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## **Equivalent Notations in Relational Algebra, Tuple Relational Calculus, and Domain Relational Calculus**

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### ***Select Operation***

$R = (A, B)$

Relational Algebra:  $\sigma_{B=17}(r)$

Tuple Calculus:  $\{t \mid t \in r \wedge B = 17\}$

Domain Calculus:  $\{\langle a, b \rangle \mid \langle a, b \rangle \in r \wedge b = 17\}$

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### ***Project Operation***

$R = (A, B)$

Relational Algebra:  $\Pi_A(r)$

Tuple Calculus:  $\{t \mid \exists p \in r (t[A] = p[A])\}$

Domain Calculus:  $\{\langle a \rangle \mid \exists b (\langle a, b \rangle \in r)\}$

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### ***Combining Operations***

$R = (A, B)$

Relational Algebra:  $\Pi_A(\sigma_{B=17}(r))$

Tuple Calculus:  $\{t \mid \exists p \in r (t[A] = p[A] \wedge p[B] = 17)\}$

Domain Calculus:  $\{\langle a \rangle \mid \exists b (\langle a, b \rangle \in r \wedge b = 17)\}$

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### **Natural Join**

$R = (A, B, C, D) \quad S = (B, D, E)$

Relational Algebra:  $r \bowtie s$

$$\Pi_{r.A, r.B, r.C, r.D, s.E}(\sigma_{r.B=s.B \wedge r.D=s.D}(r \times s))$$

Tuple Calculus:  $\{t \mid \exists p \in r \exists q \in s (t[A] = p[A] \wedge t[B] = p[B] \wedge t[C] = p[C] \wedge t[D] = p[D] \wedge t[E] = q[E] \wedge p[B] = q[B] \wedge p[D] = q[D])\}$

Domain Calculus:  $\{\langle a, b, c, d, e \rangle \mid \langle a, b, c, d \rangle \in r \wedge \langle b, d, e \rangle \in s\}$

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### **Union**

$R = (A, B, C) \quad S = (A, B, C)$

Relational Algebra:  $r \cup s$

Tuple Calculus:  $\{t \mid t \in r \vee t \in s\}$

Domain Calculus:  $\{\langle a, b, c \rangle \mid \langle a, b, c \rangle \in r \vee \langle a, b, c \rangle \in s\}$

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### ***Intersection***

$$R = (A, B, C) \quad S = (A, B, C)$$

Relational Algebra:  $r \cap s$

Tuple Calculus:  $\{t \mid t \in r \wedge t \in s\}$

Domain Calculus:  $\{<a, b, c> \mid <a, b, c> \in r \wedge <a, b, c> \in s\}$

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### ***Set Difference***

$$R = (A, B, C) \quad S = (A, B, C)$$

Relational Algebra:  $r - s$

Tuple Calculus:  $\{t \mid t \in r \wedge t \notin s\}$

Domain Calculus:  $\{<a, b, c> \mid <a, b, c> \in r \wedge <a, b, c> \notin s\}$

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### ***Cartesian/Cross Product***

$$R = (A, B) \quad S = (C, D)$$

Relational Algebra:  $r \times s$

Tuple Calculus:  $\{t \mid \exists p \in r \exists q \in s (t[A] = p[A] \wedge t[B] = p[B] \wedge t[C] = q[C] \wedge t[D] = q[D])\}$

Domain Calculus:  $\{<a, b, c, d> \mid <a, b> \in r \wedge <c, d> \in s\}$

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### **Division**

$$R = (A, B) \quad S = (B)$$

Relational Algebra:  $r \div s$

Tuple Calculus:  $\{t \mid \exists p \in r \ \forall q \in s (p[B] = q[B] \Rightarrow t[A] = p[A])\}$

Domain Calculus:  $\{\langle a \rangle \mid \langle a \rangle \in r \wedge \forall \langle b \rangle (\langle b \rangle \in s \Rightarrow \langle a, b \rangle \in r)\}$

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### **Use of the Universal Quantifier**

salary = (employee, salary-amount)

To find the maximum salary-amount:

(Extended) Relational Algebra:

$$\max_{\text{salary-amount}}(\text{salary})$$

Tuple Calculus:

$$\{t \mid \forall p \in \text{salary} \Rightarrow p[\text{salary-amount}] \leq t[\text{salary-amount}]\}$$

Domain Calculus:

$$\{\langle s \rangle \mid \exists e (\langle e, s \rangle \in \text{salary} \wedge \forall e_1, s_1 (\langle e_1, s_1 \rangle \in \text{salary} \Rightarrow s_1 \leq s))\}$$

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