

# Introduction

## Course Info

### ● Instructor: Evgeny Skvortsov

- Email: [evgenys@sfu.ca](mailto:evgenys@sfu.ca)
- Room: TASC 9000
- Office hours (tentative):  
Tuesday 17:30 – 18:30

### ● Teaching Assistants:

- Shekoofeh Rizi, email: [sna36@sfu.ca](mailto:sna36@sfu.ca)
- Yuanbin Shen, email: [yuanbin.shen@gmail.com](mailto:yuanbin.shen@gmail.com)

### ● Course webpage:

- <http://www.cs.sfu.ca/CC/101.MACM/evgenys>

# Course Info

## ● Course objective:

To introduce basic concepts and applications of discrete mathematics.

## ● Syllabus:

- Logic and Formal Reasoning
- Set Theory, Functions and Relations
- Mathematical Induction
- Combinatorics
- Growth of Functions
- Number Theory
- Automata and Formal Languages (if time permits)

# Course Info

## ● Textbook:

R. P. Grimaldi, *Discrete and Combinatorial Mathematics (an Applied Introduction)*, Addison-Wesley, 2004.

- It is impossible to finish studying all the contents of the textbook in one semester. The contents not covered in lectures/slides are not required.
- The content and order of topics, as presented in the class, do not one-to-one correspond to any part of the book. Use of Subject Index is advised.
- In a few cases the notation and terminology in the class differs from that in the book

## Course Info

### ● References:

- H. Rosen, *Discrete Mathematics and Its Applications*, 5/E, McGraw-Hill, 2003.
- R. L. Graham; D. E. Knuth; and O. Patashnik, *Concrete Mathematics*, Addison-Wesley, Reading, MA, 1994
- T. H. Cormen, C. E. Leiserson, R. L. Rivest, and C. Stein, *Introduction to Algorithms*, 2nd Edition, MIT Press, Cambridge, MA, 2001.
- G. Andrews, *Number theory*, Saunders or Dover Publications, Inc.
- H. Enderton, *A Mathematical Introduction to Logic*, Harcourt/Academic Press, 2001

# Course Info

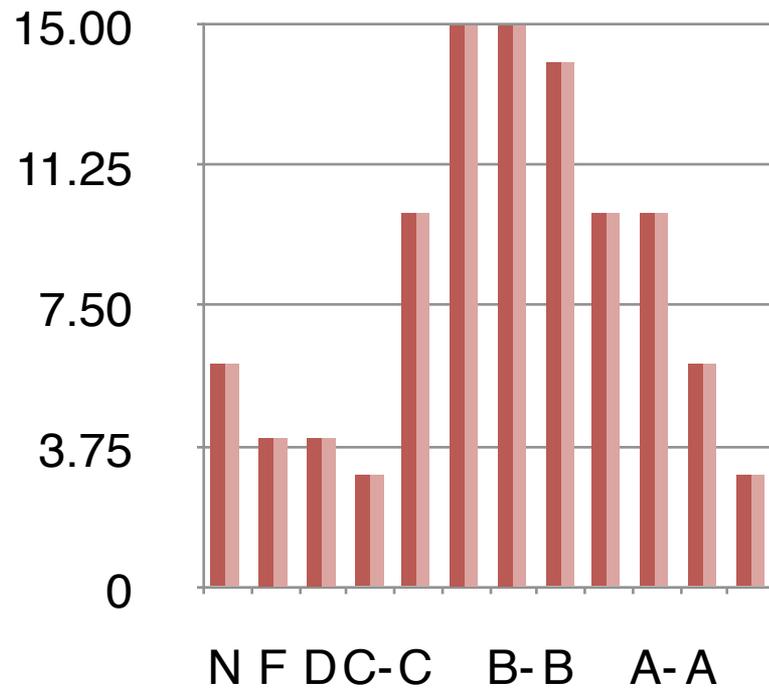
## ● Grading:

- 10 Tutorials attendance ( $10 \times 1\%$ )
- 5 Assignments ( $5 \times 5\%$ )
- 2 Midterms ( $2 \times 15\%$ )
- 1 Final Exam 35%

