Cutting Images: Graphs and Boundary Finding

“The Double Secret”, Magritte
Last class: texture synthesis and transfer
Last class: in-painting
This Lecture: Finding Seams and Boundaries

Segmentation
This Lecture: Finding Seams and Boundaries

Retargeting

http://swieskowski.net/carve/
This Lecture: Finding Seams and Boundaries

Stitching
This Lecture: Finding seams and boundaries

Fundamental Concept: The Image as a Graph

- Intelligent Scissors: Good boundary = short path
- Graph cuts: Good region has low cutting cost
Semi-automated segmentation

User provides imprecise and incomplete specification of region – your algorithm has to read his/her mind.

Key problems
1. What groups of pixels form cohesive regions?
2. What pixels are likely to be on the boundary of regions?
3. Which region is the user trying to select?
What makes a good region?

• Contains small range of color/texture
• Looks different than background
• Compact
What makes a good boundary?

• High gradient along boundary
• Gradient in right direction
• Smooth
The Image as a Graph

Node: pixel

Edge: cost of path or cut between two pixels
Intelligent Scissors

Mortenson and Barrett (SIGGRAPH 1995)
Intelligent Scissors

Mortenson and Barrett (SIGGRAPH 1995)

A good image boundary has a short path through the graph.
Intelligent Scissors

- Formulation: find good boundary between seed points
- Challenges
  - Minimize interaction time
  - Define what makes a good boundary
  - Efficiently find it
Intelligent Scissors: method

1. Define boundary cost between neighboring pixels
2. User specifies a starting point (seed)
3. Compute lowest cost from seed to each other pixel
4. Get path from seed to cursor, choose new seed, repeat
Intelligent Scissors: method

1. Define boundary cost between neighboring pixels
   a) Lower if edge is present (e.g., with \texttt{edge(im, 'canny')})
   b) Lower if gradient is strong
   c) Lower if gradient is in direction of boundary
Gradients, Edges, and Path Cost

Gradient Magnitude

Edge Image

Path Cost
Intelligent Scissors: method

1. Define boundary cost between neighboring pixels
2. User specifies a starting point (seed)
   - Snapping
Intelligent Scissors: method

1. Define boundary cost between neighboring pixels
2. User specifies a starting point (seed)
3. Compute lowest cost from seed to each other pixel
   – Djikstra’s shortest path algorithm
Djikstra’s shortest path algorithm

Initialize, given seed \( s \):
- Compute \( \text{cost}_2(q,r) \) \% cost for boundary from pixel \( q \) to neighboring pixel \( r \)
- \( \text{cost}(s) = 0 \) \% total cost from seed to this point
- \( A = \{ s \} \) \% set to be expanded
- \( E = \{ \} \) \% set of expanded pixels
- \( P(q) \) \% pointer to pixel that leads to \( q \)

Loop while \( A \) is not empty
1. \( q = \) pixel in \( A \) with lowest cost
2. Add \( q \) to \( E \)
3. for each pixel \( r \) in neighborhood of \( q \) that is not in \( E \)
   a) \( \text{cost}_\text{tmp} = \text{cost}(q) + \text{cost}_2(q,r) \)
   b) if \( (r \text{ is not in } A) \text{ OR } (\text{cost}_\text{tmp} < \text{cost}(r)) \)
      i. \( \text{cost}(r) = \text{cost}_\text{tmp} \)
      ii. \( P(r) = q \)
      iii. Add \( r \) to \( A \)
Example of Djikstra’s algorithm

```
Start

1  1  2  1  1  1
  1  1  1  4  9
```

Connections:
- Start to 1 through 5
- Start to 2 through 2
- Start to 3 through 3
- Start to 4 through 4
- Start to 5 through 3
- Start to 6 through 6
Where will intelligent scissors work well, or have problems?
Grab cuts and graph cuts

Magic Wand (198?)

Intelligent Scissors
Mortensen and Barrett (1995)

GrabCut

User Input

Result

Regions

Boundary

Regions & Boundary

Source: Rother
Segmentation with graph cuts

\[ \text{Energy}(\mathbf{y}; \theta, \text{data}) = \sum_i \psi_1(y_i; \theta, \text{data}) \sum_{i,j \in \text{edges}} \psi_2(y_i, y_j; \theta, \text{data}) \]
Segmentation with graph cuts

\[ \text{Energy}(\mathbf{y}; \theta, \text{data}) = \sum_i \psi_1(y_i; \theta, \text{data}) \sum_{ij \in \text{edges}} \psi_2(y_i, y_j; \theta, \text{data}) \]
Graph cuts segmentation

1. Define graph
   - usually 4-connected or 8-connected

2. Set weights to foreground/background
   - Color histogram or mixture of Gaussians for background and foreground
     \[
     \text{unary\_potential}(x) = -\log\left( \frac{P(c(x); \theta_{\text{foreground}})}{P(c(x); \theta_{\text{background}})} \right)
     \]

3. Set weights for edges between pixels
   \[
   \text{edge\_potential}(x, y) = k_1 + k_2 \exp \left\{ -\frac{\| c(x) - c(y) \|^2}{2\sigma^2} \right\}
   \]

4. Apply min-cut/max-flow algorithm

5. Return to 2, using current labels to compute foreground, background models
Colour Model

Gaussian Mixture Model (typically 5-8 components)

Source: Rother
What is easy or hard about these cases for graphcut-based segmentation?
Easier examples

GrabCut – Interactive Foreground Extraction
More difficult Examples

Camouflage & Low Contrast

Initial Rectangle

Initial Result

Fine structure

Harder Case

GrabCut – Interactive Foreground Extraction
Lazy Snapping (Li et al. SG 2004)
Other applications: Seam Carving

Seam Carving – Avidan and Shamir (2007)

Demo: http://swieskowski.net/carve/
Other applications: Seam Carving

- Find shortest path from top to bottom (or left to right), where cost = gradient magnitude

http://www.youtube.com/watch?v=6NciJXTlugc

Demo: http://swieskowski.net/carve/

Seam Carving – Avidan and Shamir (2007)
Other applications: stitching

Graphcut Textures – Kwatra et al. SIGGRAPH 2003
Other applications: stitching

Graphcut Textures – Kwatra et al. SIGGRAPH 2003

Ideal boundary:
1. Similar color in both images
2. High gradient in both images
Summary of big ideas

• Treat image as a graph
  – Pixels are nodes
  – Between-pixel edge weights based on gradients
  – Sometimes per-pixel weights for affinity to foreground/background

• Good boundaries are a short path through the graph (Intelligent Scissors, Seam Carving)

• Good regions are produced by a low-cost cut (GrabCuts, Graph Cut Stitching)