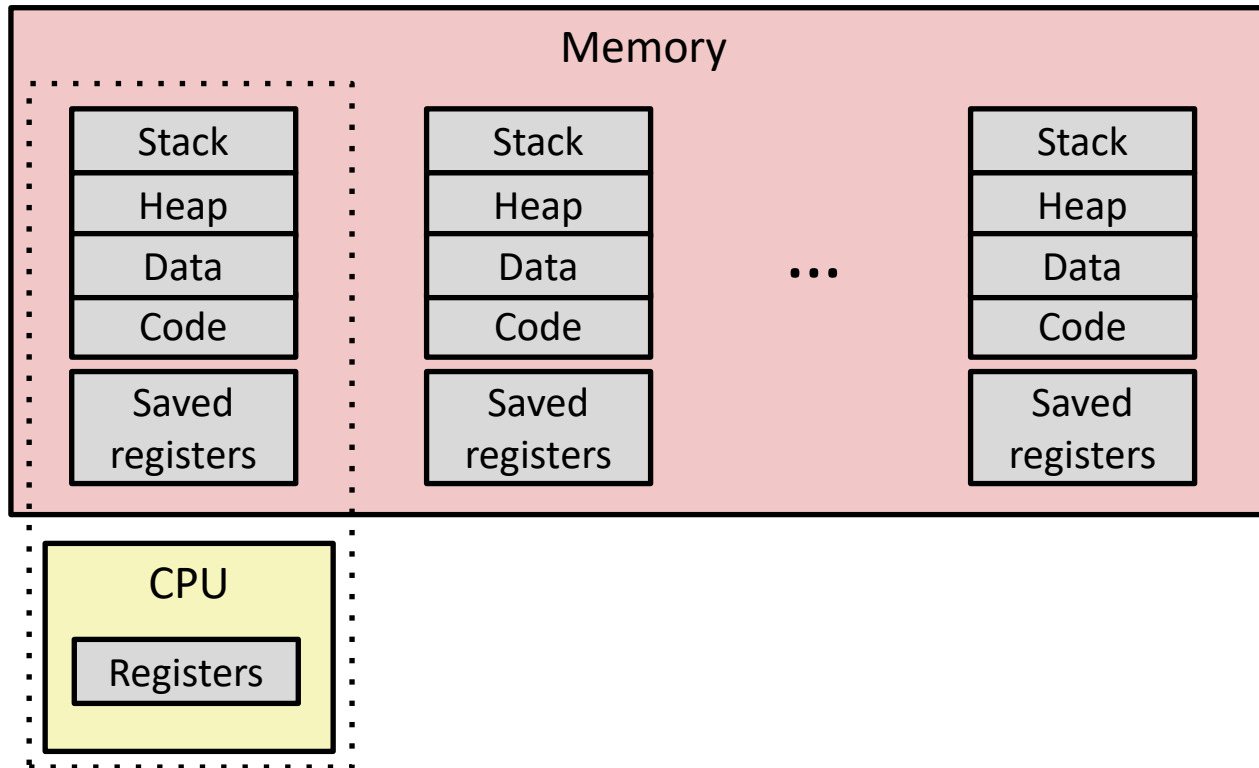


# Multiprocessing: The Illusion



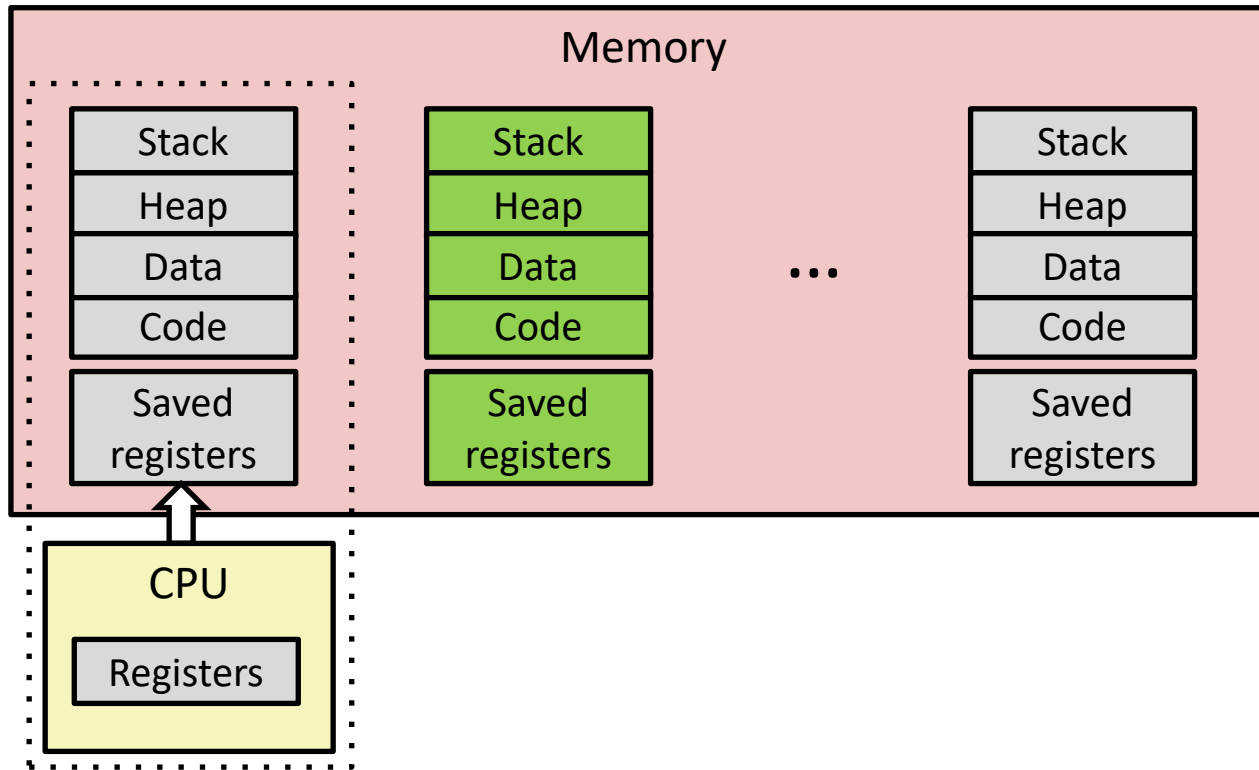
- ❖ Computer runs many processes simultaneously
  - Applications for one or more users
    - Web browsers, email clients, editors, ...
  - Background tasks
    - Monitoring network & I/O devices

# Multiprocessing: The Reality



- ❖ Single processor executes multiple processes *concurrently*
  - Process executions interleaved, CPU runs *one at a time*
  - Address spaces managed by virtual memory system (today's lecture)
  - *Execution context* (register values, stack, ...) for other processes saved in memory