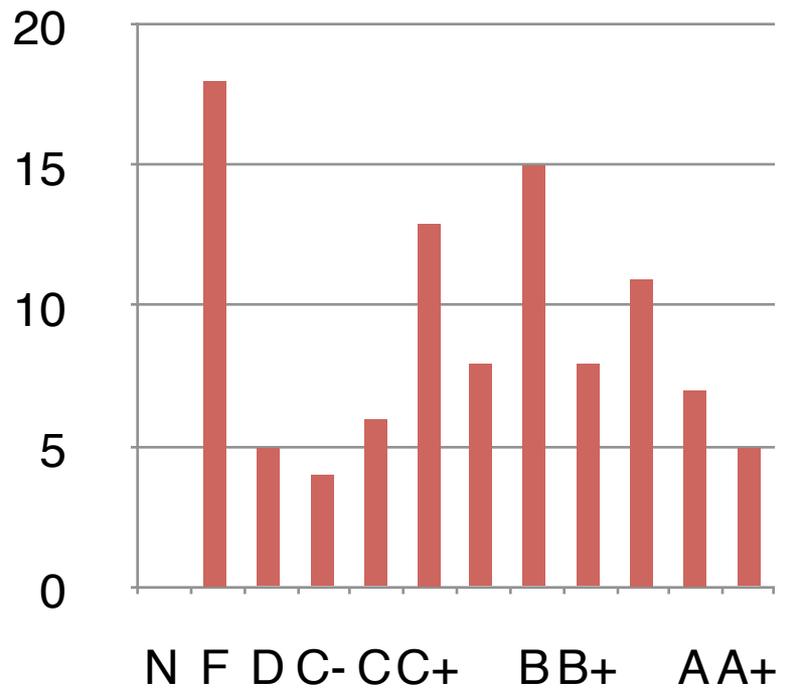
# Course Info

● Previous results:

## 2007



## 2008



# Prerequisites

- Not much of specific knowledge
- Some general knowledge is needed, as there will be examples
- Modest math erudition (e.g., 5th Euclid's postulate, see next slide)
- Basics

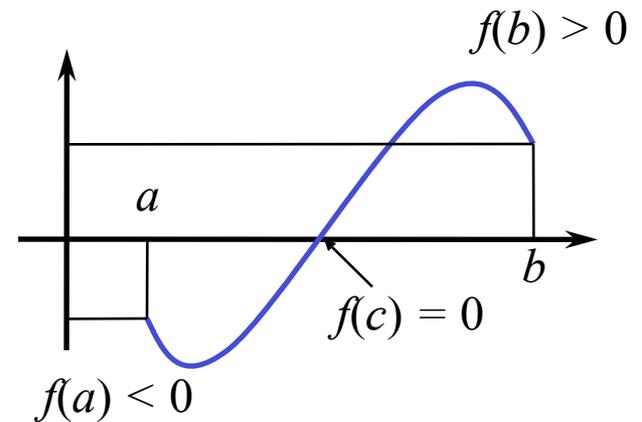
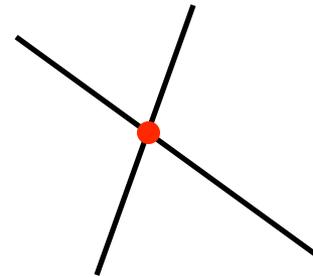
$$2 \times 2 = 4$$

$$7 \times 8 = \del{55}^{56}$$

# Two Mathematics

## Continuous Mathematics

- Fifth Euclid's Postulate
- Intermediate value theorem



## Continuous Mathematics (cntd)

- Laws of Physics

$$\vec{F} = m \frac{d^2 X}{dt^2}$$

Newton's second law of motion

$$\nabla \times \mathbf{E} = \frac{\partial \mathbf{B}}{\partial t}$$

Maxwell's law of electromagnetism

- Disciplines: geometry, calculus, differential equations, topology, ...
- Applications: physics, engineering, astronomy, ...

