CMPT 454 (Spring 2010) Assignment 2: Data Storage and Query Answering

Due: Monday, 2010-03-01, 11:29AM (at the beginning of class)

Instructions on Assignment Submission: Hard copy only!

- Option 1: drop off your assignments in the assignment box (with label CMPT 454) in CSIL.
- Option 2: bring your assignments to the class on the due day, and the instructor will collect the assignments **at the beginning of class**.

Please write legibly or typeset your answers using your favorite word processor. Late assignments will not be accepted unless there is a documented medical reason.

Problem 1.

(25 points) [Disk]

Consider a disk with a sector size of 512 bytes, 2000 tracks per surface, 50 sectors per track, 5 double-sided platters, average seek time of 10 milliseconds.

- (1) What is the capacity of a track in bytes? What is the capacity of each surface? What is the capacity of the disk?
- (2) How many cylinders does the disk have?
- (3) Give examples of valid block sizes. Is 256 bytes a valid block size? 2048? 51200?
- (4) If the disk platters rotate at 5400 rpm (revolutions per minute), what is the maximum rotational delay?
- (5) Assuming that one track of data can be transferred per revolution, what is the transfer rate?

For the following sub-questions, suppose that a block size of 1024 bytes is chosen. Suppose that a file containing 100,000 records of 100 bytes each is to be stored on such a disk and that no record is allowed to span two blocks,

- (6) how many records fit onto a block? How many blocks are required to store the entire file? If the file is arranged sequentially on disk, how many surfaces are needed?
- (7) How many records of 100 bytes each can be stored using this disk?
- (8) What is the time required to read a file containing 100,000 records of 100 bytes each sequentially?
- (9) What is the time required to read a file containing 100,000 records of 100 bytes each in some random order?

Problem 2.

(25 points) [Elevator Algorithm]

Suppose that we are scheduling I/O requests for one type of commercial disks. For simplicity, we assume that the seek time for the header to move across *n* cylinders is calculated as $1 + \frac{n}{4000}$

(milliseconds). The sum of average latency and transfer time is 4.3 milliseconds. Initially the head is at cylinder 32000, and then the following requests come in:

- time = 0; request for block on cylinder 8000 arrives;
- time = 1; request for block on cylinder 48000 arrives;
- time = 10; request for block on cylinder 4000 arrives;
- time = 20; request for block on cylinder 40000 arrives;
- (1) If we use the elevator scheduling algorithm, at what time is each request serviced completely?
- (2) If we use a first-come-first-served scheduler, at what time is each request serviced fully?

Problem 3.

(25 points) [B+-tree]



Figure 1: Problem 3.

Consider the B+ tree index (n = 4) shown in Figure 1.

- (1) Show the B+ tree that would result from inserting a data entry with key 3 into the original tree.
- (2) Show the B+ tree that would result from deleting the data entry with key 8 from the original tree, assuming that the left sibling is checked for possible redistribution.
- (3) Show the B+ tree that would result from deleting the data entry with key 8 from the original tree, assuming that the right sibling is checked for possible redistribution.
- (4) Show the B+ tree that would result from successively deleting the data entries with keys 32, 39, 41, 45, and 73 from the original tree.

Problem 4.

25 points) [Hash Table]

Consider the Extensible Hash table in Figure 2 with a block capacity of 2.

- (1) Show the Extensible Hash table after the insertion of search keys with the following hash values: 0010, 0110, 1001.
- (2) Give a hash key whose insertion (into the above hash table without the insertions from (1)) would require the creation of an overflow block. Show the resulting hash table.
- (3) Give a hash key whose deletion (from the above hash table without the insertions from (1)) would lead to a halving of the directory. Show the resulting hash table.



Figure 2: Problem 4.

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