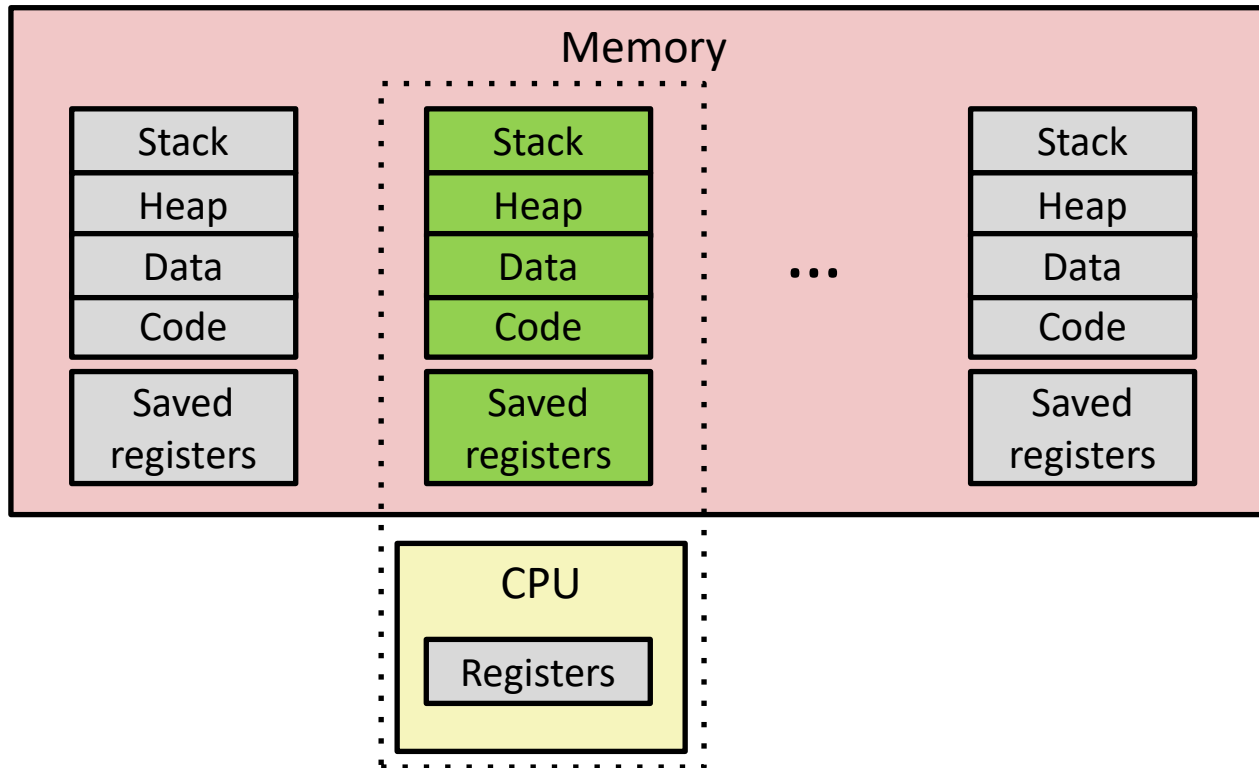
# Multiprocessing



## ❖ Context switch

- 1) Save current registers in memory

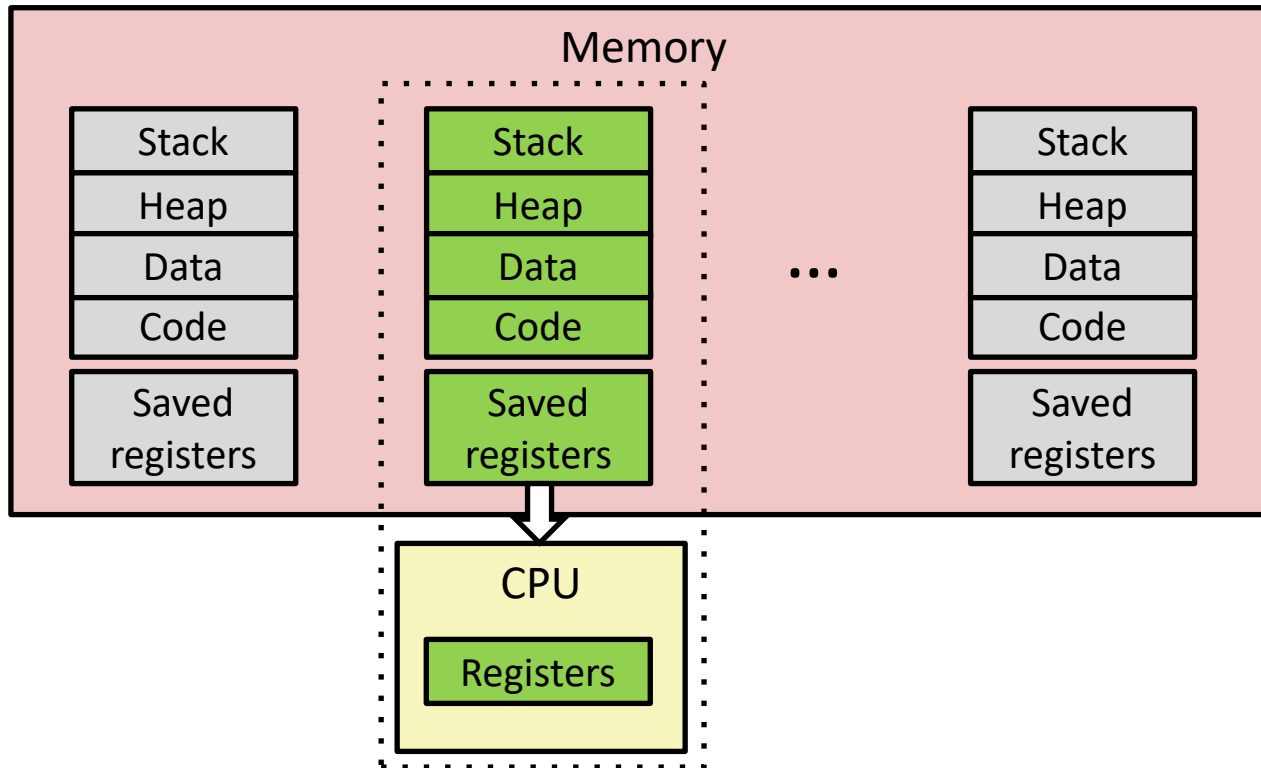
# Multiprocessing



## ❖ Context switch

- 1) Save current registers in memory
- 2) **Schedule next process for execution**

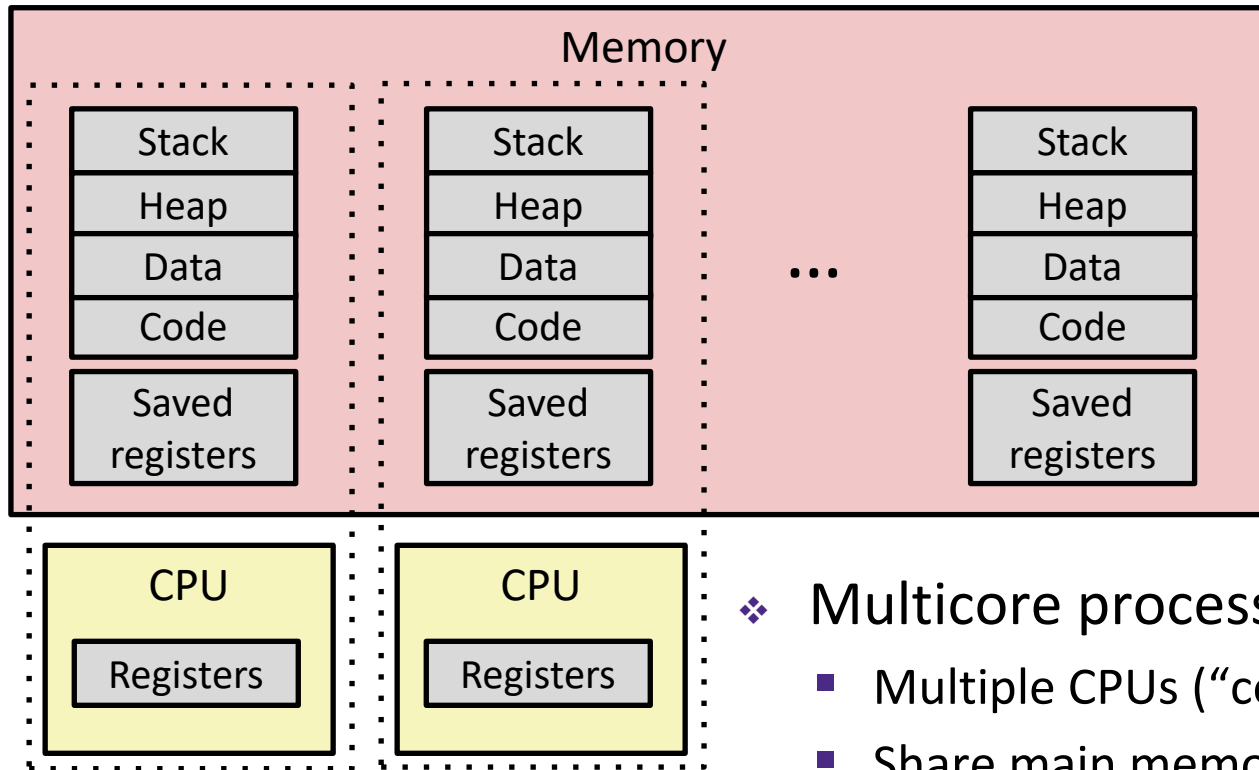
# Multiprocessing



## ❖ Context switch

- 1) Save current registers in memory
- 2) Schedule next process for execution
- 3) **Load saved registers and switch address space**

# Multiprocessing on Multicore Processors

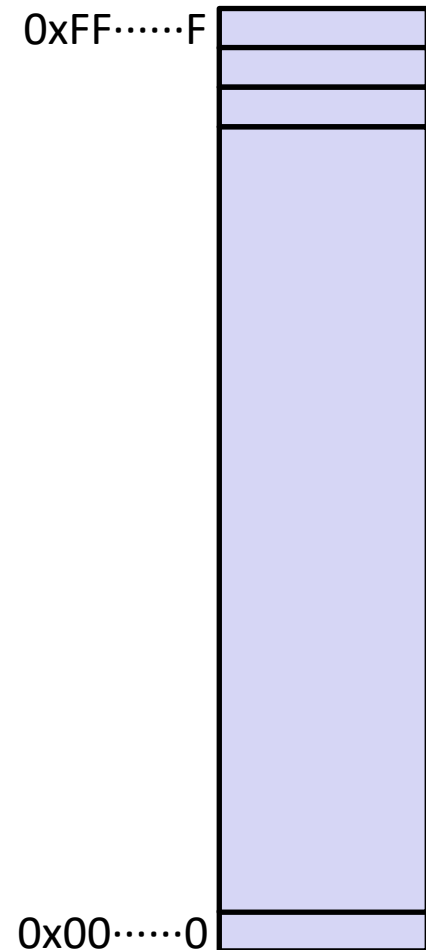


## ❖ Multicore processors

- Multiple CPUs (“cores”) on single chip
- Share main memory (and some of the caches)
- Each can execute a separate process
  - Kernel schedules processes to cores
  - **Still constantly swapping processes**

# Memory as we know it so far... is *virtual*!

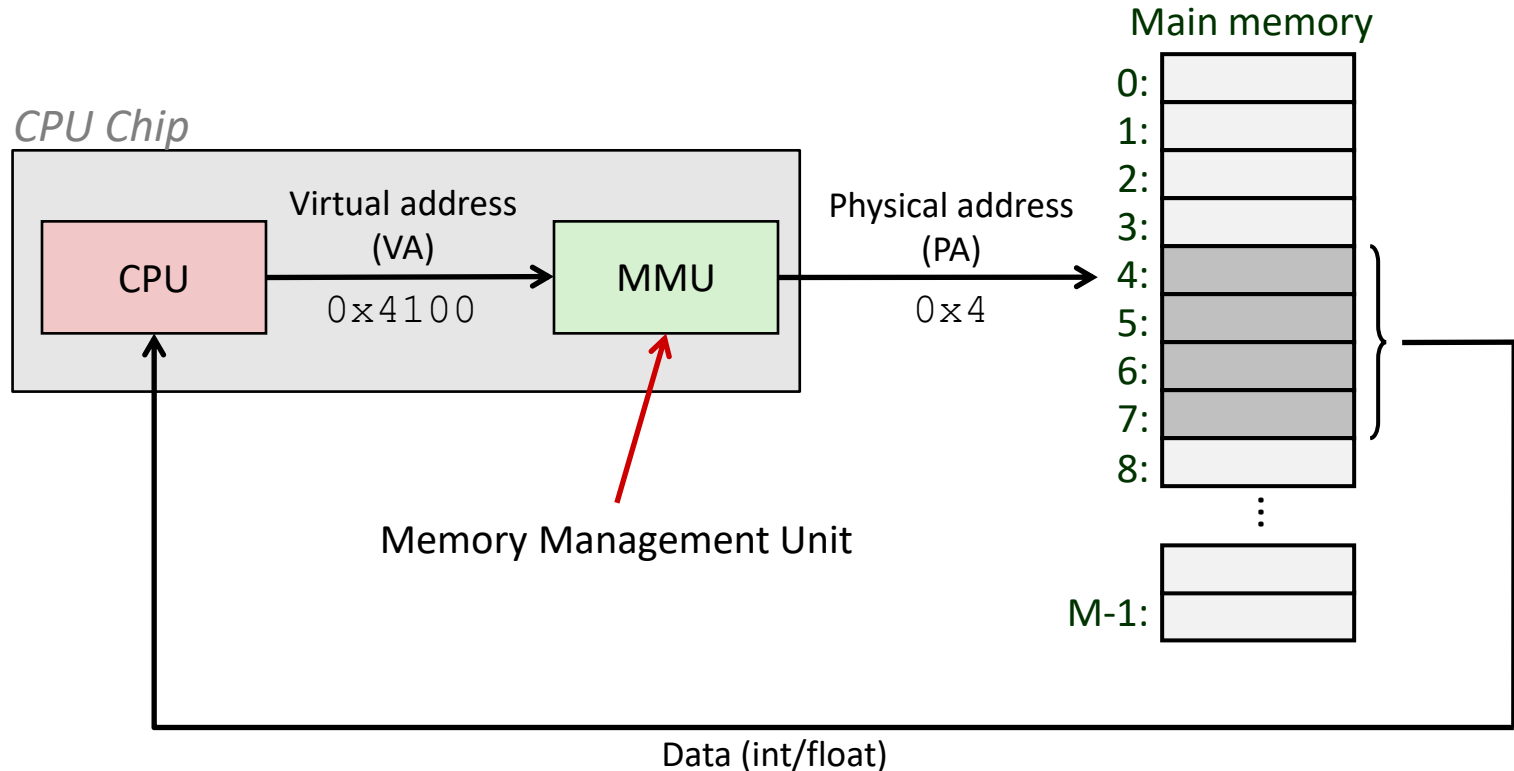
- ❖ Programs refer to virtual memory addresses
  - Conceptually memory is just a very large array of bytes ( $2^w$ ;  $w=64$  for 64-bit machines)
  - System provides private address space to each process
- ❖ Allocation: Compiler and run-time system
  - Where different program objects should be stored
  - All allocation within single virtual address space
- ❖ But...
  - We *probably* don't have  $2^w$  bytes of physical memory
  - We *certainly* don't have  $2^w$  bytes of physical memory *for every process*
  - Processes should not interfere with one another
    - Except in certain cases where they want to share code or data