# Discrete Mathematics

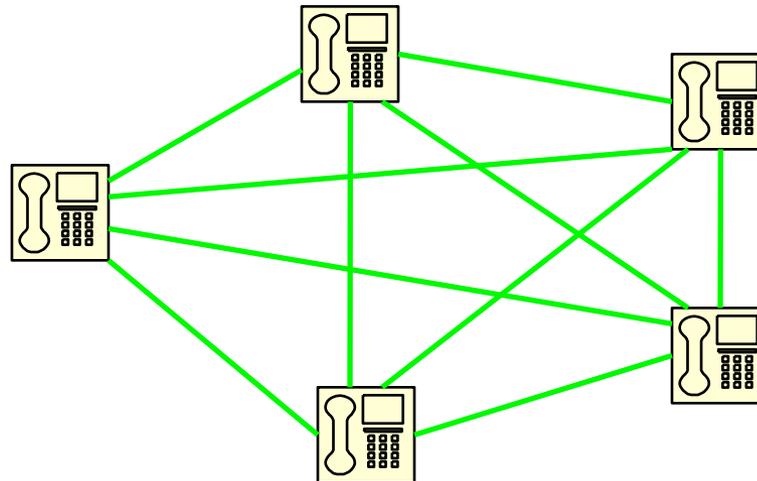
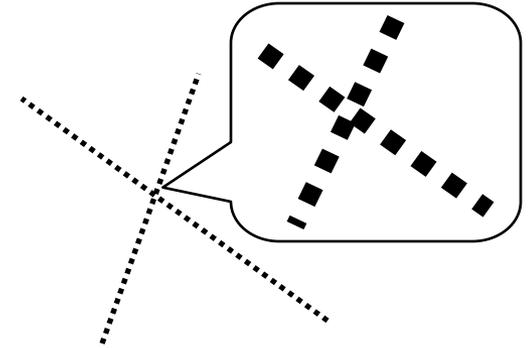
- Discrete Mathematics comprises all branches of mathematics that do not use the idea of continuity.

- `Formal' definition (Wikipedia):

**Discrete mathematics**, sometimes called **finite mathematics**, is the study of mathematical structures that are fundamentally discrete, in the sense of not supporting or requiring the notion of continuity. Most, if not all, of the objects studied in finite mathematics are countable sets, such as the integers. For contrast, see continuum, topology, and mathematical analysis

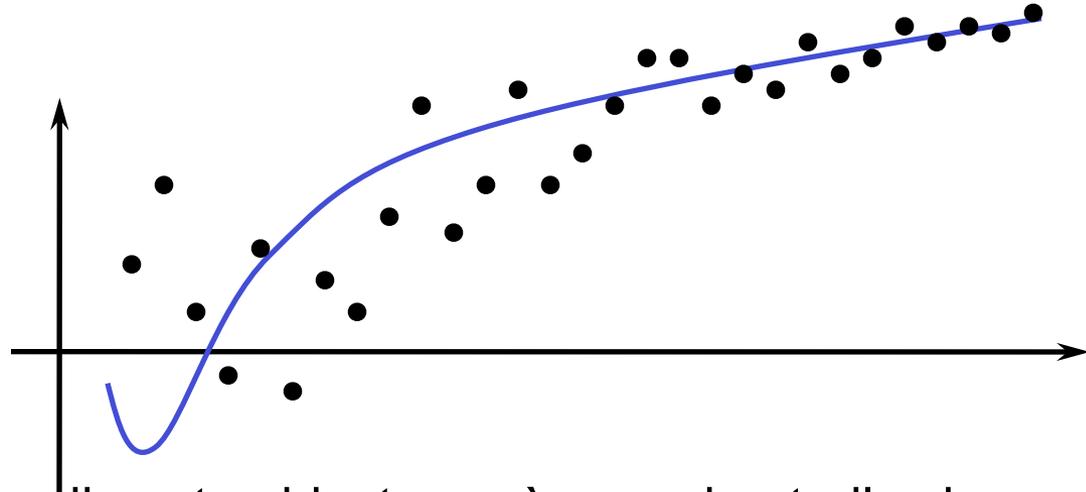
# Discrete Mathematics (cntd)

- Removing continuity
  - Discrete fifth Euclid's Postulate (???)
  
- Graphs



## Discrete Mathematics (cntd)

- Asymptotics



Properties of a discrete objects are 'approximated' using a continuous function

- Laws of discrete mathematics:

$$((\forall x F(x) \Rightarrow G(x)) \& F(a)) \Rightarrow G(a)$$

The rule of universal specification

$$X^n + Y^n = Z^n \quad \text{does not hold for any } n > 2 \text{ and integer } X, Y, Z$$

Great Fermat's Theorem

## Topics in DM

- Wikipedia says that Discrete mathematics usually includes:
  - logic - a study of reasoning
  - set theory - a study of collections of elements
  - number theory
  - combinatorics - a study of counting
  - graph theory
  - algorithmics - a study of methods of calculation
  - information theory
  - the theory of computability and complexity - a study on theoretical limitations on algorithms ...
  
