

Introduction

Course Info

● Instructor: Evgeny Skvortsov

- Email: evgenys@sfu.ca
- Room: TASC 9000
- Office hours (tentative):
Tuesday 17:30 – 18:30

● Teaching Assistants:

- Shekoofeh Rizi, email: sna36@sfu.ca
- Yuanbin Shen, email: yuanbin.shen@gmail.com

● Course webpage:

- <http://www.cs.sfu.ca/CC/101.MACM/evgenys>

Course Info

● Course objective:

To introduce basic concepts and applications of discrete mathematics.

● Syllabus:

- Logic and Formal Reasoning
- Set Theory, Functions and Relations
- Mathematical Induction
- Combinatorics
- Growth of Functions
- Number Theory
- Automata and Formal Languages (if time permits)

Course Info

● Textbook:

R. P. Grimaldi, *Discrete and Combinatorial Mathematics (an Applied Introduction)*, Addison-Wesley, 2004.

- It is impossible to finish studying all the contents of the textbook in one semester. The contents not covered in lectures/slides are not required.
- The content and order of topics, as presented in the class, do not one-to-one correspond to any part of the book. Use of Subject Index is advised.
- In a few cases the notation and terminology in the class differs from that in the book

Course Info

● References:

- H. Rosen, *Discrete Mathematics and Its Applications*, 5/E, McGraw-Hill, 2003.
- R. L. Graham; D. E. Knuth; and O. Patashnik, *Concrete Mathematics*, Addison-Wesley, Reading, MA, 1994
- T. H. Cormen, C. E. Leiserson, R. L. Rivest, and C. Stein, *Introduction to Algorithms*, 2nd Edition, MIT Press, Cambridge, MA, 2001.
- G. Andrews, *Number theory*, Saunders or Dover Publications, Inc.
- H. Enderton, *A Mathematical Introduction to Logic*, Harcourt/Academic Press, 2001

Course Info

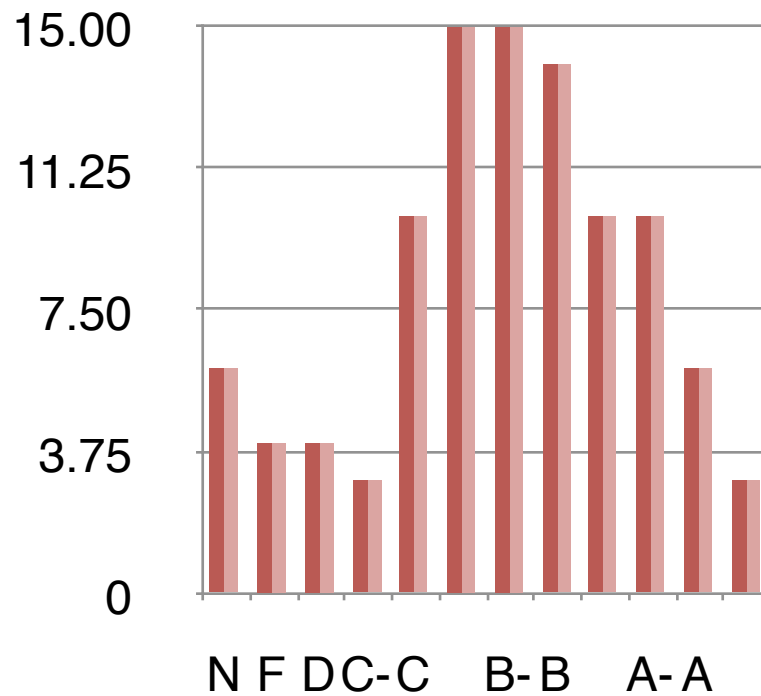
● Grading:

- 10 Tutorials attendance ($10 \times 1\%$)
- 5 Assignments ($5 \times 5\%$)
- 2 Midterms ($2 \times 15\%$)
- 1 Final Exam 35%