# Why Virtual Memory (VM)?

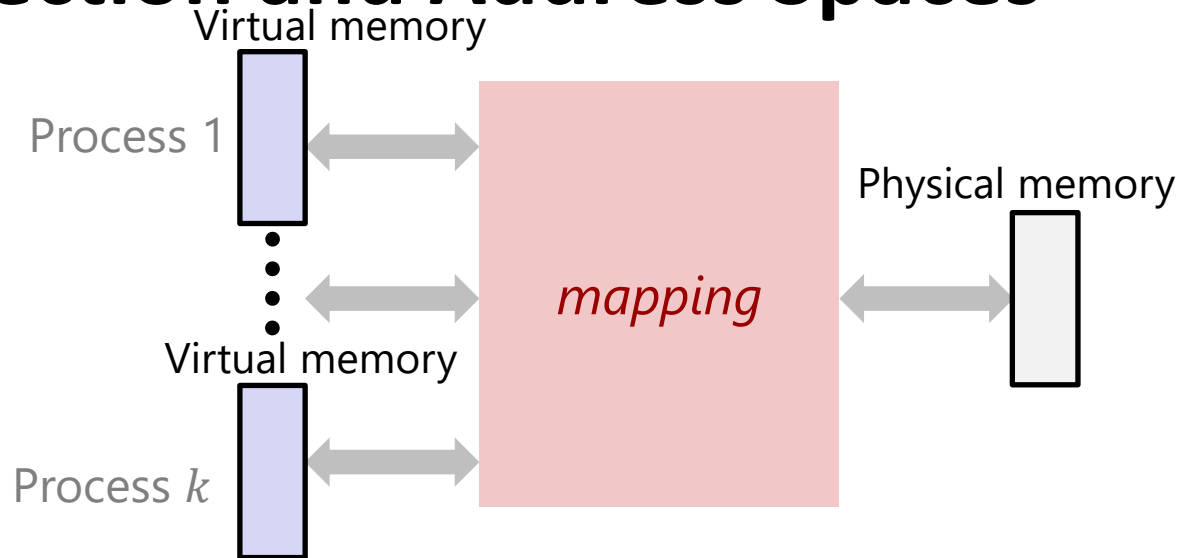
- ❖ Efficient use of limited main memory
  - Use main memory as a cache for parts of a virtual address space
    - Some non-cached parts stored on disk
    - Some (unallocated) non-cached parts stored nowhere
  - Keep only active areas of virtual address space in memory
    - Transfer data back and forth as needed
- ❖ Simplifies memory management for programmers
  - Each process “gets” the same full, private linear address space
- ❖ Isolates address spaces (protection)
  - One process can't interfere with another's memory
    - They operate in *different address spaces*
  - User process cannot access privileged information
    - Different sections of address spaces have different permissions

# A System Using Virtual Addressing



- ❖ Physical addresses are *completely invisible to programs*
  - Used in all modern desktops, laptops, servers, smartphones...
  - One of the great ideas in computer science

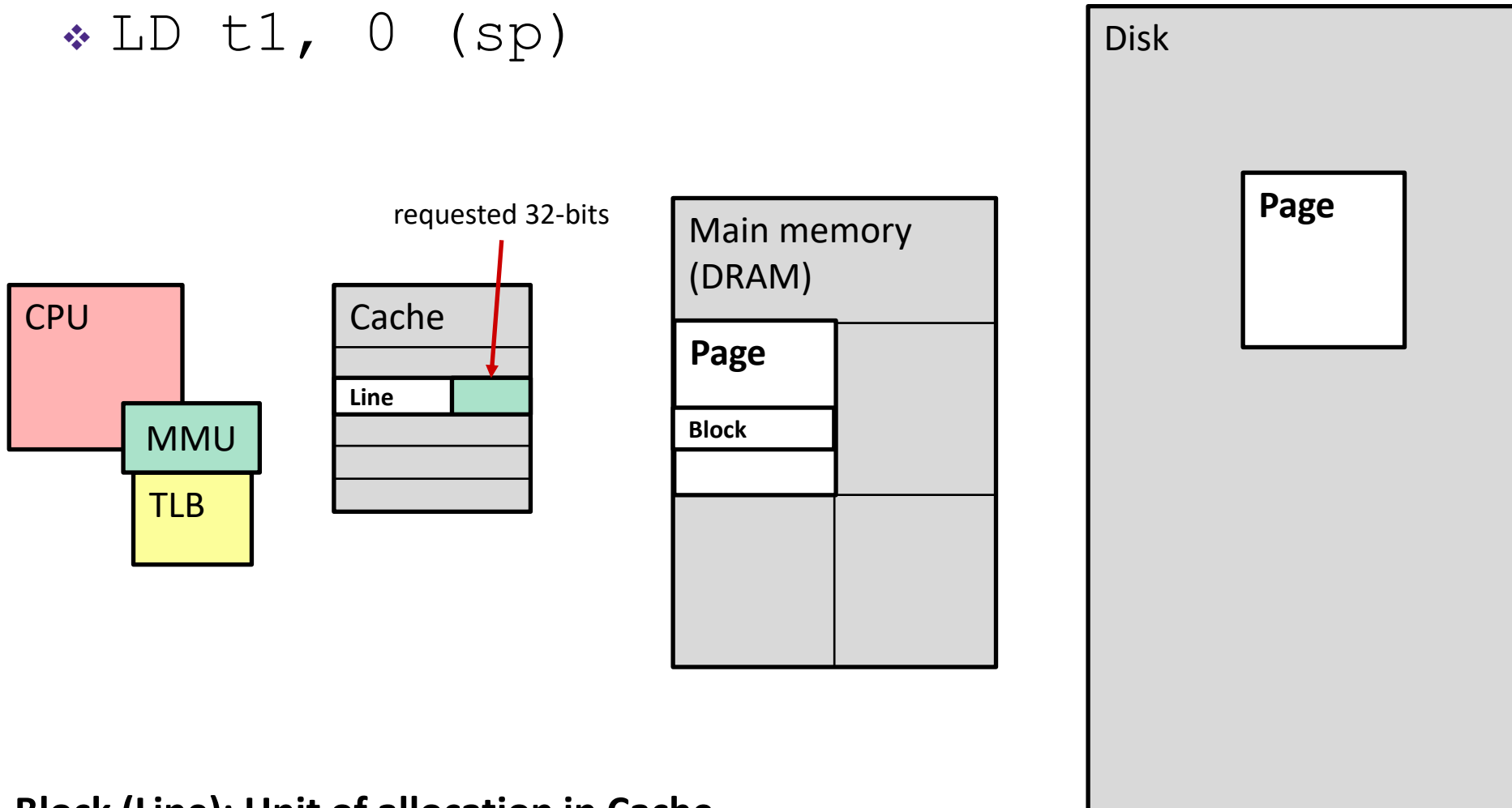
# Indirection and Address Spaces



- ❖ **Virtual address space:** Set of  $N = 2^n$  virtual addresses
  - $\{0, 1, 2, 3, \dots, N-1\}$
- ❖ **Physical address space:** Set of  $M = 2^m$  physical addresses
  - $\{0, 1, 2, 3, \dots, M-1\}$
- ❖ Every byte in main memory has:
  - One physical address (PA)
  - Zero, one, *or more* virtual addresses (VAs)

# Memory Overview

❖ LD t1, 0 (sp)