  - algebra – a study of algebraic systems (Bulatov)
  - discrete probability theory (Grimaldi)

# This is too much for us !!

## CS at SFU:

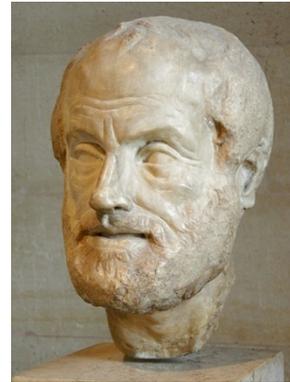
MATH-232	Elementary linear algebra	CMPT-477	Introduction to formal verification
CMPT-413	Computational linguistics	CMPT-705	Design and analysis of algorithms
CMPT-379	Principles of compiler design	CMPT-706	Parallel algorithms
CMPT-384	Symbolic computing	CMPT-710	Computational complexity
CMPT-307	Data structures and algorithms	CMPT-725	Logical methods in computational intelligence
CMPT-308	Computability and complexity	CMPT-813	Computational geometry
CMPT-405	Design and analysis of computing algorithms	CMPT-815	Algorithms of optimization
CMPT-406	Computational geometry	CMPT-816	Theory of communication networks
CMPT-407	Computational complexity	CMPT-721	Knowledge representation and reasoning
CMPT-408	Theory of computer networks / communications	CMPT-814	Algorithmic graph theory
MACM-300	Introduction to formal languages and automata		
MACM-401	Symbolic computation		

## **Our goal**

is to learn basic concepts and terminology that provide basis and common language for those and many other courses.

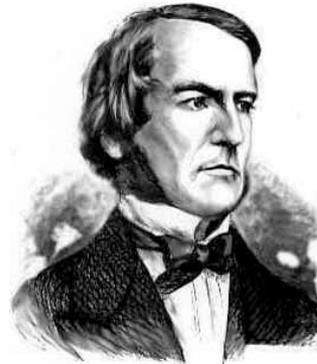
# Logic

- Formal logic, syllogisms



Aristotle  
384 - 322 B.C.

- Mathematical logic, formal reasoning



George Boole  
1815 - 1864

- Computational logic, formal verification



Pentium FDIV bug  
1994

- Other applications: artificial intelligence, robotics, software verification, automated theorem proving, ...

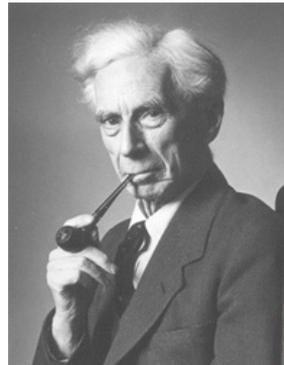
# Set theory

● Naïve set theory



Georg Cantor  
1845 - 1918

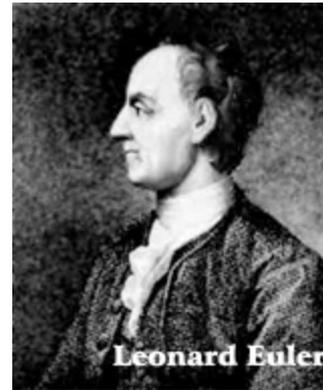
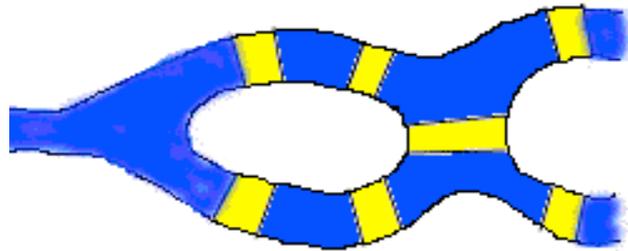
● Axiomatic set theory



Bertrand Russell  
1872 - 1970

# Graphs

- Toy graph theory  
Konigsberg 7-bridge problem



Leonard Euler  
1707 - 1783

- Other applications: modeling of nearly everything,  
electric circuits, networking, linguistics, data storage, coding  
theory, games, scheduling, combinatorial algorithms, ...

- One more face



Paul Erdős  
1913 - 1996

# Number Theory

● Arithmetic (*Arithmetica*)

● Number theory

● Algebraic geometry

● Other applications: cryptography

?



Diophantus  
200 - 284

Pierre de Fermat  
1608 - 1672

Andrew Wiles  
1953 - ?