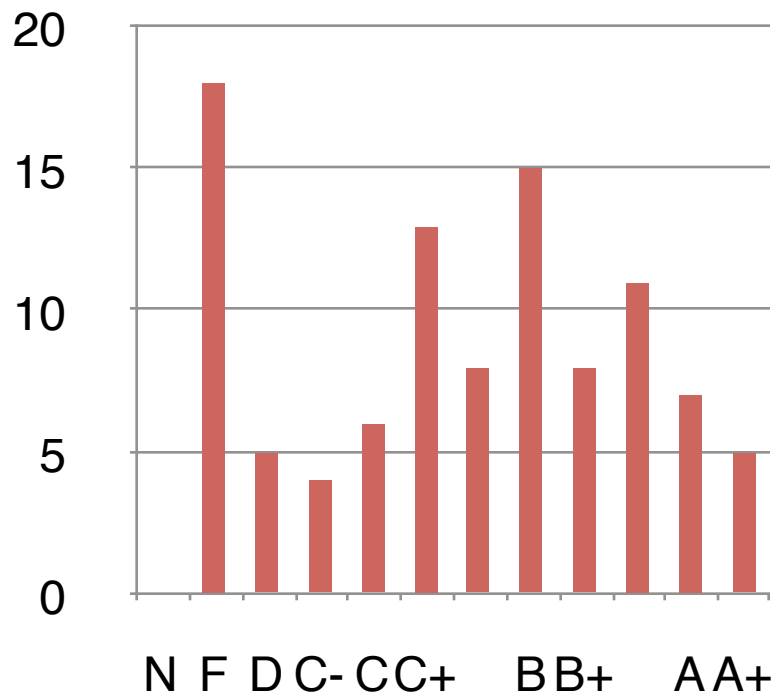
Course Info

● Previous results:

2007



2008



Prerequisites

- Not much of specific knowledge
- Some general knowledge is needed, as there will be examples
- Modest math erudition (e.g., 5th Euclid's postulate, see next slide)
- Basics

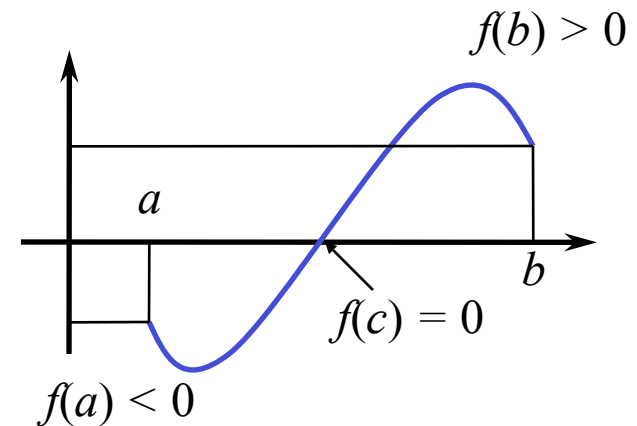
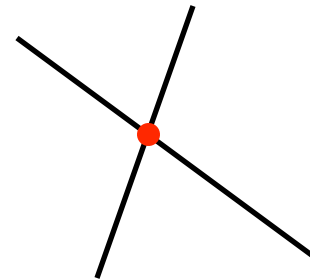
$$2 \times 2 = 4$$

$$7 \times 8 = \cancel{55}^{56}$$

Two Mathematics

Continuous Mathematics

- Fifth Euclid's Postulate
- Intermediate value theorem



Continuous Mathematics (cntd)

- Laws of Physics

$$\vec{F} = m \frac{d^2 X}{dt^2}$$

Newton's second law of motion

$$\nabla \times \mathbf{E} = \frac{\partial \mathbf{B}}{\partial t}$$

Maxwell's law of electromagnetism

- Disciplines: geometry, calculus, differential equations, topology, ...
- Applications: physics, engineering, astronomy, ...

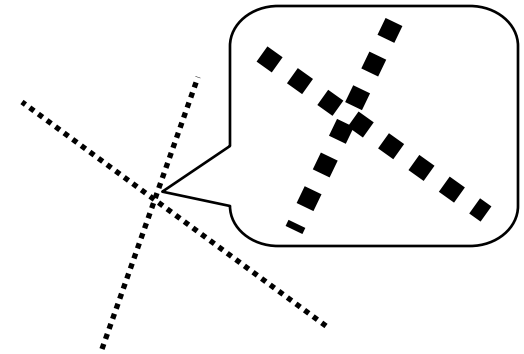
Discrete Mathematics

- Discrete Mathematics comprises all branches of mathematics that do not use the idea of continuity.
- `Formal' definition (Wikipedia):