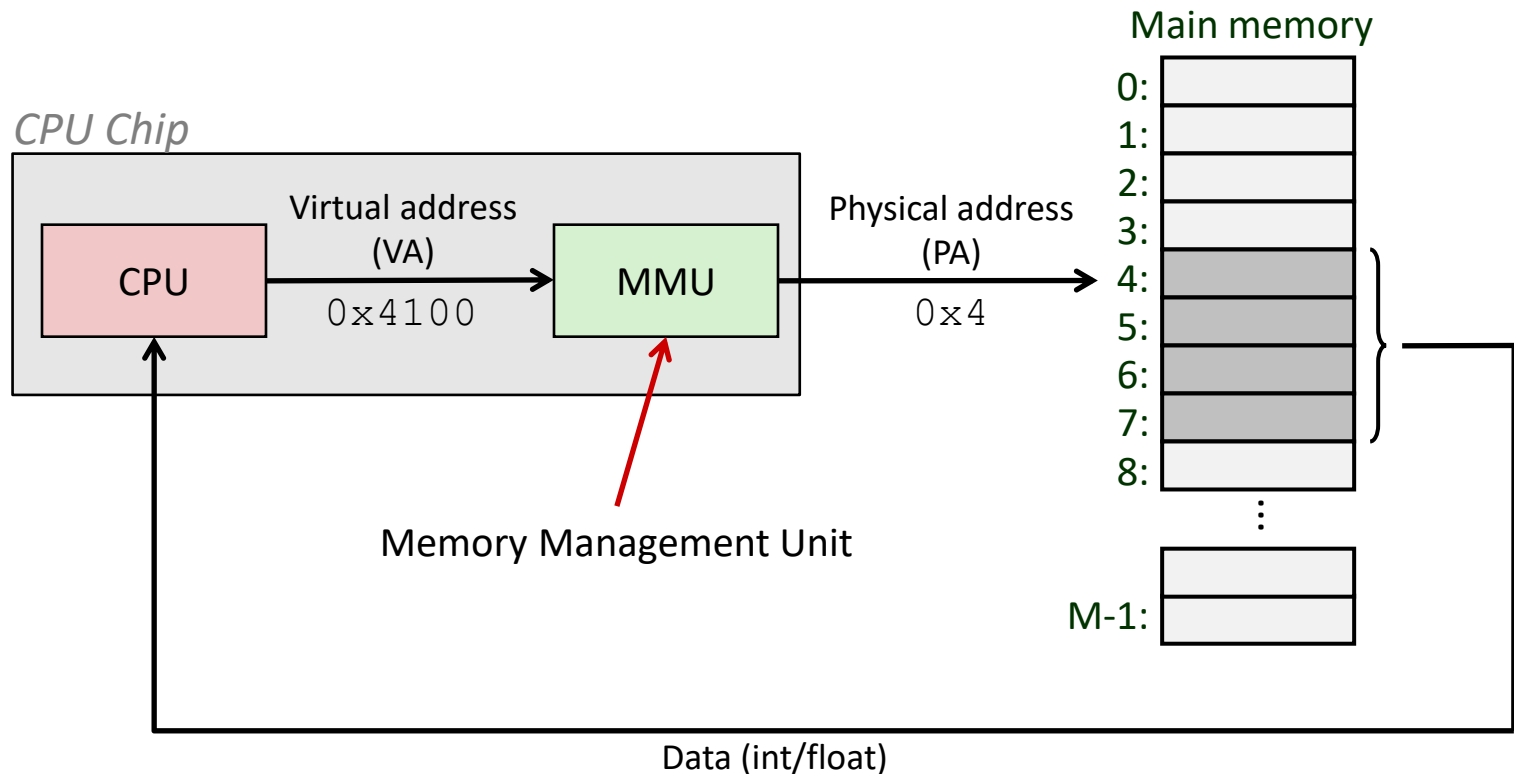


**Block (Line):** Unit of allocation in Cache

**Page:** Unit of allocation in memory (Page size typically much larger than block size)

# Address Translation

*How do we perform the virtual  
→ physical address translation?*



# Address Translation: Page Tables

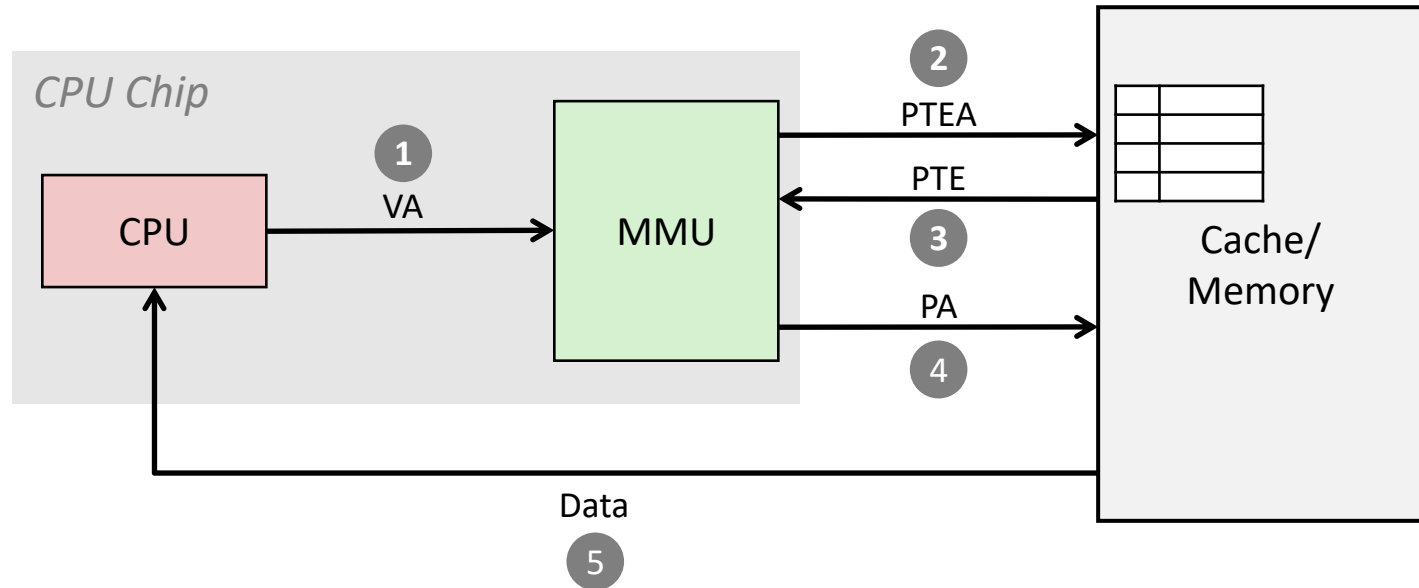
- ❖ CPU-generated address can be split into:

$n$ -bit address: 

Virtual Page Number	Page Offset
---------------------	-------------

- Request is Virtual Address (**VA**), want Physical Address (**PA**)
- Note that Physical Offset = Virtual Offset (page-aligned)
- ❖ Use lookup table called the *Page Table (PT)*
  - Replace Virtual Page Number (**VPN**) with Physical Page Number (**PPN**) to generate Physical Address
  - Index PT using VPN: Page Table Entry (**PTE**) stores the PPN plus management bits (*e.g.* Valid, Dirty, access rights)
  - Has an entry for *every* virtual page

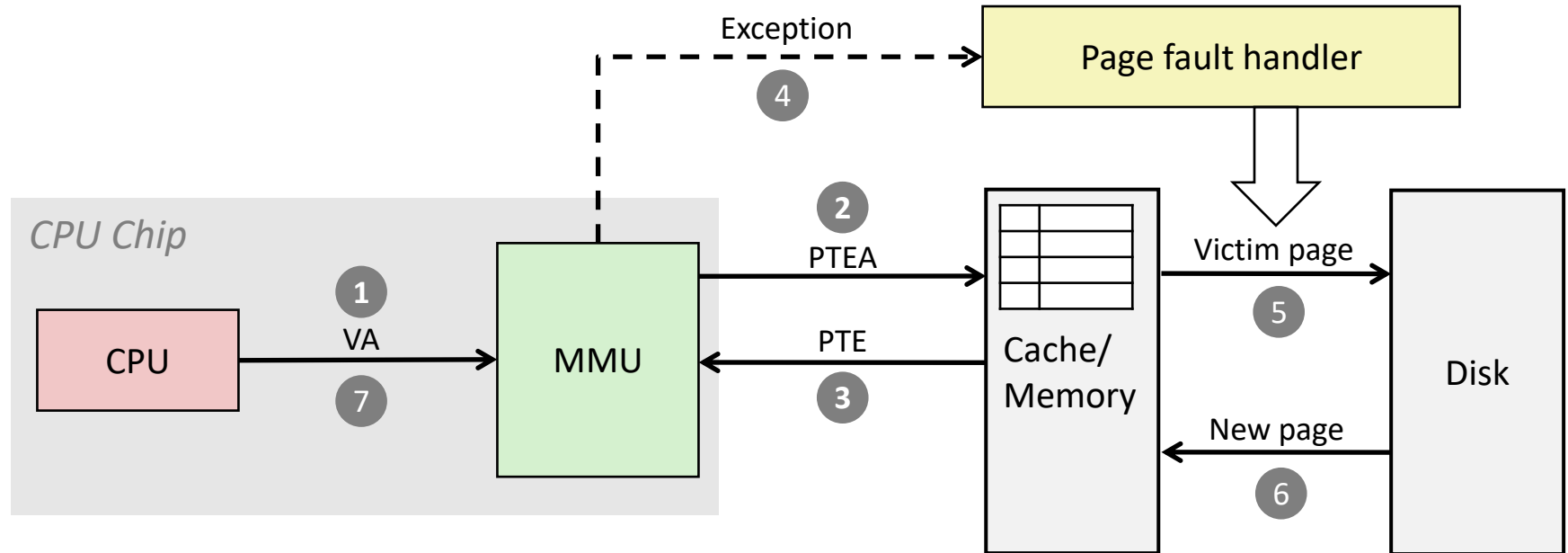
# Address Translation: Page Hit



- 1) Processor sends *virtual* address to MMU (*memory management unit*)
- 2-3) MMU fetches PTE from page table in cache/memory  
(Uses PTBR to find beginning of page table for current process)
- 4) MMU sends *physical* address to cache/memory requesting data
- 5) Cache/memory sends data to processor

VA = Virtual Address      PTEA = Page Table Entry Address      PTE = Page Table Entry  
 PA = Physical Address      Data = Contents of memory stored at VA originally requested by CPU