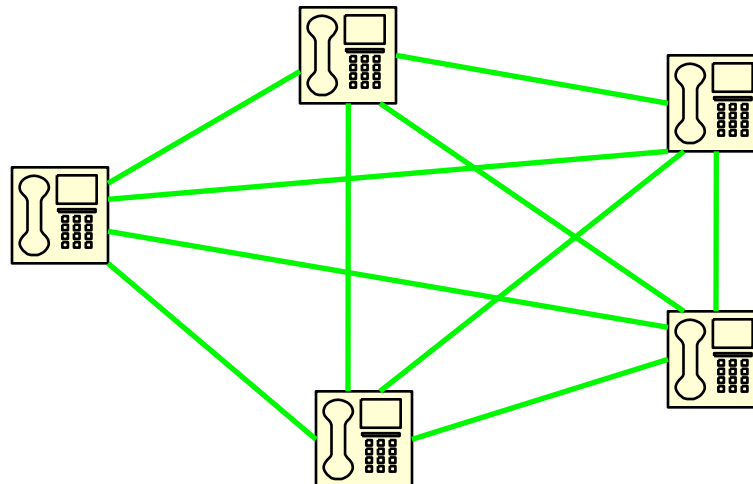
Discrete mathematics, sometimes called **finite mathematics**, is the study of mathematical structures that are fundamentally discrete, in the sense of not supporting or requiring the notion of continuity. Most, if not all, of the objects studied in finite mathematics are countable sets, such as the integers. For contrast, see continuum, topology, and mathematical analysis

Discrete Mathematics (cntd)

- Removing continuity
 - Discrete fifth Euclid's Postulate (???)

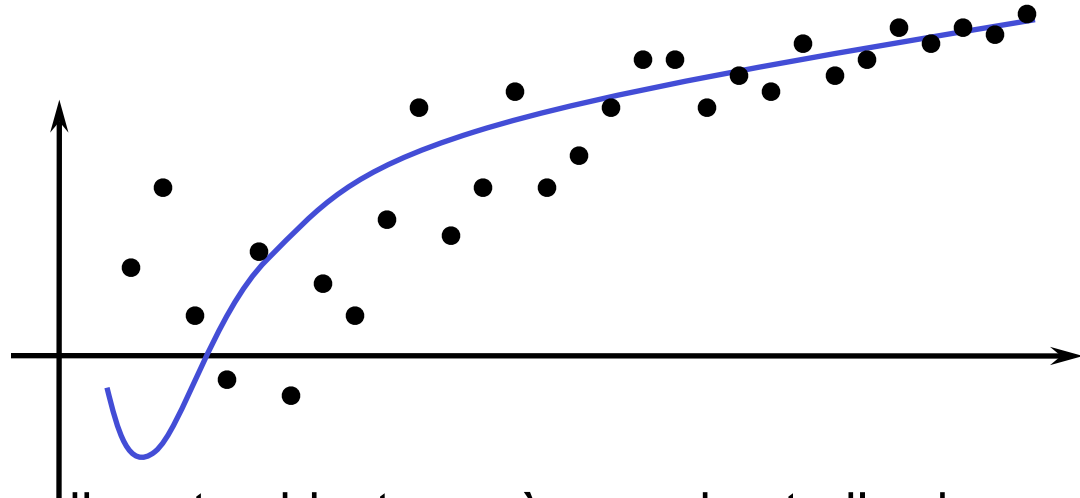


- Graphs



Discrete Mathematics (cntd)

- Asymptotics



Properties of a discrete objects are 'approximated' using a continuous function

- Laws of discrete mathematics:

$$((\forall x F(x) \Rightarrow G(x)) \& F(a)) \Rightarrow G(a)$$

The rule of universal specification

$$X^n + Y^n = Z^n \quad \text{does not hold for any } n > 2 \text{ and integer } X, Y, Z$$

Great Fermat's Theorem

Topics in DM

- Wikipedia says that Discrete mathematics usually includes:
 - logic - a study of reasoning
 - set theory - a study of collections of elements
 - number theory
 - combinatorics - a study of counting
 - graph theory
 - algorithmics - a study of methods of calculation
 - information theory
 - the theory of computability and complexity - a study on theoretical limitations on algorithms ...
- algebra – a study of algebraic systems (Bulatov)
- discrete probability theory (Grimaldi)

This is too much for us !!