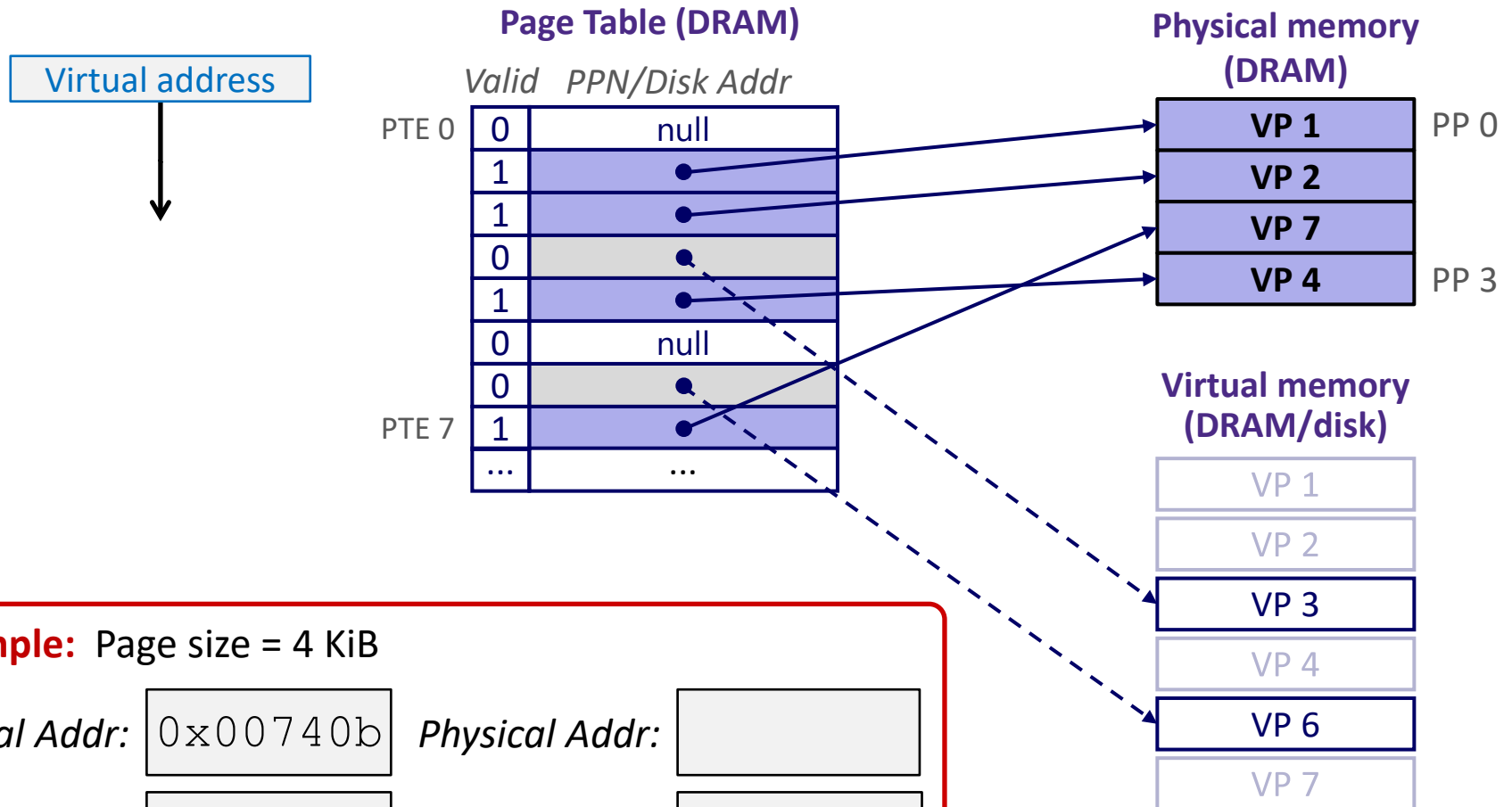
# Address Translation: Page Fault



- 1) Processor sends virtual address to MMU
- 2-3) MMU fetches PTE from page table in cache/memory
- 4) Valid bit is zero, so MMU triggers page fault exception
- 5) Handler identifies victim (and, if dirty, pages it out to disk)
- 6) Handler pages in new page and updates PTE in memory
- 7) Handler returns to original process, restarting faulting instruction

# Page Hit

❖ **Page hit:** VM reference is in physical memory



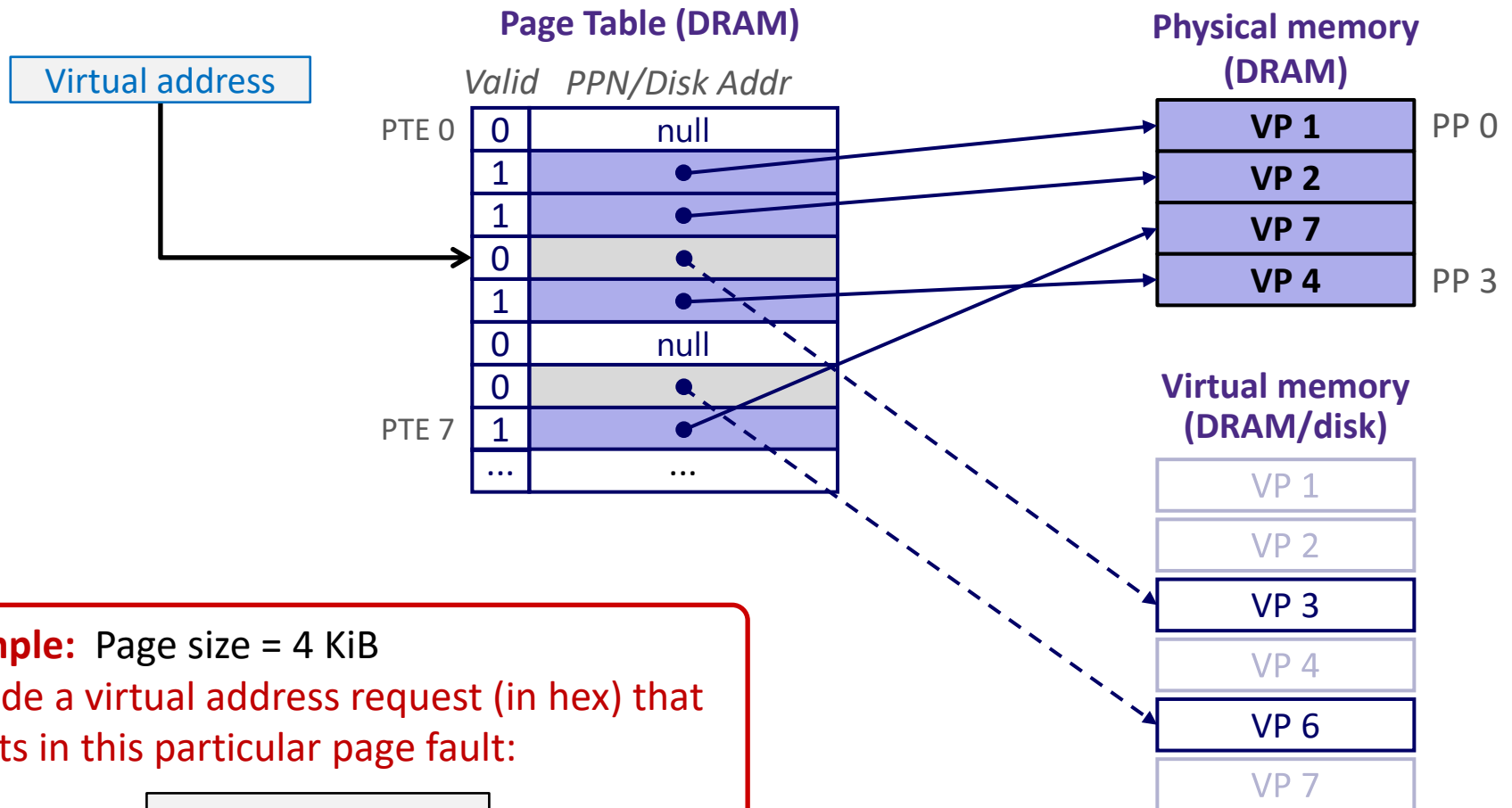
**Example:** Page size = 4 KiB

Virtual Addr:       Physical Addr:

VPN:       PPN:

# Page Fault

❖ **Page fault:** VM reference is NOT in physical memory



**Example:** Page size = 4 KiB

Provide a virtual address request (in hex) that results in this particular page fault:

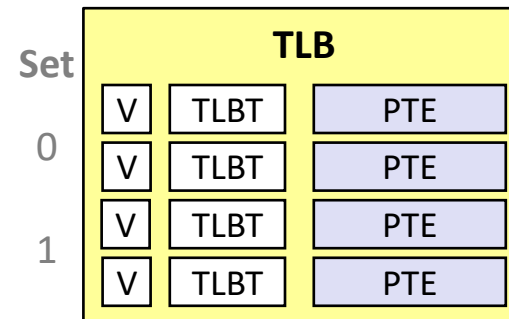
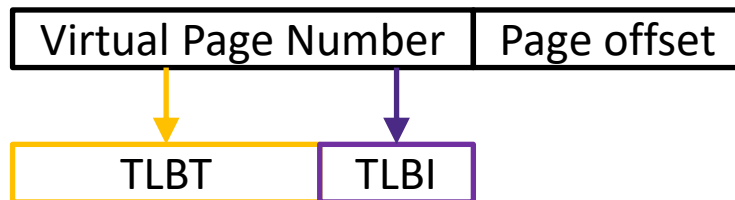
Virtual Addr:

# Address Translation Is Slow

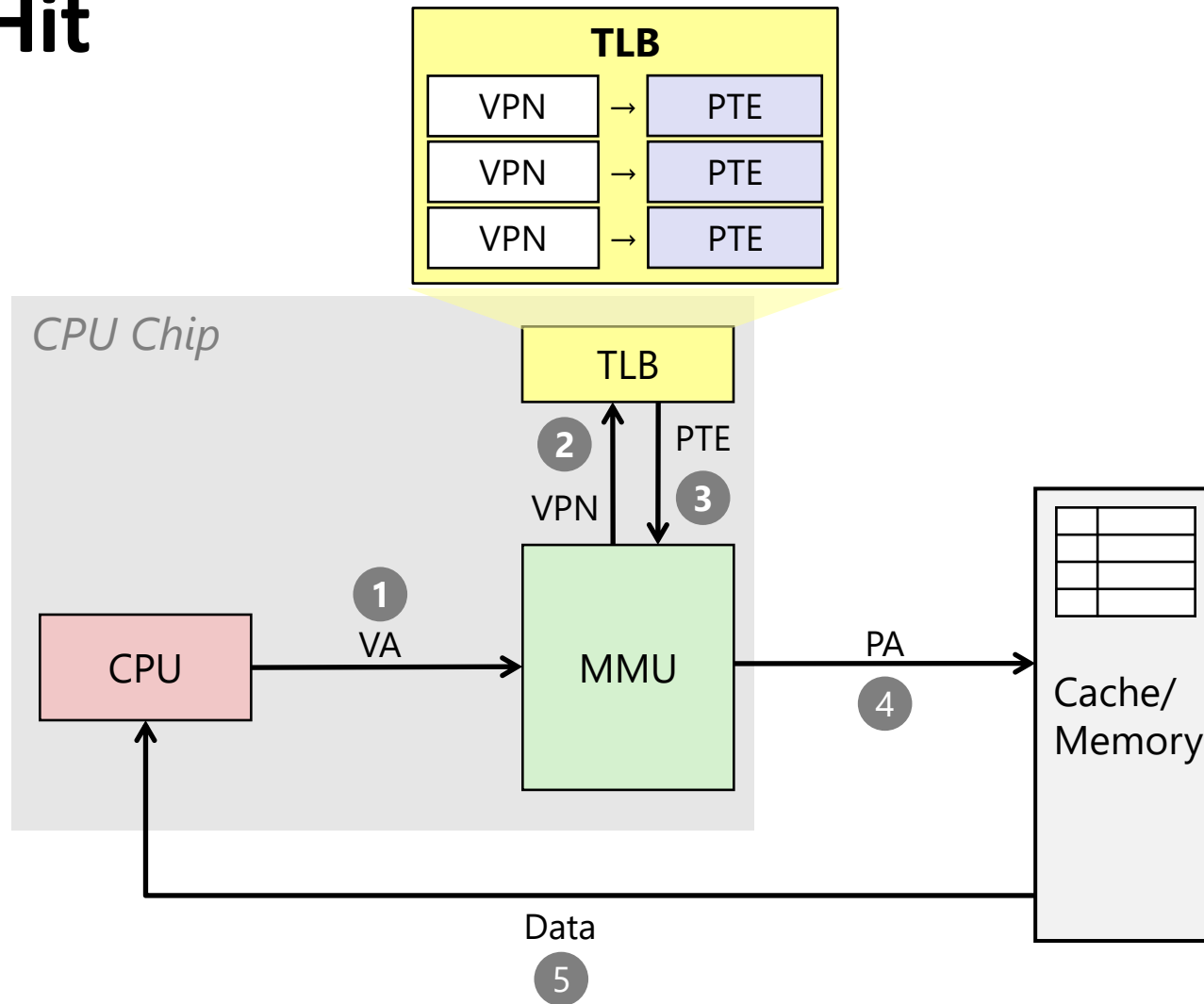
- ❖ The MMU accesses memory *twice*: once to get the PTE for translation, and then again for the actual memory request
  - The PTEs *may* be cached in L1 like any other memory word
    - But they may be evicted by other data references
    - And a hit in the L1 cache still requires 3-4 cycles
  
- ❖ *What can we do to make this faster?*
  - **Solution:** add another cache!

# Speeding up Translation with a TLB

- ❖ *Translation Lookaside Buffer (TLB)*:
  - Small hardware cache in MMU
    - Split VPN into **TLB Tag** and **TLB Index** based on # of sets in TLB
  - Maps virtual page numbers to physical page numbers
  - Stores *page table entries* for a small number of pages
  - Much faster than a page table lookup in cache/memory

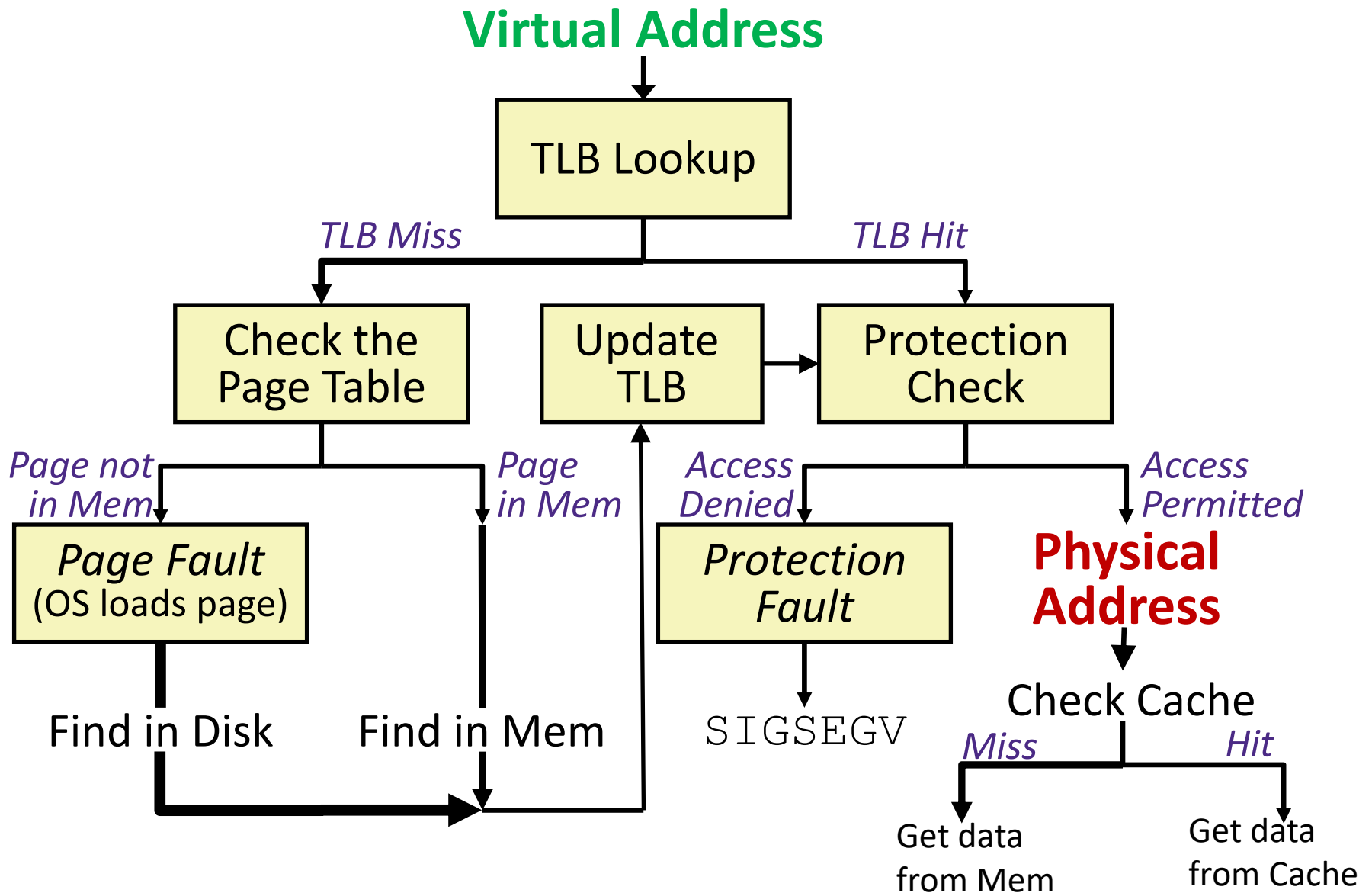


# TLB Hit

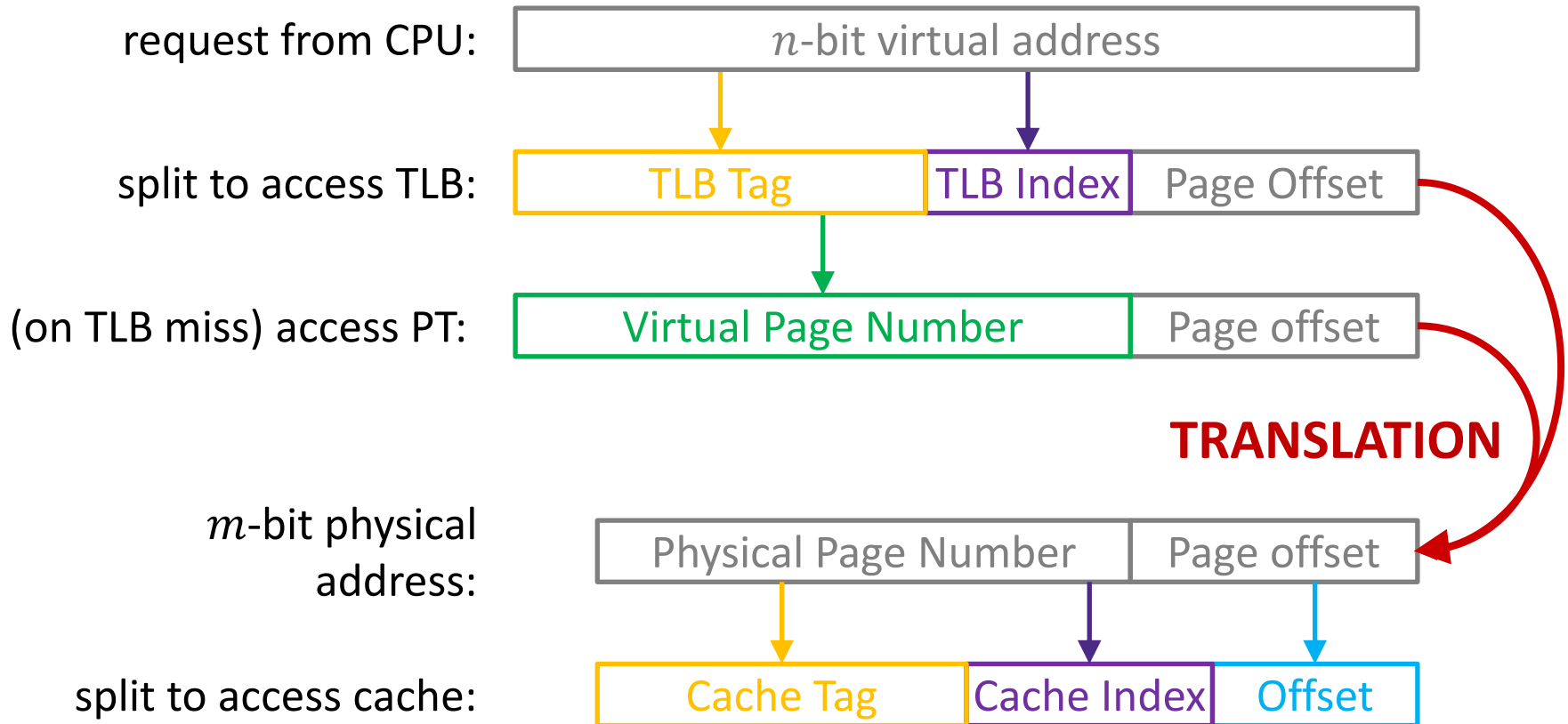


- ❖ A TLB hit eliminates a memory access!

# Address Translation and Memory Access



# Address Manipulation



# Summary of Address Translation Symbols

## ❖ Basic Parameters

- $N = 2^n$  Number of addresses in virtual address space
- $M = 2^m$  Number of addresses in physical address space
- $P = 2^p$  Page size (bytes)

## ❖ Components of the virtual address (VA)

- **VPO** Virtual page offset
- **VPN** Virtual page number
- **TLBI** TLB index
- **TLBT** TLB tag

## ❖ Components of the physical address (PA)

- **PPO** Physical page offset (same as VPO)
- **PPN** Physical page number

# Peer Question

- ❖ How many bits wide are the following fields?
  - 16 KiB pages
  - 48-bit virtual addresses
  - 16 GiB physical memory