CS at SFU:

MATH-232 Elementary linear algebra
CMPT-413 Computational linguistics
CMPT-379 Principles of compiler design
CMPT-384 Symbolic computing
CMPT-307 Data structures and algorithms
CMPT-308 Computability and complexity
CMPT-405 Design and analysis of
 computing algorithms
CMPT-406 Computational geometry
CMPT-407 Computational complexity
CMPT-408 Theory of computer networks /
 communications
MACM-300 Introduction to formal languages
 and automata
MACM-401 Symbolic computation

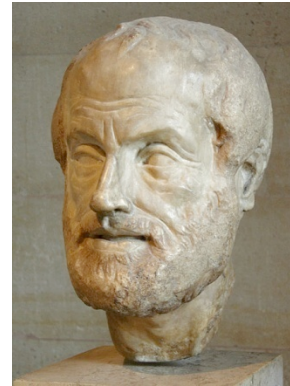
CMPT-477 Introduction to formal
 verification
CMPT-705 Design and analysis of
 algorithms
CMPT-706 Parallel algorithms
CMPT-710 Computational complexity
CMPT-725 Logical methods in
 computational intelligence
CMPT-813 Computational geometry
CMPT-815 Algorithms of optimization
CMPT-816 Theory of communication
 networks
CMPT-721 Knowledge representation
 and reasoning
CMPT-814 Algorithmic graph theory

Our goal

is to learn basic concepts and terminology that provide basis and common language for those and many other courses.

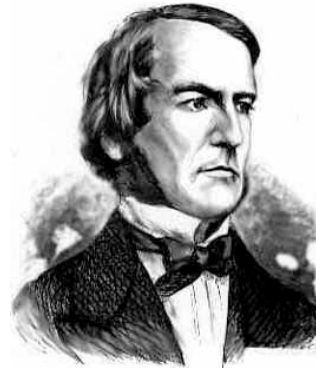
Logic

- Formal logic, syllogisms



Aristotle
384 - 322 B.C.

- Mathematical logic, formal reasoning



George Boole
1815 - 1864

- Computational logic, formal verification



Pentium FDIV bug
1994

- Other applications: artificial intelligence, robotics, software verification, automated theorem proving, ...

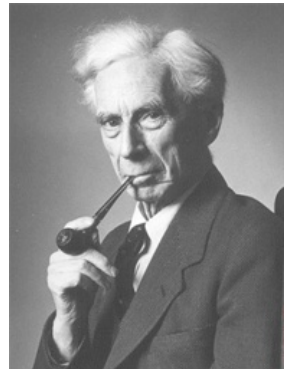
Set theory

● Naïve set theory



Georg Cantor
1845 - 1918

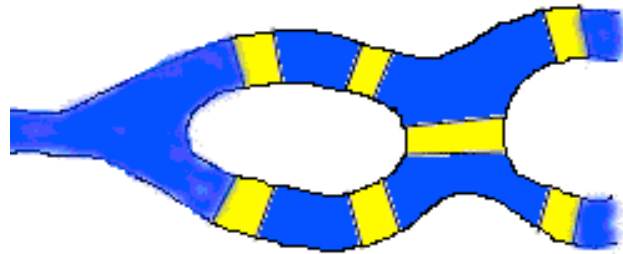
● Axiomatic set theory



Bertrand Russell
1872 - 1970

Graphs

- Toy graph theory
Konigsberg 7-bridge problem



Leonard Euler
1707 - 1783

- Other applications: modeling of nearly everything,
electric circuits, networking, linguistics, data storage, coding
theory, games, scheduling, combinatorial algorithms, ...

- One more face



Paul Erdős
1913 - 1996

Number Theory

● Arithmetic (*Arithmetica*)

● Number theory

● Algebraic geometry

● Other applications: cryptography

?



Diophantus
200 - 284

Pierre de Fermat
1608 - 1672

Andrew Wiles
1953 - ?