	VPN	PPN
(A)	34	24
(B)	32	18
(C)	30	20
(D)	34	20

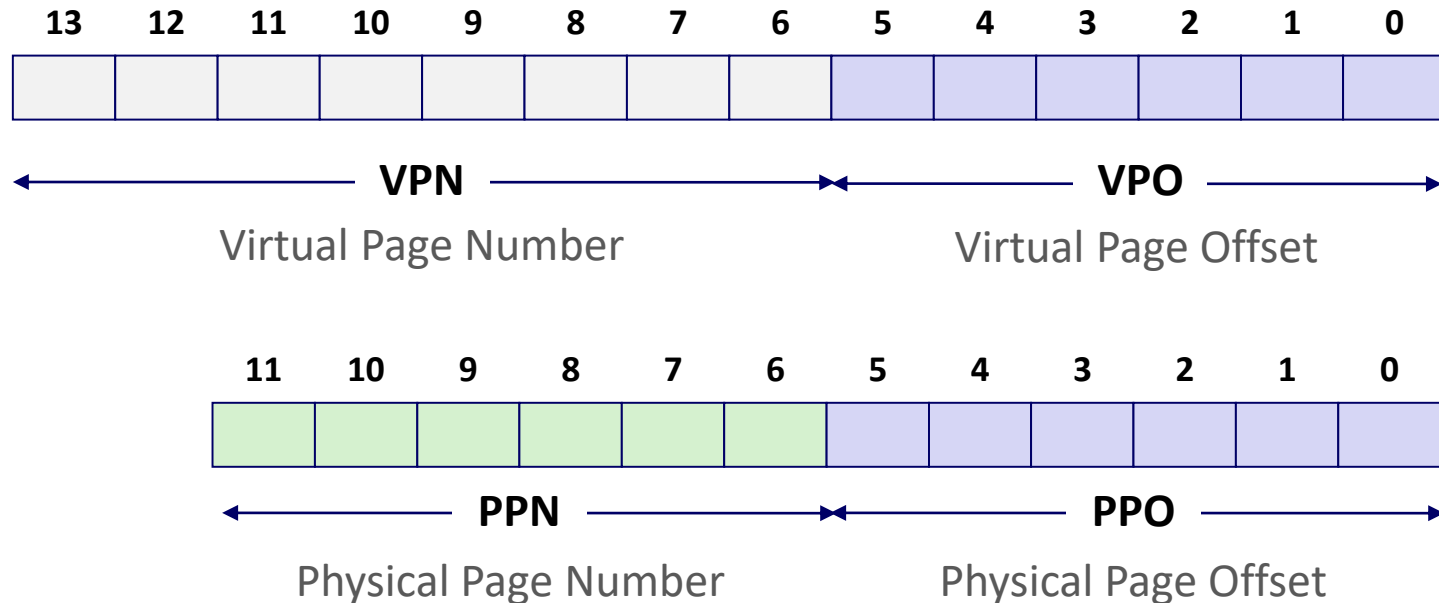
# Some VM Topics Not Covered in 295

- ❖ Supporting more than one page size
  - Small pages lead to more TLB misses; large pages lead to fragmentation
  - Modern CPUs support >1 page size (e.g., 4KB, 2MB, 1GB)
- ❖ Multi-level page tables
  - Needed to support large VM address space
  - [https://en.wikipedia.org/wiki/Intel\\_5-level\\_paging](https://en.wikipedia.org/wiki/Intel_5-level_paging)
- ❖ TLB hierarchy
  - Modern CPUs have more than one level in TLB
  - L1 usually split into two structures, one for instructions (iTLB) and another for data (dTLB). Entries 32-256
  - L2 TLB unified (instructions and data), 512-2048 entries

# Simple Memory System Example (small)

## ❖ Addressing

- 14-bit virtual addresses
- 12-bit physical address
- Page size = 64 bytes



# Simple Memory System: Page Table

- ❖ Only showing first 16 entries (out of \_\_\_\_\_)
  - **Note:** Showing 2 hex digits for PPN even though only 6 bits
  - **Note:** Other management bits not shown, but part of PTE

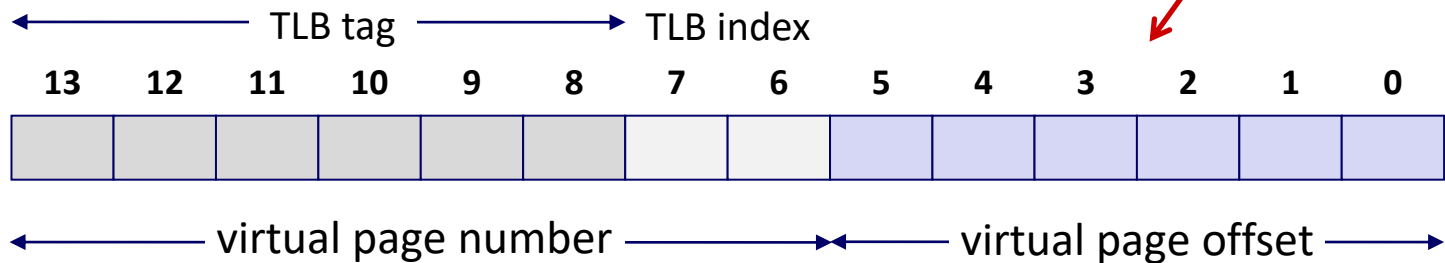
<i>VPN</i>	<i>PPN</i>	<i>Valid</i>
<b>0</b>	28	1
<b>1</b>	–	0
<b>2</b>	33	1
<b>3</b>	02	1
<b>4</b>	–	0
<b>5</b>	16	1
<b>6</b>	–	0
<b>7</b>	–	0

<i>VPN</i>	<i>PPN</i>	<i>Valid</i>
<b>8</b>	13	1
<b>9</b>	17	1
<b>A</b>	09	1
<b>B</b>	–	0
<b>C</b>	–	0
<b>D</b>	2D	1
<b>E</b>	–	0
<b>F</b>	0D	1

# Simple Memory System: TLB

- ❖ 16 entries total
- ❖ 4-way set associative

Why does the TLB ignore the page offset?

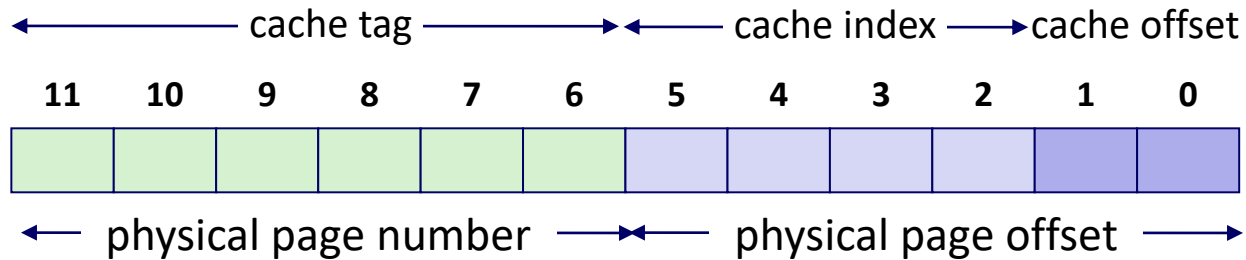


<i>Set</i>	<i>Tag</i>	<i>PPN</i>	<i>Valid</i>	<i>Tag</i>	<i>PPN</i>	<i>Valid</i>	<i>Tag</i>	<i>PPN</i>	<i>Valid</i>	<i>Tag</i>	<i>PPN</i>	<i>Valid</i>
<b>0</b>	03	–	0	09	0D	1	00	–	0	07	02	1
<b>1</b>	03	2D	1	02	–	0	04	–	0	0A	–	0
<b>2</b>	02	–	0	08	–	0	06	–	0	03	–	0
<b>3</b>	07	–	0	03	0D	1	0A	34	1	02	–	0

# Simple Memory System: Cache

**Note:** It is just coincidence that the PPN is the same width as the cache Tag

- ❖ Direct-mapped with  $K = 4 \text{ B}$ ,  $C/K = 16$
- ❖ Physically addressed



Index	Tag	Valid	B0	B1	B2	B3
0	19	1	99	11	23	11
1	15	0	-	-	-	-
2	1B	1	00	02	04	08
3	36	0	-	-	-	-
4	32	1	43	6D	8F	09
5	0D	1	36	72	F0	1D
6	31	0	-	-	-	-
7	16	1	11	C2	DF	03

Index	Tag	Valid	B0	B1	B2	B3
8	24	1	3A	00	51	89
9	2D	0	-	-	-	-
A	2D	1	93	15	DA	3B
B	0B	0	-	-	-	-
C	12	0	-	-	-	-
D	16	1	04	96	34	15
E	13	1	83	77	1B	D3
F	14	0	-	-	-	-

# Current State of Memory System

## TLB:

Set	Tag	PPN	V	Tag	PPN	V	Tag	PPN	V	Tag	PPN	V
0	03	-	0	09	0D	1	00	-	0	07	02	1
1	03	2D	1	02	-	0	04	-	0	0A	-	0
2	02	-	0	08	-	0	06	-	0	03	-	0
3	07	-	0	03	0D	1	0A	34	1	02	-	0

## Page table (partial):

VPN	PPN	V	VPN	PPN	V
0	28	1	8	13	1
1	-	0	9	17	1
2	33	1	A	09	1
3	02	1	B	-	0
4	-	0	C	-	0
5	16	1	D	2D	1
6	-	0	E	-	0
7	-	0	F	0D	1

## Cache:

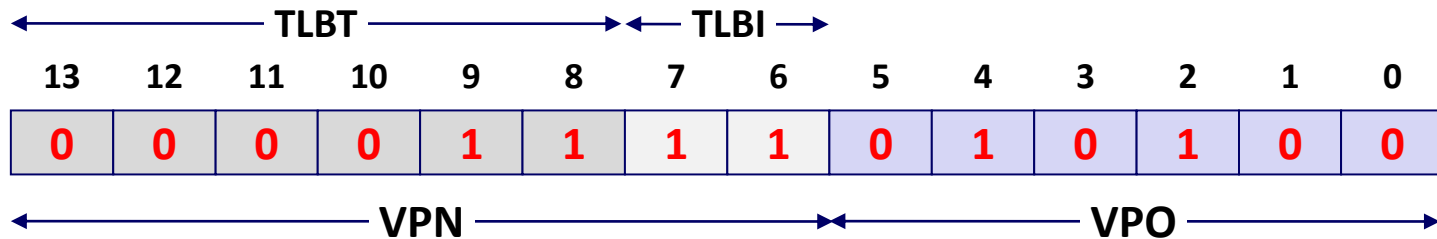
Index	Tag	V	B0	B1	B2	B3
0	19	1	99	11	23	11
1	15	0	-	-	-	-
2	1B	1	00	02	04	08
3	36	0	-	-	-	-
4	32	1	43	6D	8F	09
5	0D	1	36	72	F0	1D
6	31	0	-	-	-	-
7	16	1	11	C2	DF	03

Index	Tag	V	B0	B1	B2	B3
8	24	1	3A	00	51	89
9	2D	0	-	-	-	-
A	2D	1	93	15	DA	3B
B	0B	0	-	-	-	-
C	12	0	-	-	-	-
D	16	1	04	96	34	15
E	13	1	83	77	1B	D3
F	14	0	-	-	-	-

# Memory Request Example #1

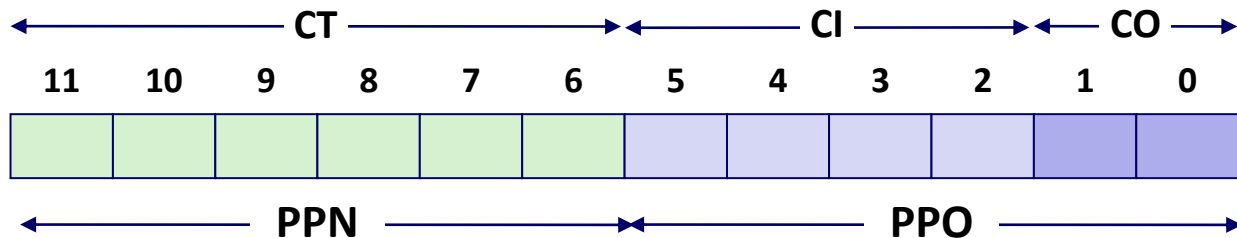
**Note:** It is just coincidence that the PPN is the same width as the cache Tag

❖ Virtual Address: 0x03D4



VPN \_\_\_\_\_ TLBT \_\_\_\_\_ TLBI \_\_\_\_\_ TLB Hit? \_\_\_\_ Page Fault? \_\_\_\_ PPN \_\_\_\_\_

❖ Physical Address:

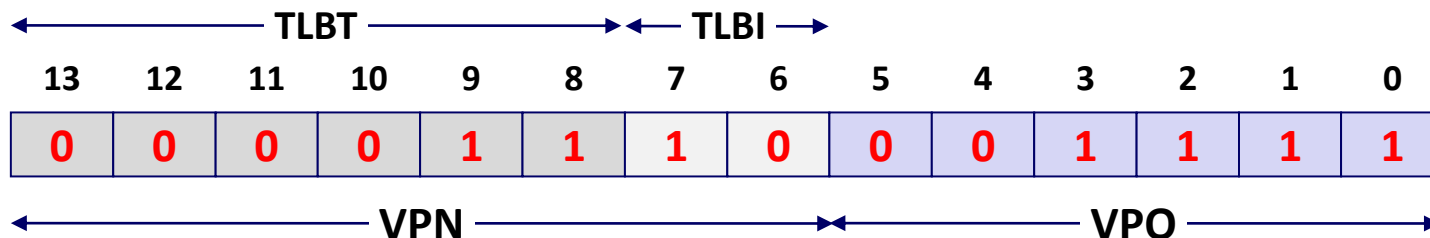


CT \_\_\_\_\_ CI \_\_\_\_\_ CO \_\_\_\_\_ Cache Hit? \_\_\_\_ Data (byte) \_\_\_\_\_

# Memory Request Example #2

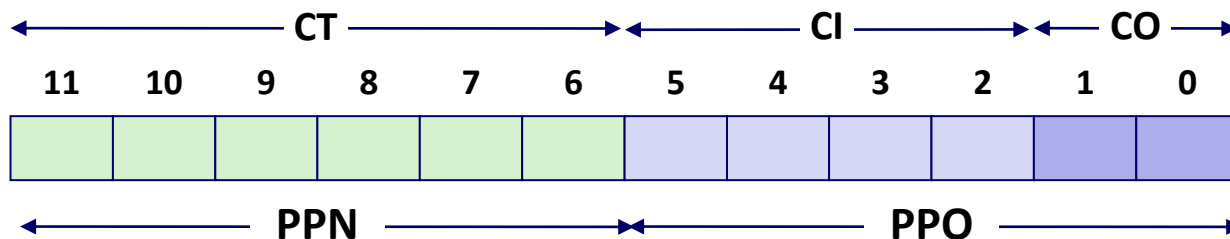
**Note:** It is just coincidence that the PPN is the same width as the cache Tag

❖ Virtual Address: 0x038F



VPN \_\_\_\_\_ TLBT \_\_\_\_\_ TLBI \_\_\_\_\_ TLB Hit? \_\_\_\_ Page Fault? \_\_\_\_ PPN \_\_\_\_\_

❖ Physical Address:

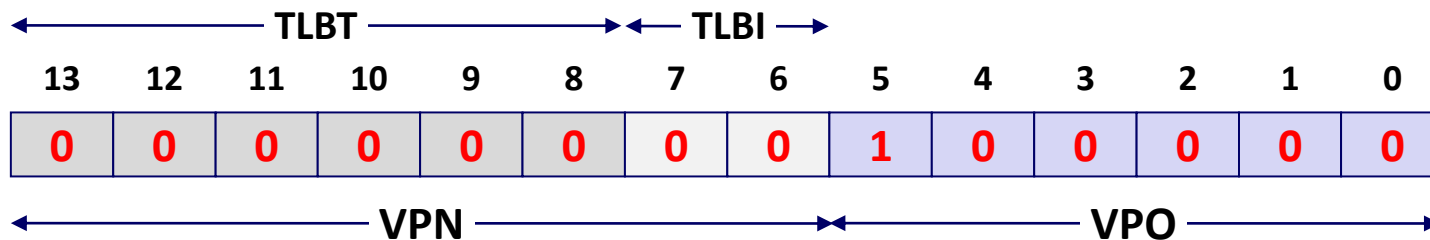


CT \_\_\_\_\_ CI \_\_\_\_\_ CO \_\_\_\_\_ Cache Hit? \_\_\_\_ Data (byte) \_\_\_\_\_

# Memory Request Example #3

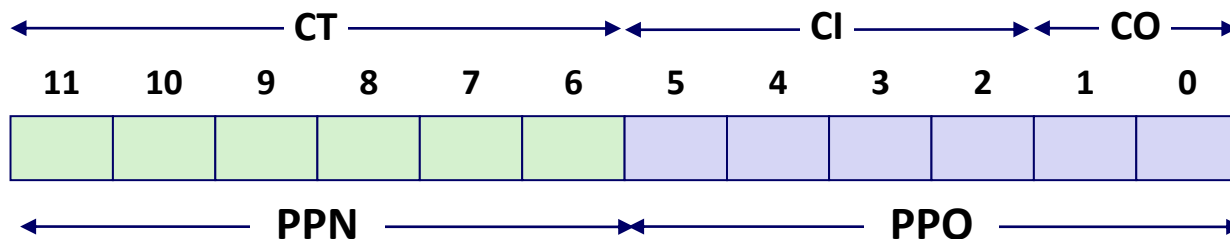
**Note:** It is just coincidence that the PPN is the same width as the cache Tag

❖ Virtual Address: 0x0020



VPN \_\_\_\_\_ TLBT \_\_\_\_\_ TLBI \_\_\_\_\_ TLB Hit? \_\_\_\_ Page Fault? \_\_\_\_ PPN \_\_\_\_\_

❖ Physical Address:

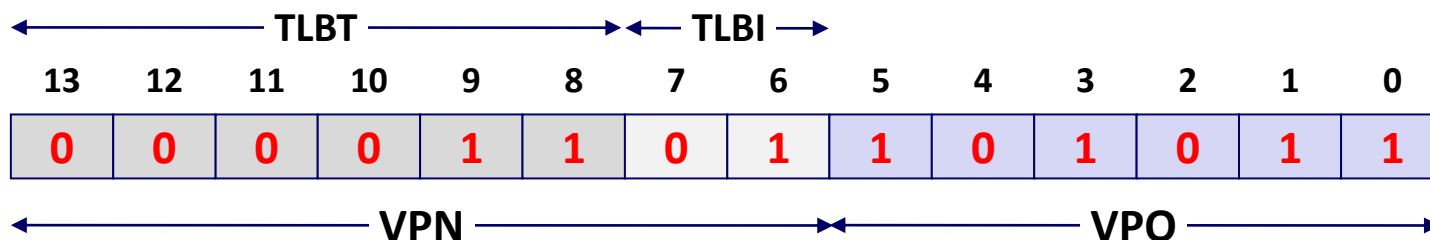


CT \_\_\_\_\_ CI \_\_\_\_\_ CO \_\_\_\_\_ Cache Hit? \_\_\_\_ Data (byte) \_\_\_\_\_

# Memory Request Example #4

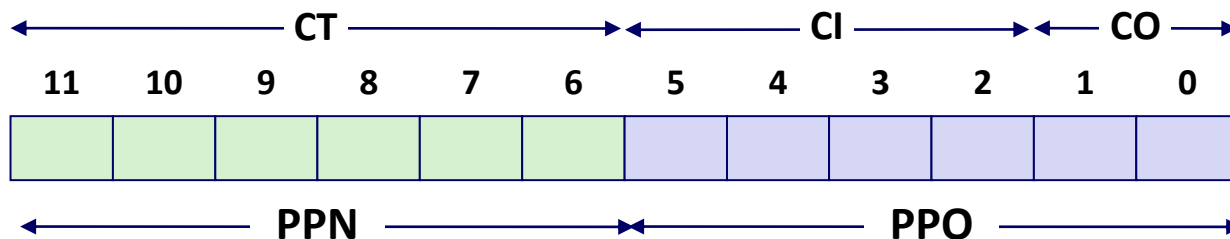
**Note:** It is just coincidence that the PPN is the same width as the cache Tag

❖ Virtual Address: 0x036B



VPN \_\_\_\_\_ TLBT \_\_\_\_\_ TLBI \_\_\_\_\_ TLB Hit? \_\_\_\_ Page Fault? \_\_\_\_ PPN \_\_\_\_\_

❖ Physical Address:



CT \_\_\_\_\_ CI \_\_\_\_\_ CO \_\_\_\_\_ Cache Hit? \_\_\_\_ Data (byte) \_\_\_\_\_

# Practice VM Question

- ❖ Our system has the following properties
  - 1 MiB of physical address space
  - 4 GiB of virtual address space
  - 32 KiB page size
  - 4-entry fully associative TLB with LRU replacement

a) Fill in the following blanks:

\_\_\_\_\_ Entries in a page table

\_\_\_\_\_ Minimum bit-width of  
PTBR

\_\_\_\_\_ TLBT bits

\_\_\_\_\_ Max # of valid entries  
in a page table

# Practice VM Question

- ❖ One process uses a page-aligned *square* matrix `mat [ ]` of 32-bit integers in the code shown below:

```
#define MAT_SIZE = 2048
for(int i = 0; i < MAT_SIZE; i++)
    mat[i*(MAT_SIZE+1)] = i;
```

- b) What is the largest stride (in bytes) between successive memory accesses (in the VA space)?

# Practice VM Question

- ❖ One process uses a page-aligned *square* matrix `mat []` of 32-bit integers in the code shown below:

```
#define MAT_SIZE = 2048
for(int i = 0; i < MAT_SIZE; i++)
    mat[i*(MAT_SIZE+1)] = i;
```

- c) Assuming all of `mat []` starts on disk, what are the following hit rates for the execution of the for-loop?

\_\_\_\_\_ TLB Hit Rate

\_\_\_\_\_ Page Table Hit Rate